

Assignment 3

Problem 1

New Binary Search (int[] A, int key, int low, int high)

A = array

key = target value

$\frac{low+high}{2}$ used to split array

low = start index

in half

high = end index

$\frac{high-low}{3}$ divides array into

Need to split array

thirds

Use two more indexes

int x = low + $\left(\frac{high-low}{3}\right)$ // top of lower array

int y = high - $\left(\frac{high-low}{3}\right)$ // bottom of higher array

low can't be larger than high

If low is greater than high

return -1, so program gives null

compare key to values in A[x] and A[y]

If key is equal to value in A[x]

return x

If key is equal to value in A[y]

return y

If key is less than value in A[x]

return NewBinarySearch(A, key, low, x-1)

// search lower array

If key is greater than value in A[y]

return NewBinarySearch(A, key, y+1, high)

// search higher array

Else key is none of the above

return NewBinarySearch(A, key, x+1, y-1)

// search middle array

Binary Search Tree has time complexity of $O(\log_2 n)$, because it searches two halves of an array. Searching a third array would make the time complexity $O(\log_3 n)$.

Problem 2

FindLargest(int[] A, int low, int high)

A = array

low = start index

high = end index

Array needs to be split using $\frac{low+high}{2}$

Need two indexes to hold largest integers

int x = left side int z = low+high

int y = right side $\frac{z}{2}$

Case where start index and end index are the same

If low is equal to high

return A[low]

// This value would already be the largest
Use recursion to check both sides of array

X = FindLargest(A, low, z) // search left side

y = FindLargest(A, z+1, high) // search right side

// z+1 so z is not checked again

Compare values of x and y // return the largest

If x is greater than y of the two.

return X

If y is greater than x

return y

Similar to a Binary Search Tree, which searches two subtrees, with a time complexity of O(n).

FindLargest searches two sides of an array, which should make its time complexity O(n) as well.

Problem 31

Find Majority (int[] A, int low, int high)

A = array

low = start index

high = end index

Need to split array using $(\text{low} + \text{high})/2$

Need two indexes

X = left side let $Z = (\text{low} + \text{high})/2$

y = right side

Need case if start index and end index are the same

If low is equal to high

return $A[\text{low}]$

//array length is size of 1

Set X and Y indexes and search using recursion

X = Find Majority (A, low, Z)

Y = Find Majority (A, Z+1, high)

Case if X and Y are the same

If X is equal to Y

return X // Majority is already X and Y

Need to count values to find majority

int leftCount = 0;

int rightCount = 0

Case if leftCount and rightCount are the same

If leftCount is equal to rightCount

return leftCount // both would be majority

For loop // for counting values "while loop" could also work

int i = 0; i <= Z; i++

If A[i] is equal to X

leftCount = leftCount + 1

Majority needs to be

greater than $\frac{\text{array size}}{2} = W$

For loop

int i = 0; i < Z+1; i++

If A[i] is equal to Y

rightCount = rightCount + 1

Compare left side and right side

If X is greater than W

return X

If Y is greater than W

return Y

Problem 3] cont'

Search both sides of the array, similar to Binary Search, makes time complexity $O(n)$. Comparing values and merging them is similar to a Merge Sort, which has a time complexity of $O(\log n)$. Since the algorithm Find Majority searches both sides of the array and compares and counts, or merges, then the time complexity would be $O(n \log n)$.