$\operatorname{Re}\Sigma^{(2)}[G_H,U](\mathbf{k},i\omega_n)$

