

# Natural Language Processing Sequence Labeling and Hidden Markov Models

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# Overview

- The Sequence Labeling (or Tagging) Problem
- Generative models, and the noisy-channel model, for supervised learning
- Hidden Markov Model (HMM) taggers
  - Basic definitions
  - Parameter estimation
  - The Viterbi algorithm

This slides are based on the course material by Michael Collins: <http://www.cs.columbia.edu/~mcollins/cs4705-spring2019/slides/tagging.pdf>

## Sequence Labeling or Tagging Tasks

- Sequence Labeling or Tagging is a task in NLP different from document classification.
- Here the goal is to map a sentence represented as a sequence of tokens  $x_1, x_2, \dots, x_n$  into a sequence of tags or labels  $y_1, y_2, \dots, y_n$ .
- Well known examples of this task are Part-of-Speech (POS) tagging and Named Entity Recognition (NER) to be presented next.

# Part-of-Speech Tagging

**INPUT:** Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results.

**OUTPUT:** Profits/**N** soared/**V** at/**P** Boeing/**N** Co./**N** ,/, easily/**ADV** topping/**V** forecasts/**N** on/**P** Wall/**N** Street/**N** ,/, as/**P** their/**POSS** CEO/**N** Alan/**N** Mulally/**N** announced/**V** first/**ADJ** quarter/**N** results/**N** ./.

- **N** = Noun
- **V** = Verb
- **P** = Preposition
- **Adv** = Adverb
- **Adj** = Adjective
- ...

# Part-of-Speech Tag Descriptions

	Tag	Description	Example
Open Class	<b>ADJ</b>	Adjective: noun modifiers describing properties	<i>red, young, awesome</i>
	<b>ADV</b>	Adverb: verb modifiers of time, place, manner	<i>very, slowly, home, yesterday</i>
	<b>NOUN</b>	words for persons, places, things, etc.	<i>algorithm, cat, mango, beauty</i>
	<b>VERB</b>	words for actions and processes	<i>draw, provide, go</i>
	<b>PROPN</b>	Proper noun: name of a person, organization, place, etc..	<i>Regina, IBM, Colorado</i>
	<b>INTJ</b>	Interjection: exclamation, greeting, yes/no response, etc.	<i>oh, um, yes, hello</i>
Closed Class Words	<b>ADP</b>	Adposition (Preposition/Postposition): marks a noun's spacial, temporal, or other relation	<i>in, on, by, under</i>
	<b>AUX</b>	Auxiliary: helping verb marking tense, aspect, mood, etc.,	<i>can, may, should, are</i>
	<b>CCONJ</b>	Coordinating Conjunction: joins two phrases/clauses	<i>and, or, but</i>
	<b>DET</b>	Determiner: marks noun phrase properties	<i>a, an, the, this</i>
	<b>NUM</b>	Numeral	<i>one, two, first, second</i>
	<b>PART</b>	Particle: a function word that must be associated with another word	<i>'s, not, (infinitive) to</i>
	<b>PRON</b>	Pronoun: a shorthand for referring to an entity or event	<i>she, who, I, others</i>
Other	<b>SCONJ</b>	Subordinating Conjunction: joins a main clause with a subordinate clause such as a sentential complement	<i>that, which</i>
	<b>PUNCT</b>	Punctuation	<i>; , ()</i>
	<b>SYM</b>	Symbols like \$ or emoji	<i>\$, %</i>
	<b>X</b>	Other	<i>asdf, qwfg</i>

Source: [Jurafsky and Martin, 2008]

# Named Entity Recognition (NER)

A **named entity** is, roughly speaking, anything that can be referred to with a named entity proper name: a person, a location, an organization.

**INPUT:** Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results.

**OUTPUT:** Profits soared at [Company Boeing Co.], easily topping forecasts on [Location Wall Street], as their CEO [Person Alan Mulally] announced first quarter results.

- Since entities can span multiple words (i.e., a span recognition problem), we can use BIO tagging [Ramshaw and Marcus, 1999] to turn the problem into a sequence labeling problem.
- BIO tagging: use tags that capture both the boundary and the named entity type.

