Phy 321 Spring 2017
$$HW 12.1$$

$$I. @T = \frac{1}{2} M (r^2 + (ro)^2)$$

$$V = -Mg r \omega o + \frac{1}{2} k (r-B)^2$$

$$L = T - V$$

$$L = \frac{1}{2} M (r^2 + r^2 o^2)$$

$$+ Mg r \omega o - \frac{1}{2} k (r-B)^2$$

$$Fr = \frac{3k}{9r} = Mr$$

$$- k (r-B)$$

$$Pr = Fr$$

$$Mr = Mr o + Mg \omega o - k(r-B)$$

$$Fr = \frac{3k}{90} = -Mr o$$

$$Fo = \frac{3k}{90} = -Mr o$$

$$Fo = \frac{3k}{90} = -Mr o$$

$$Fo = Fo \Rightarrow Mr o + 2Mr o$$

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HW12.2 Pivide $P_r = F_r$ by $M = \frac{1}{r} - r \theta - g \cos \theta + k (r - B) = 0$ Pivide Pg = Fo by Mr $\begin{bmatrix} r\ddot{o} + 2\dot{r}\ddot{\delta} + g\sin{\delta} = 0 \end{bmatrix}$ 2. (a) $T = \frac{1}{2} (60) \dot{x}^2 + \frac{1}{2} T \omega^2$ where $\omega = v/R = \dot{\gamma}/R$ $\Rightarrow T = \frac{1}{2} \left(60 + \frac{1}{2} \right) \hat{\chi}^2$ $V = -(\sigma x) \frac{x}{2} - (\sigma (b - \pi R - x))(b - \pi x x)$ $= - \frac{\sigma x^2}{2} - \frac{\sigma (b - \pi r - x)^2}{2}$ $= -\sigma \chi^{2} + \sigma \chi \left(b - H R \right) + const$ $= -\sigma \left(\chi - b - H R \right)^{2} + const$

$$2.(c) L = T - V$$

$$= \frac{1}{2} \left(b\sigma + \frac{1}{2} \right) \chi$$

$$+ \sigma \left(\chi - \frac{b - \pi R}{2} \right)^{2}$$

$$+ curst$$

$$\sqrt{ant} care$$

$$P = \frac{1}{2} L - \left(b\sigma + \frac{1}{R^{2}} \right) \chi$$

$$F = \frac{\partial L}{\partial x} = 2\sigma \left(x - \frac{J - \pi R}{2} \right)$$

$$F = P \Rightarrow$$

$$\left(b\sigma + \frac{1}{R^2}\right)\pi = 2\sigma\left(x - \frac{b - rR}{2}\right)$$

2. (d)
$$E = T + V = \frac{1}{2} (bo + \frac{\pi}{2}) \chi$$

$$-\sigma\left(x-\frac{5-1/2}{2}\right)^2$$

$$0 = \lambda E = (30 + \frac{1}{2}) \times \times$$

$$-20 (x - \frac{1772}{2}) \times$$

2. (e)
$$(b + I) \dot{x} - 2\sigma(x - b - i\tau R)$$

Let $x - b - i\tau R = y$

$$J = C_{j} \sinh \left(\left(\frac{2\sigma}{b\sigma + \frac{T}{R^{2}}} \right) \right)$$

$$+ C_2 \cosh \left(\frac{2\sigma}{5\sigma + \frac{\pm}{R^2}} \right)$$

$$\chi = \frac{b - HL}{2} + C_1 salpha \frac{50}{50 + \frac{7}{2}} \uparrow$$

$$\dot{\chi} = 0$$
 at $\dot{\chi} = 0 \Rightarrow C_1 = 0$

$$\chi = \chi_0 \text{ wt } \chi = 0 \Rightarrow$$

HW 12.5

$$x = b - 17R + \left(x_0 - \frac{b - 17R}{2}\right) \cosh\left(\frac{2\sigma}{b\sigma + L}\right)$$

 $= \frac{1}{2} M \left(\frac{1}{2} \cos \phi \right)^{2}$ $+ \left(w R \cos \omega t - \frac{1}{2} \sin \phi \right)^{2}$ + 1 mp2 12

= IM [l² j² + (w R wswt)² - w R l cws a t Fin p p + 12 b

HW12.6 T= IM[l2 p2 - wRlcoswt snfp + (wR wwwt)2) V = Mg y = Mg [Rsinwt + 2 worl] - mg [Rsmwt + 2 w f] 3. (b) $p = \frac{\partial \mathcal{L}}{\partial \hat{p}} + \frac{\partial \mathcal{L}}{\partial \hat$ $F = \partial L = -M \text{ well as we to as } \phi$ $+ M J L \text{ sin } \phi$

HW12.7

Me f + MwRl sinf - MWRl Cus(wt) Cosp & = -M w R l cos(ut) cosp p+ Mgl sind Ml f + Mwrl sn(wt) sint/ -Mgl sind =0 multiply by 3 to get $\frac{1}{2} + \frac{3}{2} \frac{\omega^2 R}{2} \operatorname{sin}(\omega t) \operatorname{sind} - \frac{3}{2} \operatorname{sind}$

3. (c) with
$$q=1$$
, $l=1$, $k=0.05$ this because $\frac{3}{2} - \frac{3}{2} \operatorname{Sm}(\phi) + 0.075 \omega^2 \operatorname{Sm}(\omega +) \operatorname{Sm}(\phi) = 0$

In Marlamatica, let

 $zero = phi''(t) - \frac{3}{2} sin(phi(t))$

+ 0.075 omega12 sin [omega*t] 1

Sin [Phicks)

sol = NDSolve [{Zero 1. omega > 40} == 0,

phico] == 0.4, phi [0] ==0}

phi[t], {t, 0, 20}]

Plot [Phi[t] 1. sol[[1]], {t,0,20}]

Find Stable motion (with -1.265 (\$<1.265)

UNSTABLE Y W < 38,2360

HW 12,9

If change initial phi [0] from 0.4 70 0,3, then Stable for with -1.07
with -1.07 < p < 1.07

H clienge initial phi(0) 70 0.2) 5 table for ω > 27,68/1 with - 0.846< \$ < 0.846