

# Signals and Systems: PS 06

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- ① The shooting range acts as the impulse response, meaning that if we input some signal  $x(t)$ , in this case, the output from the shooting range is some signal  $y(t)$ . Because the impulse (violin sound) must be modified by the impulse response  $h(t)$  in the frequency domain, we know that in the time domain that is equivalent to convolution, i.e.  $y(t) = x(t) * h(t)$
- $\begin{matrix} & \uparrow & \uparrow & \uparrow \\ & \text{output} & \text{impulse} & \text{impulse response} \end{matrix}$

- ② We know that  $y(t) = x(t) * h(t)$  so,

$$\begin{aligned}
 y(t) &= \frac{1}{2} x(t-1) + \frac{1}{4} x(t-10) \\
 &= \frac{1}{2} (\text{impulse at } t=1) + \frac{1}{4} (\text{impulse at } t=10) \\
 &= \frac{1}{2} \delta(t-1) + \frac{1}{4} \delta(t-10)
 \end{aligned}$$

This model can reasonably be called an echo channel since it returns a response 1 second later at half the amplitude and the 9 seconds after that it responds at a quarter of the amplitude. Such it would sound like an echo:

