## **CHM 101 LECTURE NOTE**

**COURSE TITLE: INTRODUCTORY PHYSICAL CHEMISTRY** 

CREDIT UNIT: 03

PART TITLE: CHEMICAL EQUILIBRIUM

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## **COURSE SYNOPSIS**

- The concept of equilibrium
- Equilibrium Law (Law of Mass action)
- Relationship between K<sub>p</sub> and K<sub>c</sub>
- Relationship between △G and K
- Effect of temperature on the equilibrium constant.
- Homogenous chemical equilibria
- Heterogeneous equilibria system
- Factors affecting equilibrium constants
- Chemical equilibrium in solution
  - water dissociation constant
  - hydrolysis and hydrolysis constant
- Solubility equilibria
- Common-ion effects

# RECOMMENDED TEXTBOOKS/ REFERENCES

- 1. Principle of physical chemistry by J.M. Gross
- 2. Physical chemistry by Atkins
- 3. Essentials of physical chemistry by Bahl and Bahl
- 4. Chemistry: The central science by Brown, Lemay, Bursten and Murphy.
- 5. Physical chemistry by K.K. Sharma and L.K. Sharma

# **Concept of Equilibrium**

Consider this direct reaction,

$$aA + bB \rightarrow cC + dD$$

The reaction stops when the reactants are used up.

However, for a reversible reaction like this

$$aA + bB \implies cC + dD$$

the equilibrium is attained when the rate of forward reaction is equal to the rate of backward reaction.

Chemical equilibrium is the state of a reversible reaction when the two opposing reactions occur simultaneously.

At equilibrium, the concentrations of reactants and products do not change with time.

# The Equilibrium Law (Law of Mass action)

The law states that "at constant temperature, the rate at which a substance reacts is directly proportional to the active masses of the reactant"

Active mass is a thermodynamic quantity and it is expressed *a*=*fc*, where a -active mass, f- activity coefficient (fugacity), c- molar concentration.

For ideal gaseous and solution reaction, f = 1.

Therefore, the active mass is equal to molar concentration.

According to the law,  $R_f \alpha [A]^a [B]^b$ 

$$\implies R_f = K_f \quad [A]^a [B]^b$$

**Also,**  $R_b \alpha [C]^c [D]^d$ 

$$\implies R_b = K_b [C]^c [D]^d$$

At equilibrium,  $K_f [A]^a [B]^b = K_b [C]^c [D]^d$ 

$$\frac{K_f}{K_b} = \frac{[C]^c [D]^d}{[A]^a [B]^b} = K_c$$

 $K_c$  is the equilibrium constant in term of concentration,

In term of activities,

$$K_A = \left\{ \frac{\left(a_C\right)^c \left(a_D\right)^d}{\left(a_A\right)^a \left(a_B\right)^b} \right\},\,$$

The concept of activity addresses the deviation from ideal behaviour. Therefore, it can be defined as an idealized concentration.  $K_A$  is exact and does not depend on pressure.

In term of pressure,

$$K_{p} = \frac{P_{C}^{c} P_{D}^{d}}{P_{A}^{a} P_{B}^{b}}$$
 where  $P_{A}^{a}$ ,  $P_{B}^{b}$ ,  $P_{C}^{c}$  and  $P_{D}^{d}$  are

the partial pressure of various gaseous species at equilibrium.

# Relationship between K p and K c

In a gaseous reaction, the concentration of the gases at any given temp is expressed in term of their partial pressures.

Consider this gaseous reaction

$$aA_{(g)} + bB_{(g)} \iff cC_{(g)} + dD_{(g)},$$

the equilibrium constant in term of pressure is expressed as

$$K_p = \frac{P_C^c P_D^d}{P_A^a P_B^b}$$
 where  $P_A^a, P_B^b, P_C^c$  and  $P_D^d$  are

the partial pressure of various gaseous species at equilibrium.

