# Natural Language Processing Text Classification and Naïve Bayes

Felipe Bravo-Marquez

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## Is this spam?

Subject: Important notice!

From: Stanford University <newsforum@stanford.edu>

Date: October 28, 2011 12:34:16 PM PDT

To: undisclosed-recipients:;

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This slides are based on the course material by Daniel Jurafsky:

https://web.stanford.edu/~jurafsky/slp3/4.pdf

## Who wrote which Federalist papers?

- 1787-8: Anonymous essays attempted to convince New York to ratify the U.S Constitution: Jay, Madison, Hamilton.
- Authorship of 12 of the letters is in dispute.
- 1963: Solved by Mosteller and Wallace using Bayesian methods.

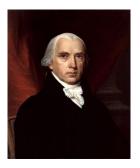


Figure: James Madison

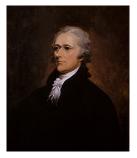


Figure: Alexander Hamilton

## What is the subject of this medical article?

#### MEDLINE Article



#### **MeSH Subject Category Hierarchy**

Antogonists and Inhibitors

**Blood Supply** 

Chemistry

**Drug Therapy** 

Embryology

Epidemiology

• • •

## Positive or negative movie review?

- + ...zany characters and richly applied satire, and some great plot twists
- It was pathetic. The worst part about it was the boxing scenes...
- + ...awesome caramel sauce and sweet toasty almonds. I love this place!
- ...awful pizza and ridiculously overpriced...

## Why sentiment analysis?

- Movie: Is this review positive or negative?
- Products: What do people think about the new iPhone?
- Public sentiment: How is consumer confidence?
- Politics: What do people think about this candidate or issue?
- Prediction: Predict election outcomes or market trends from sentiment.

## Scherer Typology of Affective States

- Emotion: Brief organically synchronized ... evaluation of a major event
  - Angry, sad, joyful, fearful, ashamed, proud, elated
- Mood: Diffuse non-caused low-intensity long-duration change in subjective feeling
  - Cheerful, gloomy, irritable, listless, depressed, buoyant
- Interpersonal stances: Affective stance toward another person in a specific interaction
  - Friendly, flirtatious, distant, cold, warm, supportive, contemptuous
- Attitudes: Enduring, affectively colored beliefs, dispositions towards objects or persons
  - Liking, loving, hating, valuing, desiring
- Personality traits: Stable personality dispositions and typical behavior tendencies
  - Nervous, anxious, reckless, morose, hostile, jealous

#### **Basic Sentiment Classification**

Sentiment analysis is the detection of attitudes.

- Simple task we focus on in this class
  - Is the attitude of this text positive or negative?

## Summary: Text Classification

Text classification can be applied to various tasks, including:

- Sentiment analysis
- Spam detection
- Authorship identification
- Language identification
- Assigning subject categories, topics, or genres
- ...

#### Text Classification: Definition

#### Input:

- A document d
- A fixed set of classes  $C = \{c_1, c_2, \dots, c_J\}$

**Output**: A predicted class  $c \in C$ 

#### Classification Methods: Hand-coded rules

Rules based on combinations of words or other features

- Spam: black-list-address OR ("dollars" AND "you have been selected")
- Accuracy can be high if rules carefully refined by experts
- But building and maintaining these rules is expensive

## Classification Methods: Supervised Machine Learning

#### Input:

- A document d
- A fixed set of classes  $C = \{c_1, c_2, \dots, c_J\}$
- A training set of m hand-labeled documents:  $(d_1, c_1), (d_2, c_2), \dots, (d_m, c_m)$

#### Output:

• A learned classifier  $\gamma: d \rightarrow c$ 

# Classification Methods: Supervised Machine Learning

#### Any kind of classifier can be used:

- Naïve Bayes
- Logistic regression
- Neural networks
- k-Nearest Neighbors

## Naive Bayes Intuition

Naive Bayes is a simple ("naive") classification method based on Bayes' rule.

 Relies on a very simple representation of a document: Bag of words

## The Bag of Words Representation

I love this movie! It's sweet, but with satirical humor. The dialogue is great and the adventure scenes are fun... It manages to be whimsical and romantic while laughing at the conventions of the fairy tale genre. I would recommend it to just about anyone. I've seen it several times, and I'm always happy to see it again whenever I have a friend who hasn't seen it yet!



