Phy 321 Spring 2017 HW 13.1 $I_{\bullet}(a) \qquad \qquad \int dr' F(r')$ $=\int dr' \frac{A}{r'^3} = \left(\frac{Ar}{-2}\right)^{r}$ $= \frac{-A}{2r^2} + \sqrt{x^2}$ chech this: $F = -\frac{dU}{dr} = (-1)\frac{A}{2}\frac{-2}{r^3}$ (b) use polar cords $T = \frac{1}{2}M(\dot{r} + r\dot{\rho})$ $V = \frac{-A}{2r^2}$ L = T-V $\mathcal{F}_{\beta} = \frac{\partial \mathcal{J}}{\partial \dot{\beta}} = M \dot{\gamma} \dot{\beta}$ $\frac{F}{p} = \frac{2k}{2q} = 0$ $\frac{F}{p} = F \Rightarrow P = const = argula Mon$

$$E = T + V$$

$$= \frac{1}{2} M \left(r + r \right) - \frac{P}{2r^2}$$

$$=\frac{1}{2}m\dot{r}^2+\frac{1}{2}n\frac{1}{r^2}\left(\frac{p_0^2}{m}\right)^2-\frac{A}{2r^2}$$

$$E = \frac{1}{2} \text{min}^2 + \text{Voff}(r)$$
where $\text{Voff}(r) = \frac{p}{2mr^2} - \frac{A}{2r^2}$

1. (c) let
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$$V_{eff} = 1$$
 $\left(\frac{l^2}{M} - A\right) \frac{1}{V^2}$

 $\left(\frac{1}{M} - A\right) < 0$ Can have boursel orbit (will be bonded wherever 12-A < 0 and E < 0 / | 2 | < AM | (. (d) l = Pp = Mvoro $V_{eff} = \frac{\left(Mv_{o}r_{o}\right)^{2}}{2Nr^{2}} - \frac{A}{2r^{2}}$ $= (M v_0^2 + \frac{2}{0} - A) \frac{1}{2 r^2}$ $E = V_{\phi}(r_0) = \frac{1}{2} \left(M V_0^2 - \frac{A}{r_0^2} \right)$ because r=0 at r=ro from t=0

$$E = \frac{1}{2} \mu r^{2} + 166$$

$$\frac{1}{2} \left(\frac{M v_{0}^{2} - \frac{A}{r_{0}^{2}}}{2r^{2}} \right) = \frac{1}{2} \mu r^{2} + \left(\frac{\mu v_{0}^{2} r_{0}^{2} - A}{r_{0}^{2} - A} \right)$$

$$\frac{1}{2} \left(\frac{M v_{0}^{2} - \frac{A}{r_{0}^{2}}}{r_{0}^{2}} \right) - \left(\frac{v_{0}^{2} r_{0}^{2} - \frac{A}{m}}{r_{0}^{2}} \right) = \frac{r^{2}}{r^{2}}$$

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$$\frac{1}{2} \left($$

HW 13.5

let
$$\sqrt{r_0^2 - r_0^2} = u^2$$

$$\int_{r_0-r_0}^{r_0-r_0} = \pm b(x-x_0)$$

$$\Gamma = \sqrt{r_0 - b^2 (t - t_0)^2}$$

$$r = 0$$
 at $A = 0$ \Rightarrow A

$$r = \int_0^2 -6^2 t^2 \text{ where } b = \int_M r_0^2 -v_0^2$$

$$1(e) \quad l = P_f = M \sigma_0 r_0 = M r^2 \phi$$

$$\frac{db}{dx} = \frac{v_0 r_0}{r^2} = \frac{v_0 r_0}{r^2 - b^2 t^2}$$

MW13.6 $\phi = \frac{\sigma}{b} \operatorname{arctanh}(\frac{bt}{r_0}) + const$ initial condition \$ =0 at \$=0 => cont=0 $\phi = \frac{\sqrt{5}}{5} \operatorname{arctanh}\left(\frac{bt}{r_0}\right)$ romanh (not required) motion Ends when I hits O, at I time $t = t_0$ I the velocity in radial direction is goes to in finity in that limit. 2. (a) T = 1 m (r + r p) $V = -\frac{M_m M}{r^2}$ L=T-V $P_{\phi} = \frac{\partial k}{\partial \dot{p}} = mr\dot{\phi}$ $F_{\phi} = \frac{\partial k}{\partial \dot{p}} = 0 \Rightarrow P_{\phi} = const$

HW13.7 $E = \frac{1}{2}m(r^2) + \frac{p^2}{2mr^2} + \frac{2mm}{r}$ In the circular orbit, $p = mr^2 \dot{p} = m R(R\dot{p}) = m v R$ $\frac{d \text{ Volt}}{d \text{ Volt}} = 0 \Rightarrow \frac{f_0}{2m} - \frac{2}{r^3} + \frac{M_m M}{r^2} = 0$ $\frac{P}{mR^3} = \frac{MmM}{R^2}$ $P_{\beta} = (m \sigma R)^2 = m R^3 \frac{\mathcal{B}_m M}{p^2}$ VF = RDM V = MD R another way to get it: mv = F = DmM

HW13.8 2. (b) After the burn (ie elliptical orbit) E = 1 2 m r + 10 - 2 m M turning points, uhere i =0, are at r=Rand r=3R $\int E = \frac{p_0^2}{2mR^2} - \frac{kmM}{R}$ $\left(E = \frac{f \rho^2}{2m(3k)^2} - \frac{ZmM}{(3k)}\right)$ Subtract these to cancel E $O = \frac{Pp}{2m} \left(\frac{1}{R^2} - \frac{1}{9R^2} \right) - 2mm \left(\frac{1}{R} - \frac{1}{3R} \right)$ $\frac{9}{2mR^{2}}\left(\frac{8}{9}\right) = \frac{ymM}{R}\left(\frac{2}{3}\right)$ also g = m v R where ~ = velving
just afterborn

HW 13.9 $\left(mV_{b}^{2}\right)^{2}=\frac{3}{2}y_{m}^{2}\mu^{2}$ C) Pf = MV R just afterburn Pf is conserved, so ff = MV (3K)

A when V_A = relocity at

"-mel $m \mathcal{F} \left(3R \right) = m \mathcal{F} R$ $\frac{1}{A} = \frac{1}{3} \text{ is } = \frac{1}{6} \frac{4M}{R}$