# However, $K_p$ and $K_c$ are not numerically equal, the relationship can be derived as follow

## For an ideal gases,

$$PV = nRT$$

$$\Rightarrow P = \frac{n}{V}RT$$

But 
$$\frac{n}{V} = C$$

$$P = CRT$$

$$K_{p} = \frac{C_{C}^{c}(RT)^{c} C_{D}^{d}(RT)^{d}}{C_{A}^{a}(RT)^{a} C_{B}^{b}(RT)^{b}}$$

$$=\frac{C_C^c C_D^d (RT)^{(c+d)}}{C_A^a C_B^b (RT)^{(a+b)}}$$

#### **Recall that**

$$K_c = \frac{C_C^{\phantom{c}c} D_D^{\phantom{c}d}}{A_A^{\phantom{c}a} B_B^{\phantom{c}b}}$$

$$K_p = K_c (RT)^{\Delta n}$$

Where  $\Delta n = (c+d) - (a+b)$  i.e change in the amount of gaseous reagents

When  $\Delta n$  is positive,  $\Rightarrow$  the number of molecules of products are larger than those of the reactants i.e  $K_p \succ K_c$ 

When  $\Delta n$  is zero,  $\Rightarrow$  the number of molecules of products = the number of molecules of the reactants i.e  $K_p = K_c$ 

When  $\Delta n$  is negative,  $\Rightarrow$  the number of molecules of products are smaller than those of the reactants i.e  $K_p \prec K_c$ 

If the equilibrium constant is expressed in term of mole fractions, X it is related to  $K_p$  by

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$$K_{p} = \frac{(X_{C}P)^{c}(X_{C}P)^{d}}{(X_{A}P)^{a}(X_{B}P)^{b}}$$

$$K_{p} = \left(\frac{(X_{C})(X_{D})}{(X_{A})(X_{B})}\right) \times P^{(c+d)-(a+b)}$$

$$K_p = K_x P^{\Delta n}$$

where 
$$\Delta n = (c+d) - (a+b)$$

# Relationship between $\Delta G$ and the equilibrium constant

The change in free energy of a reaction and the equilibrium constant K are related to each other by the expressions

$$\Delta G^{o} = -RT \ln K$$

Temperature dependence on the equilibrium constant

The value of equilibrium constant varies with temperature change. The relationship between the equilibrium constants at two different temperatures and the enthalpy change is given by

$$\log \frac{K_{p_2}}{K_{p_1}} = \frac{\Delta H^o}{2.303R} \left[ \frac{T_2 - T_1}{T \times_1 T_2} \right]$$

Where  $K_{p_2}$  and  $K_{p_1}$  are the equilibrium constants at temperature  $T_2$  and  $T_1$  respectively.

In terms of change in internal energy ( $\Delta E^{o}$ ), the equation becomes

$$\log \frac{K_{p_2}}{K_{p_1}} = \frac{\Delta E^o}{2.303R} \left[ \frac{T_2 - T_1}{T \times_1 T_2} \right]$$

# **HOMOGENOUS CHEMICAL EQUILIBRUM**

Homogenous equilibrium is an equilibrium in which the reactants and the products are in the same phase.

-Homogenous gaseous equilibria

**Case I:** The Hydrogen-lodide system

Consider a reaction

e.g 
$$H_{2(g)} + I_{2(g)} \longrightarrow 2HI_{(g)}$$
 t=0 a b t=t a-x b-x 2x

if V (in dm<sup>3</sup>) is the total volume of the reaction mixture

then, 
$$\frac{a-x}{V} \qquad \frac{b-x}{V} \qquad \frac{2x}{V}$$
 Hence, 
$$K_c = \frac{\begin{bmatrix} HI \end{bmatrix}^2}{\begin{bmatrix} H_2 \end{bmatrix} \begin{bmatrix} I_2 \end{bmatrix}} = \frac{\begin{pmatrix} 2x/V \end{pmatrix}^2}{\begin{pmatrix} \frac{a-x}{V} \end{pmatrix} \begin{pmatrix} \frac{b-x}{V} \end{pmatrix}}$$

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$$K_c = \frac{4x^2}{(a-x)(a-b)}$$
 $K_c$  is independent of the

volume

In term of partial pressure,

$$K_p = \frac{P_C^2}{P_A \times P_B}$$

But 
$$P_A = \frac{n_A}{N} \times P$$
,  $P_B = \frac{n_B}{N} \times P$  and  $P_C = \frac{n_C}{N} \times P$ 

Where  $N = n_A + n_B + n_C = \text{total number of moles,}$ 

 $P = \text{total (external) pressures } P_A, P_B \& P_C \text{ are partial}$ pressures of A, B and C respectively.

$$K_p = \frac{\left(\frac{n_C}{N} \times P\right)^2}{\left(\frac{n_A}{N} \times P\right) \times \left(\frac{n_B}{N} \times P\right)} = \frac{n_C^2}{n_A + n_B}$$

## **Examples:**

1. A mixture of 1 mole of H<sub>2</sub> and 1 mole of I<sub>2</sub> in a flask was heated until the equilibrium is reached. On analysis, the equilibrium mixture is found to contain 0.7mole of HI. Calculate the  $K_{\rm c}$ 

2. Consider this reaction  $H_{2(g)} + I_{2(g)}$ 

Given that the partial pressures of the following substances at 45°C are  $P_{H_2} = 0.065$ atm,  $P_{I_2} = 0.45$  atm. and  $P_{HI} = 0.245$  atm. Calculate (a) the equilibrium constant  $K_p$  for the reaction at 45°C (b) the equilibrium constant  $K_p$  for the backward reaction

3.  $K_c$  for this reaction  $SO_{2(g)} + \frac{1}{2}O_{2(g)}$   $SO_{3(g)}$ 

at 727°C is16.7, calculate  $K_p$  for this reaction at 727°C.

N.B-Solutions to these examples shall be treated during the lecture hours

#### **Exercises:**

1. The K<sub>p</sub> for this equilibrium reaction:

 $^{NH_4Cl}{}_{(s)}$   $\stackrel{\longleftarrow}{\longleftarrow}$   $^{NH_{3(g)}}$  +  $^{HCl}{}_{(g)}$  is 0.11 at 25°C, calculate K<sub>c</sub> at this temperature.

2. The following results were obtained during

analysis of a reaction 
$$CO_{2(g)} + H_{2(g)}$$

$$CO_{(g)} + H_2O_{(g)}$$

3. At 25°C and 4 atm.,  $PCl_5$  is 10% dissociated, calculate the  $K_p$  for this reaction,  $PCl_{5(g)}$  $PCl_{3(g)} + Cl_{2(g)}$ 

Case II: A ←→ 2B

e.g. Decomposition of  $N_2O_4$ , i.e  $\sqrt[4]{2}O_4$ 

$$K_c = \frac{\left[NO_2\right]^2}{\left[N_2O_4\right]} = \frac{\left(2x/V\right)^2}{\left(\frac{a-x}{V}\right)}$$

$$\therefore K_c = \frac{4x^2}{(a-x)V}$$

In term of K<sub>p</sub>,

$$K_p = \frac{[NO_2]^2}{[N_2O_4]} = \frac{P_{NO_2}^2}{P_{N_2O_4}}$$

Also, while considering the equation, if x represent the degree of dissociation, then 2x of  $NO_2$  will be produced, then 1-x of  $N_2O_4$  will be left. then, the total number of moles present at equilibrium = (1-x) + 2x = 1 + x.

$$\therefore P_{N_2O_4} = \left(\frac{1-x}{1+x}\right)P \quad P_{NO_2} = \left(\frac{2x}{1+x}\right)P$$

So, 
$$K_p = \frac{P_{NO_2}^2}{P_{N_2O_4}} = \frac{\left[\left(\frac{2x}{1+x}\right)P\right]^2}{\left(\frac{1-x}{1+x}\right)P}$$

$$\therefore K_p = \frac{4x^2P}{1-x^2}$$

#### **Examples:**

- $1.\,N_2O_4$  at 1 atm and  $25^{\circ}C$  dissociated by 18.5%, calculate its  $K_p$  at this temperature. If the atmospheric temperature was reduced to half its original value at the same temperature, calculate the degree of dissociation of the gas.
- 2. N<sub>2</sub>O<sub>4</sub> is 25% dissociated at 30<sub>o</sub>C and 1 atm., calculate
- (a) The equilibrium constant for the decomposition
- (b) The amount of NO₂ that would be attained if there had been 4 moles of N₂O₄ at the same temperature and pressure.

N.B- Solutions to these examples shall be treated during the lecture hours

#### **Exercises:**

- 1. N<sub>2</sub>O<sub>4</sub> is 25% dissociated at 37°C and 1 atm., calculate
  - (i) The  $K_p$  and (ii) the % dissociation at 0.1 atm and 37°C

2. An equilibrium mixture at  $27^{\circ}$ C contains  $N_2O_4$  and  $NO_2$  having 0.28 atm. and 1.1 atm. pressures respectively. If the volume of the container is doubled, calculate the new equilibrium pressure of the gases.

<u>Case III:</u> A + 3<del>B</del> → 2C

e.g. synthesis of Ammonia

$$N_{2(g)} + 3H_{2(g)} \rightleftharpoons 2NH_{3(g)}$$

$$\frac{a-x}{V} \frac{b-x}{V} \frac{2x}{V}$$

$$K_c = \frac{[NH_3]^2}{[N_2][H_2]^3} = \frac{(2x/V)^2}{\left(\frac{a-x}{V}\right) \times \left(\frac{b-x}{V}\right)^3}$$

$$\vdots$$

$$K_c = \frac{4x^2V^2}{(a-x)(b-x)^3}$$

Also,

$$K_{p} = \frac{P_{NH_{3}}^{2}}{P_{N_{2}} \times P_{H_{2}}^{3}}$$

## **Examples:**

- 1. In an experiment, H<sub>2</sub> and N<sub>2</sub> in the mole ratio 3:1 produced 0.0735mole fraction of NH<sub>3</sub> at 350°C and total pressure of 1013KNm<sup>-2</sup>. Calculate Kp for the forward and reverse reactions
- 2. The K<sub>p</sub> for this equilibrium reaction

 $N_{2\,(g)} + 3H_{2\,(g)} \implies 2NH_{3\,(g)}$  is 1.45 x 10<sup>-5</sup> at 500°C. Calculate the partial pressure of NH<sub>3</sub> when the partial pressure of H<sub>2</sub> is 0.928atm and that of N<sub>2</sub> is 0.432atm.

#### **Exercise:**

- 1. The dissociation pressure of CaCO<sub>3</sub> is 342mmHg at 840°C and at 860°C, the dissociation pressure is 420mmHg. Calculate the heat of dissociation of the carbonate. Given that R=8.314KJmol<sup>-1</sup>.
- 2. consider this reaction

 $N_{2 (g)} + 3H_{2 (g)} \longrightarrow 2NH_{3 (g)}$ , The  $K_p$  is 1.64x10<sup>-4</sup> at 400°C. calculate (i) the  $\triangle G$  of the reaction (ii)  $\triangle G$  when the partial pressure of N<sub>2</sub>, H<sub>2</sub> and NH<sub>3</sub> are 10atm, 30 atm and 3 atm respectively.

## HOMOGENOUS (LIQUID) EQUILIBRIA

$$A_{(I)} + B_{(I)} \rightleftharpoons C_{(I)} + D_{(I)}$$
e.g.  $CH_3COOC_1 + C_2H_5OH_{(I)} \rightleftharpoons CH_3COOC_2H_5_{(I)} + H_2O_{(I)}$ 
 $t=0$  a b 0 0
 $t=t$  a-x b-x x x

X

X

$$K_{c} = \frac{\left(\frac{x}{V}\right) \times \left(\frac{x}{V}\right)}{\left(\frac{a-x}{V}\right) \times \left(\frac{b-x}{V}\right)}$$

$$K_c = \frac{x^2}{(a-x)(b-x)}$$

The equation above is the general expression for the liquid equilibria. However, in the example above where water molecule is involved, the expression can be written as

$$K_c = \frac{\left[ CH_3COOC_2H_5 \right] \left[ H_2O \right]}{\left[ CH_3COOH \right] \left[ C_2H_5OH \right]}$$

$$\frac{K_{c}}{[H_{2}O]} = K_{c}' = \frac{[CH_{3}COOC_{2}H_{5}]}{[CH_{3}COOH][C_{2}H_{5}OH]}$$

The above expression is written in term of  $K_c$  because the concentration of water is taken to be constant,  $K_c$  has the unit of  $[Concn]^{-1}$  but  $K_c$  has no unit.

