

## FAMA - MACBETH REGRESSION

### INTRODUCTION

- FM REGRESSION IS A PARAMETRIC TECHNIQUE THAT ENABLE US TO EXAMINE THE RELATION BETWEEN PAIRS OF VARIABLES WHILE INCLUDING MANY CONTROLS IN THE ANALYSES
- THE TEST OF THIS APPROACH IS THE ASSUMPTION THAT THE RELATIONSHIP BETWEEN THE VARIABLES OF INTEREST ARE LINEAR

### 6.1. IMPLEMENTATION

- IMPLEMENTED USING TWO-STEP PROCEDURE
- THE FIRST STEP CONSISTS OF RUNNING A PERIODIC CROSS-SECTIONAL REGRESSION ON THE DEPENDENT VARIABLE  $y$  AGAINST ONE OR MANY INDEPENDENT VARIABLES  $x_1, x_2, \dots, x_m$ , USING TIME SERIES DATA
- THIS PROCEDURE RESULTS IN ESTIMATES FOR THE FIXED COEFFICIENT AND SLOPE COEFFICIENTS FOR EACH INDEPENDENT VARIABLE FOR EACH  $t$ .
- THE SECOND STEP CONSISTS OF ANALYZING THE TIME SERIES OF SLOPE COEFFICIENTS TO DETERMINE WHETHER THE AVERAGE COEFFICIENT DIFFERS FROM ZERO

#### 6.1.1. PERIODIC CROSS-SECTIONAL REGRESSIONS

- OUR CROSS-SECTIONAL REGRESSION SPECIFICATION IS:

$$y_{i,t} = \alpha_{i,t} + \beta_{1,t} x_{1,i,t} + \beta_{2,t} x_{2,i,t} + \dots + \epsilon_{i,t}$$

WHERE INDEPENDENT VARIABLES ARE TYPICALLY WINZERIZED, AND WHERE THE DEPENDENT VARIABLE IS NOT EXCESS RETURN ITS ALSO WINZERIZED.

- THE RESULT IS A TIME SERIES OF:
  - (a) PARAMETERS  $\alpha_{i,t}, \beta_{1,t}, \dots$
  - (b) REGRESSION STATISTICS SUCH AS  $R^2, \text{ADJ-}R^2, N$  OF OBS, WHICH WE CAN DENOTE  $R^2_t, \text{ADJ-}R^2_t, N_t$ .
- THIS STEP CAN BE ESTIMATED USING OLS, WOLS, OR EVEN LOGISTIC REG.

#### EXAMPLE

$$\begin{aligned} y_{i,t+1} &= \alpha_{i,t} + \beta_{1,t} p_{i,t} + \beta_{2,t} \text{Size}_{i,t} + \beta_{3,t} BM_{i,t} + \epsilon_{i,t+1} \\ &\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ \text{one-year.} & \text{Market port.} & \log \text{of the} & \text{Book-to-Market} \\ \text{Annual excess} & \text{Riskless} & \text{Market cap.} & \text{Value Ratio} \\ \text{return of stock } i & & & \end{aligned}$$

#### 6.1.2. AVERAGE CROSS-SECTIONAL REGRESSION RESULTS

- THE SECOND STEP OF THE FM REGRESSION CONSISTS IN COMPUTING THE TIME-SERIES AVERAGES OF THE PERIODIC CROSS-SECTIONAL REGRESSION RESULTS AND OTHER STATISTICS ( $R^2, \text{ADJ-}R^2, N$ )
- OUR GOAL IS TO TEST WHETHER THE AVERAGE COEFFICIENT IS STATISTICALLY DIFFERENT THAN ZERO
- THE THEREFORE, WE NEED TO COMPUTE STANDARD ERRORS, T-STATISTICS, AND P-VALUES TO TEST THE NULL HYPOTHESIS THAT THE AVERAGE COEFFICIENT IS  $= 0$

### 6.2 INTERPRETING FM REGRESSIONS

- STATISTICALLY SIGNIFICANT AVERAGE SLOPE COEFFICIENT INDICATES A CS RELATION BETWEEN THE INDEPENDENT VARIABLE  $X$  AND THE INDEPENDENT VARIABLE  $y$  IN THE AVERAGE TIME PERIOD

$p < 0.05 \Rightarrow t\text{-stat} > 2$  (USUALLY THE LOWER BOUND FOR SIGNIFICANCE)