## Bayes' Rule Applied to Documents and Classes

For a document *d* and a class *c*:

$$P(c|d) = \frac{P(d|c)P(c)}{P(d)}$$

## Naive Bayes Classifier (I)

MAP stands for "maximum a posteriori," which represents the most likely class:

$$c_{\mathsf{MAP}} = \arg\max_{c \in C} P(c|d)$$

To calculate the most likely class, we apply Bayes' rule:

$$=\arg\max_{c\in C}\frac{P(d|c)P(c)}{P(d)}$$

Finally, we can drop the denominator since it remains constant for all classes:

$$= \arg \max_{c \in C} P(d|c)P(c)$$

## Naive Bayes Classifier (II)

To classify document d, we use the MAP estimate:

$$c_{\mathsf{MAP}} = \arg\max_{c \in C} P(d|c)P(c)$$

- The document d is represented as a set of features x<sub>1</sub>, x<sub>2</sub>,..., x<sub>n</sub>.
- The classifier calculates the conditional probability of the features given a class and the prior probability of the class:

$$=\arg\max_{c\in C}P(x_1,x_2,\ldots,x_n|c)P(c)$$

- The term  $P(x_1, x_2, ..., x_n | c)$  represents the "likelihood" of the features given the class.
- The term P(c) represents the "prior" probability of the class.

## Naïve Bayes Classifier (IV)

 The Naïve Bayes classifier calculates the MAP estimate by considering the likelihood and prior probabilities:

$$c_{\mathsf{MAP}} = \arg\max_{c \in C} P(x_1, x_2, \dots, x_n | c) P(c)$$

- The probability of the features given the class,  $P(x_1, x_2, ..., x_n | c)$ , can be estimated by counting the relative frequencies in a corpus.
- The prior probability of the class, P(c), represents how often this class occurs.
- The Naïve Bayes classifier requires estimating  $O(|X|^n \cdot |C|)$  parameters, where |X| is the number of distinct features and n is the length of the document.
- Accurate estimation of these parameters would require a very large number of training examples.

## Multinomial Naive Bayes Independence Assumptions

- Bag of Words assumption: We assume that the position of words in the document does not matter.
- Conditional Independence assumption: We assume that the feature probabilities  $P(x_i|c_i)$  are independent given the class  $c_i$ .
- In the Multinomial Naive Bayes classifier, the probability of a document with features  $x_1, x_2, \ldots, x_n$  given class c can be calculated as:

$$P(x_1, x_2, ..., x_n | c) = P(x_1 | c) \cdot P(x_2 | c) \cdot P(x_3 | c) \cdot ... \cdot P(x_n | c)$$

## Multinomial Naive Bayes Classifier

 The Maximum A Posteriori (MAP) estimate for class c in the Multinomial Naive Bayes classifier is given by:

$$c_{\mathsf{MAP}} = \arg\max_{c \in C} P(x_1, x_2, \dots, x_n | c) P(c)$$

Alternatively, we can write it as:

$$c_{\mathsf{NB}} = \arg\max_{c \in C} P(c_j) \prod_{x \in X} P(x|c)$$

- $P(c_i)$  represents the prior probability of class  $c_i$ .
- $\prod_{x \in X} P(x|c)$  represents the likelihood of the features  $x_1, x_2, \dots, x_n$  given class c.

# Applying Multinomial Naive Bayes Classifiers to Text Classification

 The Multinomial Naive Bayes classifier for text classification can be applied as follows:

$$c_{\mathsf{NB}} = \arg\max_{c_j \in C} P(c_j) \prod_{i \in \mathsf{positions}} P(x_i | c_j)$$

- c<sub>NB</sub> represents the predicted class for the test document.
- C is the set of all possible classes.
- $P(c_i)$  is the prior probability of class  $c_i$ .
- ∏<sub>i∈positions</sub> P(x<sub>i</sub>|c<sub>j</sub>) calculates the likelihood of each feature x<sub>i</sub> at position i given class c<sub>i</sub>.
- The product is taken over all word positions in the test document.