#### **Example:**

- In an esterification process between 1 mole of ethanoic acid and 1 mole of ethanol at 25°C, 66.7% of the acid is esterified calculate the equilibrium constant and ∆G°.
- 2. When 1 mole of ethanoic acid and 1 mole of ethanol were heated together at a temperature of

25°C until the equilibrium is reached. Titration of the reaction mixture shows that 2/3 of the acid have been used up. Calculate the equilibrium constant.

#### **HETEROGENEOUS EQUILIBRIA SYSTEM**

Heterogeneous equilibrium is an equilibrium in which the reactants and the products are not in the same phase.

e.g. 
$$3Fe_{(s)} + 4H_2O_{(g)} \longrightarrow Fe_3O_{4(s)} + 4H_{2(g)}$$

$$K_{c} = \frac{[Fe_{3}O_{4}][H_{2}]^{4}}{[Fe]^{3}[H_{2}O]^{4}} = \frac{1 \times [H_{2}]^{4}}{1 \times [H_{2}O]^{4}} = \frac{[H_{2}]^{4}}{[H_{2}O]^{4}}$$

N.B: the concentration of substances in solid phase is taken to be unity.

In term of  $K_p$ ,

$$K_{p} = \frac{P_{H_{2}}^{4}}{P_{H_{2}O}^{4}}$$

Exercises: Express the equilibrium constants  $K_p$ , for the following reactions.

1.  $CaCO_{3(s)}$   $\longrightarrow$   $CaO_{(s)} + CO_{2(g)}$ 2.  $2H_2O_{(l)}$   $\longrightarrow$   $2H_{2(g)} + O_{2(g)}$ 3.  $NH_4CI_{(s)}$   $\longrightarrow$   $NH_{3(g)} + HCI_{(g)}$ 

## **Le-Chatelier's Principle**

It states that "if a chemical system is in equilibrium and one of the factors involved in the equilibrium is altered, the equilibrium will shift, so as to neutralize the effect of the change".

## FACTORS AFFECTING EQUILIBRIUM

The factors are: temperature, concentration and pressure of the reactants and products, catalyst.

N.B: catalyst does not change the position of equilibrium, but affects the reaction equally in both directions.

1. Effect of temperature changes on equilibrium mixture: If a chemical system is in equilibrium and the temperature is lowered, the equilibrium position according to Le-Chatelier's Principle will shift so as to neutralize the cooling effect by releasing more heat.

Conversely, if the temperature is raised, the equilibrium position will shift so as to neutralize the heating effect by absorbing more heat.

e.g. 
$$H_2O_{(1)} \iff H_2O_{(g)} \triangle H=+ve$$

Since the forward reaction is an endothermic, if the temperature is raised, more steam will be produced and the equilibrium position will shift to the right. On the other hand, if the temperature is lowered, the equilibrium position shifts to the left and more water will be formed as the steam condenses.

The table below summarises the effect of temperature change on the equilibrium position.

