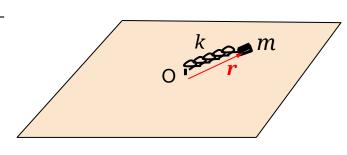
Name \_\_\_\_grading key\_

In the figure, the mass m slides without friction on the horizontal plane, and the spring (Hooke's constant = k, equilibrium length =  $\ell_O$ ) is free to revolve around the point O.

- (A) What is the potential energy U(r)? (Taylor states that the potential energy is not  $\frac{1}{2}$  k  $r^2$ .)
- (B) Now assume the mass moves on a circle of radius R. Calculate the period of revolution.



(A) 
$$U(r) = \frac{1}{2} k (r - l_0)^2$$
;

the force is  $F_r = -k(r - l_0)$ .

(B) For circular motion, 
$$a_r = -v^2/r = -r\omega^2$$
.

Newton's second law,  $a_r = F_r/m = -(k/m) (r - l_0)$ .

So 
$$\omega^2 = (k/m) (r - l_0)/r$$

The period is

$$T = 2\pi / \omega = 2\pi \sqrt{\frac{m}{k}} \sqrt{\frac{r}{r - l_0}}$$

Homework Assignment #8

Name grading

due in class Friday, October 28

Cover sheet: Staple this page in front of your solutions.

Write the *answers* (without calculations) on this page; write the detailed *solutions* on your own paper.

[37] Problem 4.26.\*

*Answer: What is dE/dt?* 

dE/dt = m y dg/dt

1 point

[38] Problem 4.28 and 4.29.\*\*\*[computer]

For #4.29, hand in the computer program and any plots. Check plot.

Answer: What is the period for #4.29 part (d)?

3.708 time units

3 points

[39] Problem 4.33.\*\*[computer]

Hand in the computer program and any plots.

Answer: Did you hand in the computer results?

Check the plots of  $U(\theta)$  for b = 0.9 r and b = 1.1 r.

2 points

[40] Problem 4.34.\*\*

Answer: What is the period if the length is 1 m?

2.007 seconds

2 points

[40x] Problem 4.37.\*\*\*[computer]

Hand in the computer program and any plots.

Answer: Did you hand in the computer results? Check the plots of U vs  $\varphi$ .

Answer: What is the critical ratio m/M? 0.7426

3 points

[40xx] Problem 4.38.\*\*\*[computer]

Hand in the computer program and any plots.

Answer: Did you hand in the computer results? Check the plot of  $\tau$  vs  $\Phi$ .

Answer: <u>Explain</u> what becomes of  $\tau$  as the amplitude of oscillation approaches  $\pi$ . The period approaches infinity because  $\Phi = \pi$  is a point of (unstable) equilibrium.

3 points