## Problems with Multiplying Lots of Probabilities

- Multiplying lots of probabilities can result in floating-point underflow, especially when dealing with small probabilities.
- Example:  $0.0006 \times 0.0007 \times 0.0009 \times 0.01 \times 0.5 \times 0.000008...$
- Idea: Use logarithms, as log(ab) = log(a) + log(b).
- Instead of multiplying probabilities, we can sum the logarithms of probabilities.
- The Multinomial Naive Bayes classifier can be expressed using logarithms as follows:

$$c_{\mathsf{NB}} = rg \max_{c_j \in C} \left( \log(P(c_j)) + \sum_{i \in \mathsf{position}} \log(P(x_i | c_j)) \right)$$

- By taking logarithms, we avoid the issue of floating-point underflow and perform calculations in the log space.
- The classifier becomes a linear model, where the prediction is the argmax of a sum of weights (log probabilities) and the inputs (log conditional probabilities):
- Thus, Naïve Bayes is a linear classifier, operating in the log space.

## Learning the Multinomial Naive Bayes Model

First attempt: Maximum Likelihood Estimates

- The probabilities are estimated using the observed counts in the training data.
- The prior probability of a class c<sub>i</sub> is estimated as:

$$\hat{P}(c_j) = \frac{N_{c_j}}{N_{\text{total}}}$$

where  $N_{c_j}$  is the number of documents in class  $c_j$  and  $N_{\text{total}}$  is the total number of documents.

The estimate of the probability of word w<sub>i</sub> given class c<sub>i</sub> is calculated as:

$$\hat{P}(w_i|c_j) = \frac{\text{count}(w_i, c_j)}{\sum_{w \in V} \text{count}(w, c_j)}$$

where  $w \in V$  represents a word in the vocabulary V.

• The denominator is the sum of counts of all words in the vocabulary within class  $c_j$ .

#### Parameter Estimation

To estimate the parameters of the Multinomial Naive Bayes model, we follow these steps:

- Create a mega-document for each topic  $c_i$  by concatenating all the documents in that topic.
- We calculate the frequency of word w<sub>i</sub> in the mega-document, which represents the fraction of times word w<sub>i</sub> appears among all words in the documents of topic c<sub>i</sub>.
- The estimated probability  $\hat{P}(w_i|c_j)$  of word  $w_i$  given class  $c_j$  is obtained by dividing the count of occurrences of  $w_i$  in the mega-document of topic  $c_j$  by the total count of words in the mega-document:

$$\hat{P}(w_i|c_j) = \frac{\text{count}(w_i, c_j)}{\sum_{w \in V} \text{count}(w, c_j)}$$

Here,  $\operatorname{count}(w_i, c_j)$  represents the number of times word  $w_i$  appears in the mega-document of topic  $c_j$ , and  $\operatorname{count}(w, c_j)$  is the total count of words in the mega-document.

#### Problem with Maximum Likelihood

Zero probabilities and the issue of unseen words

- Consider the scenario where we have not encountered the word "fantastic" in any training documents classified as positive (thumbs-up).
- Using maximum likelihood estimation, the probability P("fantastic" | positive) would be calculated as:

$$\hat{P}(\text{"fantastic"} \mid \text{positive}) = \frac{\text{count}(\text{"fantastic"}, \text{positive})}{\sum_{w \in V} \text{count}(w, \text{positive})}$$

 In this case, the count of the word "fantastic" in positive documents is zero, leading to a zero probability:

$$\hat{P}(\text{"fantastic"} \mid \text{positive}) = \frac{0}{\sum_{w \in V} \text{count}(w, \text{positive})} = 0$$

- However, zero probabilities cannot be conditioned away, regardless of the other evidence present.
- This poses a problem when calculating the maximum a posteriori (MAP) estimate, which is used for classification:

$$c_{\mathsf{MAP}} = \arg\max_{c} \hat{P}(c) \prod_{i} \hat{P}(x_i \mid c)$$

 With a zero probability for a word, the entire expression becomes zero, regardless of other evidence.