- IN ADDITION, IT'S USEFUL TO INVESTIGATE IF THE STATISTICALLY SIGNIFICANT RELATION IS ECONOMICALLY MEANINGFUL

(1) THERE ARE SITUATIONS WHERE THE CHANGE IN ONE UNIT IN  $X$  CAN BE EASILY INTERPRETED, THEREFORE IT'S EASY TO EVALUATE ITS ECONOMIC IMPORTANCE

(2) ASSESS THE EFFECT OF ONE STD-DEV. CHANGE IN  $X$  ON  $y$ . TO DO THIS, WE MULTIPLY THE AVERAGE SLOPE COEFFICIENT BY THE CROSS-SECTIONAL STD-DEV. OF  $X$  IN THE AVERAGE PERIOD

(3) PERCENTILES COMPARISON

- Pastor, Stambaugh, and Taylor (2010) SHOW THAT:
  - (a) UNIVARIATE REGRESSION SPECIFICATION (ONE INDEPENDENT VARIABLE)
  - (b) BALANCED PANEL DATA (SAME ENTITIES IN EACH CS)
  - (c) CROSS-SECTIONAL VARIANCE OF THE INDEPENDENT VARIABLE IS CONSTANT ACROSS ALL TIME PERIODS

⇒ AVERAGE SLOPE COEFFICIENT OF FM REGRESSION IS IDENTICAL TO THE SLOPE GENERATED BY PANEL REGRESSION WITH TIME FIXED EFFECTS.

#### FROM CHAPTER 1 - SECTION 1.1: SAMPLE

- EACH STATISTICAL METHODOLOGY PRESENTED IN THIS BOOK IS PERFORMED USING PANEL DATA
- EACH ENTRY IN THE PANEL CORRESPONDS TO A PARTICULAR COMBINATION OF ENTITY  $i$ , AND TIME PERIOD  $t$

$i$ : STOCKS, BONDS, OPTIONS, OR FILMS  
 $t$ : MONTHS, WEEKS, QUARTERS, YEARS, AND DAYS

- THE DATA CORRESPONDING TO ANY GIVEN TIME PERIOD ARE REFERRED TO AS A CROSS SECTION
- IN MOST CASES, THE SAMPLE IS NOT A FULL PANEL, WHICH MEANS THAT THE NUMBER OF ENTITIES  $i$  CAN VARY WITH TIME
- FOR EACH PAIR  $(i,t)$ , THE DATA INCLUDE SEVERAL CHARACTERISTICS  $X$ , WHICH WE DENOTE  $X_{it}$
- PART 1 OF THE BOOK ASSUMES THAT EACH ENTITY  $i$  CORRESPONDS TO A STOCK, AND  $t$  CORRESPONDS TO A YEAR
- THE SAMPLE CORRESPONDS TO 25 YEARS (1980-2012), WHERE FOR EACH YEAR THE SAMPLE INCLUDES ALL STOCKS  $i$  IN THE CRSP DATABASE THAT ARE LISTED AS US-BASED COMMON STOCKS ON DECEMBER 31 OF YEAR  $t$
- PART 2 USES THE SAME DATA IN MONTHLY FREQUENCY
- FOR EACH OBSERVATION IN THE SAMPLE WE CALCULATE:
  - (a)  $\beta$  OF STOCK  $i$  IN YEAR  $t$  AS THE SLOPE COEFFICIENT FROM A REGRESSION OF EXCESS RETURN OF STOCK  $i$  ON EXCESS RETURN OF THE MARKET PORTFOLIO USING DAILY DATA DURING ALL YEARS

(b) MARKET CAPITALIZATION ( $Mktcap$ ) FOR STOCK  $i$  IN YEAR  $t$  AS THE NUMBER OF OUTSTANDING SHARES TIMES THE PRICE OF THE STOCK AT THE END OF YEAR  $t$  DIVIDED BY \$MM. WE TAKE THE SIZE =  $\log(Mktcap)$

(c) BOOK-TO-MARKET RATIO ( $BM$ ) IS COMPUTED AS THE BOOK VALUE OF THE FIRM'S EQUITY DIVIDED BY MARKET VALUE OF THE FIRM'S EQUITY ( $Mktcap$ )

- STOCK RETURNS, PRICES, AND OTHERS OUTSTANDING DATA COMES FROM CRSP DATA
- BOOK VALUE OF EQUITY DATA COMES FROM COMPUSTAT
- RISK-FREE SECURITY DATA COMES FROM KENNETH THOMAS LIBRARY