Berlin 2010 Cat 5

Problem: No Theme

Proposed by Tom Bach

Let $\{a_n\}_{n\in\mathbb{N}}$ be a sequence of real numbers. Prove or disprove: $\{a_n\}$ is a Cauchy sequence if and only if $\{a_n\}$ is a bounded sequence.