

Learning algorithm:

$$\arg \min_w \left\{ \frac{1}{N} \sum_{i=1}^N (\langle w, x_i \rangle - y_i)^2 + \lambda \|w\|_2^2 \right\}$$
$$x_i, w \in \mathbb{R}^d, \lambda \in \mathbb{R}, y_i \in \{-1, 1\}$$

Analytical solution to the problem:

$$w^* = (X^T X + \lambda I_d)^{-1} X^T Y$$
$$w^* = \frac{\sum_{i=1}^N x_i^T y_i}{\sum_{i=1}^N x_i x_i^T + N\lambda}$$

Generating a prediction in the binary case due to Bayes Decision Rule:

$$\hat{y}_i = \text{sign}(\langle x_i, w^* \rangle)$$

Multi-class: k is the number of classes

For $j \in [1, k]$:

Solve

$$\arg \min_{w_j} \left\{ \frac{1}{N} \sum_{i=1}^N (\langle w_j, x_i \rangle - y_i^k)^2 + \lambda \|w_j\|_2^2 \right\}$$

$$\hat{y}_i = \text{index} \left(\arg \max \{ \langle x_i, w_1^* \rangle, \dots, \langle x_i, w_j^* \rangle, \dots, \langle x_i, w_k^* \rangle \} \right)$$