## Laplace (Add-1) Smoothing for Naïve Bayes

Handling zero probabilities with Laplace (Add-1) smoothing

- To address the problem of zero probabilities, we can employ Laplace (Add-1) smoothing technique.
- The smoothed estimate  $\hat{P}(w_i \mid c)$  is calculated as:

$$\hat{P}(w_i \mid c) = \frac{\text{count}(w_i, c) + 1}{\sum_{w \in V}(\text{count}(w, c) + 1)}$$

- Here, an additional count of 1 is added to both the numerator and the denominator.
- The denominator is adjusted by adding the size of the vocabulary V to ensure proper normalization.
- By doing so, we prevent zero probabilities and allow some probability mass to be distributed to unseen words.
- This smoothing technique helps to mitigate the issue of unseen words and avoids the complete elimination of certain classes during classification.

#### Multinomial Naïve Bayes: Learning

Learning the Multinomial Naïve Bayes Model

- In order to learn the parameters of the model, we need to calculate the terms  $P(c_i)$  and  $P(w_k \mid c_i)$ .
- For each class  $c_i$  in the set of classes C, we perform the following steps:
  - Retrieve all the documents *docs*<sub>i</sub> that belong to class *c*<sub>i</sub>.
  - Calculate the term  $P(w_k \mid c_j)$  for each word  $w_k$  in the vocabulary V:

$$P(w_k \mid c_j) = \frac{n_k + \alpha}{n + \alpha \cdot |Vocabulary|}$$

where  $n_k$  represents the number of occurrences of word  $w_k$  in the concatenated document  $Text_i$ .

• Calculate the prior probability  $P(c_i)$ :

$$P(c_j) = \frac{|docs_j|}{|total \ number \ of \ documents|}$$

 To calculate P(w<sub>k</sub> | c<sub>j</sub>), we need to extract the vocabulary V from the training corpus.

#### **Unknown Words**

#### Dealing with unknown words in the test data:

- When we encounter unknown words in the test data that do not appear in the training data or vocabulary, we ignore them.
- We remove these unknown words from the test document as if they were not present at all.
- We do not assign any probability to these unknown words in the classification process.

#### Why don't we build an unknown word model?

- Building a separate model for unknown words is not generally helpful.
- Knowing which class has more unknown words does not provide useful information for classification.

## Stop Words

Stop words are frequently used words like "the" and "a" that are often considered to have little or no significance in text classification. Some systems choose to ignore stop words in the classification process. Here is how it is typically done:

- Sort the vocabulary by word frequency in the training set.
- Create a stopword list by selecting the top 10 or 50 most frequent words.
- Remove all stop words from both the training and test sets, treating them as if they were never there.

However, removing stop words doesn't usually improve the performance of Naive Bayes classifiers. Therefore, in practice, most Naive Bayes algorithms use all words and do not utilize stopword lists.

# Worked Sentiment Example

#### **Training data:**

Category	Text		
Negative	Just plain boring, entirely predictable and		
	lacks energy.		
Negative	No surprises and very few laughs.		
Positive	Very powerful.		
Positive	The most fun film of the summer.		

#### Test:

Category	Text	
?	Predictable with no fun.	

## Worked Sentiment Example

	Cat	Documents
Training	-	just plain boring
	-	entirely predictable and lacks energy
	-	no surprises and very few laughs
	+	very powerful
	+	the most fun film of the summer
Test	?	predictable with no fun

#### 3. Likelihoods from training:

$$p(w_i|c) = \frac{count(w_i, c) + 1}{(\sum_{w \in V} count(w, c)) + |V|}$$

$$P(\text{``predictable''}|-) = \frac{1+1}{14+20} \quad P(\text{``predictable''}|+) = \frac{0+1}{9+20}$$

$$P(\text{``no''}|-) = \frac{1+1}{14+20} \quad P(\text{``no''}|+) = \frac{0+1}{9+20}$$

$$P(\text{``fun''}|-) = \frac{0+1}{14+20} \quad P(\text{``fun''}|+) = \frac{1+1}{0+20}$$

#### 1. Prior from training:

#### 2. Drop "with"

#### 4. Scoring the test set:

$$P(-)P(S|-) = \frac{3}{5} \times \frac{2 \times 2 \times 1}{34^3} = 6.1 \times 10^{-5}$$

$$P(+)P(S|+) = \frac{2}{5} \times \frac{1 \times 1 \times 2}{29^3} = 3.2 \times 10^{-5}$$

Questions?

Thanks for your Attention!

## References I