# BIO tagging: NER as Sequence Labeling

**INPUT:** Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results.

**OUTPUT:** Profits/O soared/O at/O Boeing/B-C Co./I-C ,/O easily/O topping/O forecasts/O on/O Wall/B-L Street/I-L ,/O as/O their/O CEO/O Alan/B-P Mulally/I-P announced/O first/O quarter/O results/O ./O

- O = Outside (no entity)
- B-C = Begin Company
- I-C = Inside Company
- B-L = Begin Location
- I-L = Inside Location
- B-P = Begin Person
- I-P = Inside Person

# Our Goal

## Training set:

1. Pierre/NNP Vinken/NNP ,/, 61/CD years/NNS old/JJ ,/, will/MD join/VB the/DT board/NN as/IN a/DT nonexecutive/JJ director/NN Nov./NNP 29/CD ./.
2. Mr./NNP Vinken/NNP is/VBZ chairman/NN of/IN Elsevier/NNP N.V./NNP ,/, the/DT Dutch/NNP publishing/VBG group/NN ./.
3. Rudolph/NNP Agnew/NNP ,/, 55/CD years/NNS old/JJ and/CC chairman/NN of/IN Consolidated/NNP Gold/NNP Fields/NNP PLC/NNP ,/, was/VBD named/VBN a/DT nonexecutive/JJ director/NN of/IN this/DT British/JJ industrial/JJ conglomerate/NN ./.
4. ...

**Our Goal:** From the training set, induce a function/algorithm that maps new sentences to their tag sequences.



## Two Types of Constraints

Influential/JJ members/NNS of/IN the/DT House/NNP  
Ways/NNP and/CC Means/NNP Committee/NNP  
introduced/VBD legislation/NN that/WDT would/MD restrict/VB  
how/WRB the/DT new/JJ savings-and-loan/NN bailout/NN  
agency/NN can/MD raise/VB capital/NN ./.

### “Local”:

- e.g., “can” is more likely to be a modal verb MD rather than a noun NN

### “Contextual”:

- e.g., a noun is much more likely than a verb to follow a determiner

### Sometimes these preferences are in conflict:

- The trash can is in the garage

# Sequence Labeling as Supervised Learning

- We have a sequence of inputs  $x = (x_1, x_2, \dots, x_n)$  and corresponding labels  $y = (y_1, y_2, \dots, y_n)$ .
- Task is to learn a function  $f$  that maps input sequences to label sequences:  $f(x_1, x_2, \dots, x_n) = y_1, y_2, \dots, y_n$ .
- We have a training set of labeled sequences:  
 $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), \dots, (x^{(m)}, y^{(m)})\}$ .

# Generative Approach for Sequence Labeling

- Generative models such as Naive Bayes was used for classification can also be used for sequence labeling tasks in NLP.
- Approach:
  - Training: Learn the joint distribution  $p(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n)$  of input sequences.
  - Decoding: Use the learned distribution to predict label sequences for new input sequences.
- Decoding in sequence labeling involves finding the label sequence with the highest joint probability:  $\arg \max_{y_1, y_2, \dots, y_n} p(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n)$ .

# Hidden Markov Models

- Hidden Markov Models (HMMs) provide a principled way to handle sequence labeling problems using generative modeling and efficient decoding algorithms.
- We have an input sentence  $x = x_1, x_2, \dots, x_n$  ( $x_i$  is the  $i$ -th word in the sentence).
- We have a tag sequence  $y = y_1, y_2, \dots, y_n$  ( $y_i$  is the  $i$ -th tag in the sentence).
- We'll use an HMM to define  $p(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n)$  for any sentence  $x_1, \dots, x_n$  and tag sequence  $y_1, \dots, y_n$  of the same length. [Kupiec, 1992]
- Then, the most likely tag sequence for  $x$  is:

$$\arg \max_{y_1, \dots, y_n} p(x_1, \dots, x_n, y_1, \dots, y_n)$$

## Trigram Hidden Markov Models (Trigram HMMs)

For any sentence  $x_1, \dots, x_n$  where  $x_i \in V$  for  $i = 1, \dots, n$ , and any tag sequence  $y_1, \dots, y_{n+1}$  where  $y_i \in S$  for  $i = 1, \dots, n$ , and  $y_{n+1} = \text{STOP}$ , the joint probability of the sentence and tag sequence is:

$$p(x_1, \dots, x_n, y_1, \dots, y_{n+1}) = \prod_{i=1}^{n+1} q(y_i | y_{i-2}, y_{i-1}) \prod_{i=1}^n e(x_i | y_i)$$

where we have assumed that  $x_0 = x_{-1} = *$ .

