

IIB_action

Type IIB supergravity action

These are given in ¹

String frame (split into NS/R/CS)

$$S_{\text{IIB}} = S_{\text{NS}} + S_{\text{R}} + S_{\text{CS}}.$$

$$S_{\text{NS}} = \frac{1}{2\kappa_{10}^2} \int d^{10}x (-G)^{1/2} e^{-2\Phi} \left(R + 4\partial_\mu\Phi\partial^\mu\Phi - \frac{1}{2}|H_3|^2 \right). \quad (1)$$

$$S_{\text{R}} = -\frac{1}{4\kappa_{10}^2} \int d^{10}x (-G)^{1/2} \left(|F_1|^2 + |\tilde{F}_3|^2 + \frac{1}{2}|\tilde{F}_5|^2 \right). \quad (2)$$

$$S_{\text{CS}} = -\frac{1}{4\kappa_{10}^2} \int C_4 \wedge H_3 \wedge F_3. \quad (3)$$

Einstein frame (directly from string frame)

We define the Einstein-frame metric by the Weyl rescaling

$$G_{\mu\nu}^{(E)} = e^{-\Phi/2} G_{\mu\nu}.$$

In terms of G_E the action becomes

$$S_{\text{IIB}} = S_{\text{NS}}^{(E)} + S_{\text{R}}^{(E)} + S_{\text{CS}},$$

$$S_{\text{NS}}^{(E)} = \frac{1}{2\kappa_{10}^2} \int d^{10}x (-G_E)^{1/2} \left(R_E - \frac{1}{2}(\partial\Phi)^2 - \frac{1}{2}e^{-\Phi}|H_3|^2 \right), \quad (4)$$

$$S_{\text{R}}^{(E)} = -\frac{1}{4\kappa_{10}^2} \int d^{10}x (-G_E)^{1/2} \left(e^{2\Phi}|F_1|^2 + e^\Phi|\tilde{F}_3|^2 + \frac{1}{2}|\tilde{F}_5|^2 \right). \quad (5)$$

Equivalently, combining the NSNS and RR sectors into a single Einstein-frame integral and keeping the Chern-Simons term separate,

$$\begin{aligned} S_{\text{IIB}} = & \frac{1}{2\kappa_{10}^2} \int d^{10}x (-G_E)^{1/2} \left(\left(R_E - \frac{\partial_\mu\bar{\tau}\partial^\mu\tau}{2\tau_2^2} \right) - \frac{1}{2} \left(e^{-\Phi}|H_3|^2 + e^\Phi|\tilde{F}_3|^2 \right) - \frac{1}{4}|\tilde{F}_5|^2 \right) \\ & - \frac{1}{4\kappa_{10}^2} \int C_4 \wedge H_3 \wedge F_3. \end{aligned} \quad (6)$$

Einstein frame (**SL(2)**-covariant form)

$$S_{\text{IIB}} = \frac{1}{2\kappa_{10}^2} \int d^{10}x (-G_E)^{1/2} \left(R_E - \frac{\partial_\mu \bar{\tau} \partial^\mu \tau}{2(\text{Im}\tau)^2} - \frac{\mathcal{M}_{ij}}{2} \tilde{F}_3^i \cdot \tilde{F}_3^j - \frac{1}{4} |\tilde{F}_3|^2 \right) - \frac{\epsilon_{ij}}{8\kappa_{10}^2} \int C_4 /$$

References

1. J. Polchinski, *String Theory, Volume 2: Superstring Theory and Beyond*, Cambridge University Press (1998).[←](#)