

11-26

1)

$$\lambda = \frac{2L}{n} = \frac{2 \times 3}{3} = 2\text{m}$$

$$f = \frac{v}{\lambda} = \frac{100}{2} = 50\text{Hz}$$

2)

$$k = \frac{2\pi}{\lambda} = \frac{2\pi}{2} = \pi \text{ rad/m}$$

$$\omega = 2\pi f = 2\pi \times 50 = 100\pi \text{ rad/s}$$

向右传播的波: $y_1(x,t) = 0.01 \sin(\pi x - 100\pi t)$

向左传播的波: $y_2(x,t) = 0.01 \sin(\pi x + 100\pi t)$

11-27

1)

$$\cos(5\pi x) = 0$$

$$5\pi x = (n + \frac{1}{2})\pi$$

$$x = \frac{2n+1}{10} \quad (n = 0, 1, 2, \dots)$$

$n=0$ 时, 有 $x=0.1\text{m}$, $n=1$ 时, 有 $x=0.3\text{m}$

则波节的位置为 $x=0.1\text{m}$ 和 $x=0.3\text{m}$ 。

2)

$$\omega = 40\text{rad/s}, \quad T = \frac{2\pi}{\omega} = \frac{1}{20} = 0.05\text{s}$$

3)

$$k = 5\pi \text{ rad/m}, \quad \lambda = \frac{2\pi}{k} = \frac{2}{5} = 0.4\text{m}$$

$$f = \frac{1}{T} = 20\text{Hz}$$



$$v = \lambda f = 20 \times 0.4 = 8 \text{ m/s}$$

$$\text{由 } y(x, t) = 0.045 \cos 5\pi x \cos 40\pi t$$

$$\text{则 } A = 0.045$$

4)

$$v(x, t) = \frac{0.045}{0.05} \cos 5\pi x \times (-40\pi) \sin(40\pi t)$$

$$v(x, t) = -0.045 \times 40\pi \cos(5\pi x) \sin(40\pi t)$$

$$\text{要使 } v(x, t) = 0, \text{ 有 } \sin(40\pi t) = 0$$

$$\text{则有 } 40\pi t = n\pi, t = \frac{n}{40} (n = 0, 1, 2, \dots)$$

即 $t = 0, t = 0.025, t = 0.05$ 时, 弦上所有点速度为 0.

11-28

1)

$$f' = f_s \frac{v}{v - v_s} = 500 \times \frac{340}{340 - 25} \approx 539.7 \text{ Hz}$$

$$f_s = f_s \frac{v}{v + v_s} = 500 \times \frac{340}{340 + 25} \approx 465.7 \text{ Hz}$$

$$\text{则 } \Delta f = 539.7 - 465.7 = 74 \text{ Hz}$$

2)

$$f' = f_s \frac{v + v_L}{v - v_s} = 500 \times \frac{340 + 15}{340 - 25} \approx 563.5 \text{ Hz}$$

11-30

$$f' = 400 \times \frac{330 + 22.22}{330 - 33.33} \approx 474.8 \text{ Hz}$$

11-32



1)

$$\lambda = \frac{v - v_s}{f_s} = \frac{331 - 30}{1080} = \frac{301}{1080} \approx 0.2787 \text{ m}$$

2)

$$f' = f_s \frac{v + v_m}{v - v_s} = 1080 \times \frac{331 + 65}{331 - 30} = 1080 \times \frac{396}{301} \approx 1421 \text{ Hz}$$

3)

$$v = 331 - 65 = 266 \text{ m/s}$$

4)

$$\lambda' = \frac{v'}{f'} = \frac{266}{1421} \approx 0.187 \text{ m}$$

1)

$$f = \frac{331 + 65}{331 - 30} \times 1080$$

$$f = 1080 \times \frac{396}{301} \approx 1421 \text{ Hz}$$

$$\lambda = \frac{331 - 30}{1080} = \frac{301}{1080} \approx 0.28 \text{ m}$$

$$f' = \frac{331}{331 + 65} \times 1080 = 990 \text{ Hz}$$

$$\lambda' = \frac{331 + 65}{1080} = 0.33 \text{ m}$$

2)

$$f_R = \frac{331 + 65}{331 - 30} \times 1080 = 1421 \text{ Hz}$$

3)

反射波的波速为反射波在空气中的速度，即 331 m/s



4)

$$\lambda_p = \frac{331-65}{1421} = 0.187 \text{ m}$$

11-34

对于发射器探测器的波, 潜艇先以速度 v 接收, 则有

$$f' = f \left(1 + \frac{v}{v_s} \right) \text{ 波}$$

潜艇视作一个移动源, 将超声波以 f' 发射回探测器则有

$$f'' = f' \left(1 + \frac{v}{v_s} \right)$$

则拍为 f'

$$f_{\text{拍}} = |f'' - f| = 241 \text{ Hz}$$

$$\text{即} \left(1 + \frac{v}{v_s} \right)^2 - 1 = \frac{241}{30000}$$

$$\left(1 + 2 \frac{v}{v_s} + \left(\frac{v}{v_s} \right)^2 \right) - 1 = \frac{241}{30000}$$

$$2 \frac{v}{v_s} + \left(\frac{v}{v_s} \right)^2 = \frac{241}{30000}$$

~~解~~ ~~$v = 1500 \times \frac{241}{30000}$~~
 $v \approx 6.025 \text{ m/s}$