## Parameters of the Model

- $q(s|u, v)$  for any  $s \in S \cup \{\text{STOP}\}$ ,  $u, v \in S \cup \{*\}$ 
  - The value for  $q(s|u, v)$  can be interpreted as the probability of seeing the tag  $s$  immediately after the bigram of tags  $(u, v)$ .
- $e(x|s)$  for any  $s \in S$ ,  $x \in V$ 
  - The value for  $e(x|s)$  can be interpreted as the probability of seeing observation  $x$  paired with state  $s$ .

## An Example

If we have  $n = 3$ ,  $x_1, x_2, x_3$  equal to the sentence "the dog laughs", and  $y_1, y_2, y_3, y_4$  equal to the tag sequence "D N V STOP", then:

$$\begin{aligned} p(x_1, \dots, x_n, y_1, \dots, y_{n+1}) = & q(D|*, *) \times q(N|*, D) \\ & \times q(V|D, N) \times q(\text{STOP}|N, V) \\ & \times e(\text{the}|D) \times e(\text{dog}|N) \times e(\text{laughs}|V) \end{aligned}$$

- STOP is a special tag that terminates the sequence.
- We take  $y_0 = y_{-1} = *$ , where  $*$  is a special "padding" symbol.

# Independence Assumptions in Trigram HMMs

- Trigram Hidden Markov Models (HMMs) are derived by making specific independence assumptions in the model.
- Consider two sequences of random variables:  $X_1, \dots, X_n$  and  $Y_1, \dots, Y_n$ , where  $n$  is the length of the sequences.
- Each  $X_i$  can take any value in a finite set  $V$  of words, and each  $Y_i$  can take any value in a finite set  $K$  of possible tags (e.g.,  $K = \{D, N, V \dots\}$ ).
- Our goal is to model the joint probability:

$$\begin{aligned} P(x_1, x_2, \dots, x_n, y_1, \dots, y_n) \\ &= p(y_1) \times p(y_2|y_1) \\ &\quad \times \dots \\ &\quad \times p(y_n|y_{n-1}, y_{n-2}, \dots y_1) \\ &\quad \times p(x_1|y_n, y_{n-1}, \dots y_1) \\ &\quad \times p(x_2|x_1, y_n, y_{n-1}, \dots y_1) \\ &\quad \times p(x_n|x_{n-1}, \dots, x_1, y_n, y_{n-1}, \dots y_1) \end{aligned}$$

- We define an additional random variable  $Y_{n+1}$  that always takes the value "STOP."



# Independence Assumptions in Trigram HMMs

- The key idea in HMMs is the factorization of the joint probability:

$$P(X_1 = x_1, \dots, X_n = x_n, Y_1 = y_1, \dots, Y_{n+1} = y_{n+1}) \\ = \prod_{i=1}^{n+1} P(Y_i = y_i | Y_{i-2} = y_{i-2}, Y_{i-1} = y_{i-1}) \times \prod_{i=1}^n P(X_i = x_i | Y_i = y_i)$$

- We first assume that:

$$P(Y_i = y_i | Y_{i-2} = y_{i-2}, Y_{i-1} = y_{i-1}) = q(y_i | y_{i-2}, y_{i-1})$$

- This assumes that the sequence  $Y_1, \dots, Y_{n+1}$  is a second-order Markov sequence, where each state depends only on the previous two states.
- And we also assume that:

$$P(X_i = x_i | Y_i = y_i) = e(x_i | y_i)$$

- This assumes that the value of the random variable  $X_i$  depends only on the value of  $Y_i$ .
- These independence assumptions allow for the derivation of the joint probability equation.

## Why the Name?

$$\begin{aligned} p(x_1, \dots, x_n, y_1, \dots, y_n) &= q(\text{STOP} | y_{n-1}, y_n) \\ &\times \prod_{j=1}^n q(y_j | y_{j-2}, y_{j-1}) \\ &\times \prod_{j=1}^n e(x_j | y_j) \end{aligned}$$

- Markov Chain component:

$$q(\text{STOP} | y_{n-1}, y_n) \times \prod_{j=1}^n q(y_j | y_{j-2}, y_{j-1})$$

These transitions are not directly observed for a given sequence of words  $(x_1, \dots, x_n)$ , hence the name “hidden”.

- Observed component:

$$\prod_{j=1}^n e(x_j | y_j)$$

The observed component of HMMs models the emission probabilities of observed symbols ( $x$ 's) conditioned on the corresponding hidden states ( $y$ 's).

## Smoothed Estimation

$$\begin{aligned} q(Vt|DT, JJ) = & \lambda_1 \times \frac{\text{Count}(Dt, JJ, Vt)}{\text{Count}(Dt, JJ)} \\ & + \lambda_2 \times \frac{\text{Count}(JJ, Vt)}{\text{Count}(JJ)} \\ & + \lambda_3 \times \frac{\text{Count}(Vt)}{\text{Count}()} \end{aligned}$$

where  $\lambda_1 + \lambda_2 + \lambda_3 = 1$ , and for all  $i$ ,  $\lambda_i \geq 0$ .

$$e(\text{base}|Vt) = \frac{\text{Count}(Vt, \text{base})}{\text{Count}(Vt)}$$

# Dealing with Low-Frequency Words

A common method is as follows:

- Step 1: Split vocabulary into two sets
  - Frequent words = words occurring  $\geq 5$  times in training
  - Low frequency words = all other words
- Step 2: Map low frequency words into a small, finite set, depending on prefixes, suffixes, etc.

# Dealing with Low-Frequency Words: An Example

Below is an example of word classes for named entity recognition [Bikel et al., 1999]:

Word class	Example	Intuition
twoDigitNum	90	Two-digit year
fourDigitNum	1990	Four-digit year
containsDigitAndAlpha	A8956 – 67	Product code
containsDigitAndDash	09 – 96	Date
containsDigitAndSlash	11/9/89	Date
containsDigitAndComma	23,000.00	Monetary amount
containsDigitAndPeriod	1.00	Monetary amount, percentage
othernum	456789	Other number
allCaps	BBN	Organization
capPeriod	M.	Person name initial
firstWord	First word of sentence	No useful capitalization information
initCap	Sally	Capitalized word
lowercase	can	Uncapitalized word
other	,	Punctuation marks, all other words

# Dealing with Low-Frequency Words: An Example

**Original Sentence:** Profits/O soared/O at/O Boeing/B-C Co./I-C ,/O easily/O topping/O forecasts/O on/O Wall/B-L Street/I-L ,/O as/O their/O CEO/O Alan/B-P Mulally/I-P announced/O first/O quarter/O results/O ./O

## Transformed Sentence:

firstword/O soared/O at/O initCap/B-C Co./I-C ,/O easily/O lowercase/O forecasts/O on/O initCap/B-L Street/I-L ,/O as/O their/O CEO/O Alan/B-P initCap/I-P announced/O first/O quarter/O results/O ./O

- O = Outside (no entity)
- B-C = Begin Company
- I-C = Inside Company
- B-L = Begin Location
- I-L = Inside Location
- B-P = Begin Person
- I-P = Inside Person

## Decoding Problem

Decoding Problem: For an input  $x_1 \dots x_n$ , find

$$\arg \max_{y_1 \dots y_{n+1}} p(x_1 \dots x_n, y_1 \dots y_{n+1})$$

where the  $\arg \max$  is taken over all sequences  $y_1 \dots y_{n+1}$  such that  $y_i \in S$  for  $i = 1 \dots n$ , and  $y_{n+1} = \text{STOP}$ .

We assume that  $p$  takes the form:

$$p(x_1 \dots x_n, y_1 \dots y_{n+1}) = \prod_{i=1}^{n+1} q(y_i | y_{i-2}, y_{i-1}) \prod_{i=1}^n e(x_i | y_i)$$

Recall that we have assumed in this definition that

$y_0 = y_{-1} = *$ , and  $y_{n+1} = \text{STOP}$ .

# Naive Brute Force Method

The naive, brute force method for finding the highest scoring tag sequence is to enumerate all possible tag sequences  $y_1, \dots, y_{n+1}$ , score them under the function  $p$ , and select the sequence with the highest score.

- Example:
  - Input sentence: *the dog barks*
  - Set of possible tags:  $K = \{D, N, V\}$
- Enumerate all possible tag sequences:
  - *D D D STOP*
  - *D D N STOP*
  - *D D V STOP*
  - *D N D STOP*
  - *D N N STOP*
  - *D N V STOP*
  - ...



# Naive Brute Force Method

- In this case, there are  $3^3 = 27$  possible sequences.
- However, for longer sentences, this method becomes inefficient.
- For an input sentence of length  $n$ , there are  $|K|^n$  possible tag sequences.
- The exponential growth makes brute-force search infeasible for reasonable length sentences.

# Viterbi Decoding Dynamic Programming

- The algorithm used by HMMs to perform efficient decoding is called Viterbi decoding.
- Viterbi decoding uses dynamic programming.
- Dynamic programming is a technique for solving optimization problems by breaking them down into overlapping subproblems.
- It stores the solutions to these subproblems in a table so that they do not have to be recalculated.
- Dynamic programming can greatly improve the efficiency of algorithms.
- Next, we show how dynamic programming works with two examples: Factorial and Fibonacci

# Factorial

- Recursive implementation:

```
def recur_factorial(n):  
    # Base case  
    if n == 1:  
        return n  
    else:  
        return n * recur_factorial(n-1)
```

- Dynamic programming implementation:

```
def dynamic_factorial(n):  
    table = [0 for i in range(0, n+1)]  
  
    # Base case  
    table[0] = 1  
  
    for i in range(1, len(table)):  
        table[i] = i * table[i-1]  
  
    return table[n]
```

# Fibonacci

- Recursive implementation:

```
def recur_fibonacci(n):  
    if n == 1 or n == 0:  
        return 1  
    else:  
        return recur_fibonacci(n-1) + recur_fibonacci(n-2)
```

- Dynamic programming implementation:

```
def dynamic_fibonacci(n):  
    table = [0 for i in range(0, n+1)]  
  
    # Base case  
    table[0] = 1  
    table[1] = 1  
  
    for i in range(2, len(table)):  
        table[i] = table[i-1] + table[i-2]  
  
    return table[n]
```

# Complexity

- In recursive implementations, the complexity can be quite high due to repeated calculations of the same subproblems.
- However, dynamic programming can significantly reduce the complexity by storing the solutions to subproblems in a table or array and reusing them when needed.
- This approach eliminates the redundant calculations and allows for a more efficient computation.
- For the case of Fibonacci the complexity is reduced from exponential to linear.

# The Viterbi Algorithm

The Viterbi algorithm efficiently computes the maximum probability of a tag sequence by using dynamic programming.

## Definitions:

- Define  $n$  as the length of the sentence.
- Define  $S_k$  for  $k = -1 \dots n$  as the set of possible tags at position  $k$ :  
 $S_{-1} = S_0 = \{*\}$ ,  $S_k = S$  for  $k \in \{1 \dots n\}$ .
- Define a truncated version of the probability encoded by the HMM until position  $k$ ,  $r(y_{-1}, y_0, y_1, \dots, y_k)$  as:

$$r(y_{-1}, y_0, y_1, \dots, y_k) = \prod_{i=1}^k q(y_i | y_{i-2}, y_{i-1})$$

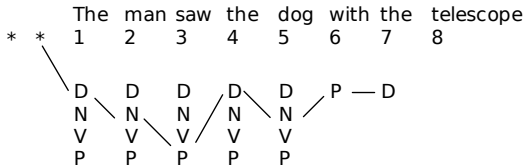
- Define a dynamic programming table  $\pi(k, u, v)$  as the maximum probability of a tag sequence ending in tags  $u, v$  at position  $k$ :

$$\pi(k, u, v) = \max_{y_{-1}, y_0, y_1, \dots, y_k : y_{k-1}=u, y_k=v} r(y_{-1}, y_0, y_1, \dots, y_k)$$

# An Example

Recall that  $\pi(k, u, v)$  is maximum probability of a tag sequence ending in tags  $u, v$  at position  $k$

$$S = \{D, N, P, V\}$$



- There are many possible sequences of tags.
- Each of them has a probability calculated from the parameters  $q$  and  $e$ .
- $\pi(7, P, D)$  is the maximum probability that one of these tag sequences ends in  $P$   $D$  at position 7.
- The path represents the sequence with the maximum probability.

# A Recursive Definition

**Base case:**

$$\pi(0, *, *) = 1$$

**Recursive definition:** For any  $k \in \{1 \dots n\}$ , for any  $u \in S_{k-1}$  and  $v \in S_k$ :

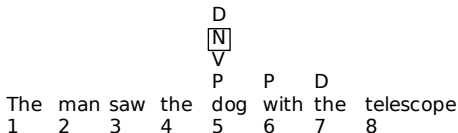
$$\pi(k, u, v) = \max_{w \in S_{k-2}} (\pi(k-1, w, u) \times q(v|w, u) \times e(x_k|v))$$



# Justification for the Recursive Definition

For any  $k \in \{1 \dots n\}$ , for any  $u \in S_{k-1}$  and  $v \in S_k$ :

$$\pi(k, u, v) = \max_{w \in S_{k-2}} (\pi(k-1, w, u) \times q(v|w, u) \times e(x_k|v))$$



$$S_5 = \mathcal{S} = \{D, N, V, P\}$$

$$\Pi(7, P, D) = \max_{w \in S_5} (\Pi(6, w, P) \times q(D|w, P) \times e(\text{the}|D))$$

- Let's consider an arbitrary tag sequence that ends with tags  $P$  and  $D$  at position 7.
- It must contain some tag at position 5.
- We are basically searching for the tag that maximizes the probability at position 5.

# The Viterbi Algorithm

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**Algorithm 1:** Viterbi Algorithm

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**Input:** a sentence  $x_1 \dots x_n$ , parameters  $q(s|u, v)$  and  $e(x|s)$

**Initialization:** Set  $\pi(0, *, *) = 1$ ;  $S_{-1} = S_0 = \{*\}$ ,  $S_k = S$   
for  $k \in \{1 \dots n\}$ .

**for**  $k = 1$  **to**  $n$  **do**

**for**  $u \in S_{k-1}, v \in S_k$  **do**

$$\pi(k, u, v) = \max_{w \in S_{k-2}} (\pi(k-1, w, u) \times q(v|w, u) \times e(x_k|v))$$

**end**

**end**

**return**  $(\max_{u \in S_{n-1}, v \in S_n} (\pi(n, u, v) \times q(STOP|u, v)))$

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# The Viterbi Algorithm with Backpointers

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## Algorithm 2: Viterbi Algorithm with Backpointers

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**Input:** a sentence  $x_1 \dots x_n$ , parameters  $q(s|u, v)$  and  $e(x|s)$

**Initialization:** Set  $\pi(0, *, *) = 1$ ;  $S_{-1} = S_0 = \{*\}$ ,  $S_k = S$  for  $k \in \{1 \dots n\}$ .

```
for  $k = 1$  to  $n$  do
    for  $u \in S_{k-1}, v \in S_k$  do
         $\pi(k, u, v) = \max_{w \in S_{k-2}} (\pi(k-1, w, u) \times q(v|w, u) \times e(x_k|v))$ 
         $\text{bp}(k, u, v) = \arg \max_{w \in S_{k-2}} (\pi(k-1, w, u) \times q(v|w, u) \times e(x_k|v))$ 
    end
end
 $(y_{n-1}, y_n) = \arg \max_{(u, v)} (\pi(n, u, v) \times q(\text{STOP}|u, v))$ ;           // Find maximum
probability and corresponding tags
for  $k = (n-2)$  to  $1$  do
     $y_k = \text{bp}(k+2, y_{k+1}, y_{k+2})$ ;           // Retrieve tag sequence using
backpointers
end
return(the tag sequence  $y_1 \dots y_n$ ); // Return the final tag sequence
```

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## The Viterbi Algorithm: Running Time

- $O(n|S|^3)$  time to calculate  $q(s|u, v) \times e(x_k|s)$  for all  $k, s, u, v$ .
- $n|S|^2$  entries in  $\pi$  to be filled in.
- $O(|S|)$  time to fill in one entry.

$\Rightarrow O(n|S|^3)$  time in total.

## Pros and Cons

- Hidden Markov Model (HMM) taggers are simple to train (compile counts from training corpus).
- They perform relatively well (over 90% performance on named entity recognition).
- Main difficulty is modeling  $e(\text{word}|\text{tag})$ , which can be very complex if "words" are complex.

Questions?

Thanks for your Attention!

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