Reversible reactions where forward rxn is	When the temp. of equilibrium system		
endothermic	increases	decreases	
$N_2O_{4(g)} \longrightarrow 2NO_{2(g)}$ $N_{2(g)} + O_{2(g)} \longrightarrow 2NO_{(g)}$ $PCI_{5(g)} \longrightarrow PCI_{3 (g} + CI_{2(g)}$	Equilibrium position shifts to right, favouring forward rxn. Kincreases	Equilibrium position shifts to left, favouring backward rxn. Kdecreases	
Forward rxn is exothermic	Equilibrium	Equilibrium	

$$2SO_{2(g)}+O_{2(g)} \longrightarrow 2SO_{3(g)}$$

$$2H_{2(g)}+O_{2(g)} \longrightarrow 2H_2O_{(g)}$$

$$N_{2(g)}+3H_{2(g)} \longrightarrow 2NH_{3(g)}$$

position shifts to right, favouring forward rxn. Kincreases

2. Effect of pressure changes on equilibrium mixture: This effect occurs in gaseous state reactions in which the total numbers of moles of gaseous molecules on the left hand side of the equation differ from that on

the right hand side of the equation.

When the pressure of a system at equilibrium is increased, then the reaction that involves a reduction in pressure will be favoured. This is in line with the Le-Chatelier's principle. Conversely, if the pressure is lowered for a system at equilibrium, the reaction that will increase the pressure will be favoured.

e.g 
$$N_{2(g)} + 3H_{2(g)} \iff 2NH_{3(g)}$$
  
4 moles 2 moles

The forward reaction involves a decrease in the number of moles and hence, a decrease in the pressure of the system. Also, the backward reaction gives an increase in the number of moles, and hence an increase in the pressure of the system.

In the formation of ammonia, a high pressure will favour the forward reaction (where a reduction in volume occurs). This causes the equilibrium position to shift to the right. on the other hand, a low pressure will cause the equilibrium position to shift to the left, favouring the backward reaction.

The table below summarises the effect of a change in pressure on the equilibrium position.

Reversible reactions	Shift in equilibrium position when the pressure	
1.Forward rxns (decrease in vol)	Increases	decreases
$ 2SO_{2(g)} + O_{2(g)} \iff 2SO_{3(g)} \\ 3H_{2(g)} + N_{2(g)} \iff 2NH_{3(g)} \\ 2CO_{(g)} + O_{2(g)} \iff 2CO_{2(g)} $	right right right	Left Left Left
2.Forward rxns (increase in vol)  N₂O₄(g) ← 2NO₂(g)	Left	right

3.No change in volume	
$H_{2(g)} + I_{2(g)} \longrightarrow 2HI_{2(g)}$ $3Fe_{(s)} + 4H_2O_{(g)} \longrightarrow Fe_3O_{4(s)}$ $2H_{2(g)}$	
-(3)	

NB: the value of K remain constant irrespective of the shift in the equilibrium position.

- 3. Effect of concentration changes on equilibrium mixture: if the concentration of any of the substances present is changed without a change in any of the other conditions. According to Le-chatelier's principle, the equilibrium position will move to increase the concentration of the added substance.
- e.g.  $N_{2(g)} + O_{2(g)} \implies 2NO_{(g)}$ The addition of more reactants (either  $N_2$  or  $O_2$  or both)will upset the equilibrium. For the system to adjust, the equilibrium position will shift to the right thereby favouring the forward reaction. This results in a proportional increase in the concentration of the product.

Similarly, if the product formed is continually removed fom the system, the equilibrium position will shift to the right to produce more of the product.

The effect of concentration change on equilibrium can be summarise in the table below

Reversible reactions	Addition of reactants or removal of products	removal of reactants or addition of products
CaCO <sub>3(g)</sub> $\iff$ CaO <sub>2(g)</sub> +CO <sub>2(g)</sub> $N_{2(g)}+O_{2(g)} \iff 2NO_{(g)}$ $3Fe_{(s)}+4H_2O_{(g)} \iff Fe_3O_{4(s)}$ $+4H_{2(g)}$	Equilibrium position shifts to the right	Equilibrium position shifts to the left

NB: the value of K remain constant irrespective of the shift in the equilibrium position.

4. Effect of Catalyst: Addition of catalyst has no effect on either the equilibrium constant or shift. It only speed up the rate at which the equilibrium is reached.

CHEMICAL EQUILIBRIUM IN SOLUTION

a. Dissociation of water:

$$H_2O_{(L)} \longrightarrow H^+ + OH^-$$

$$K = \frac{\left[H^{+} \right] O H^{-}}{\left[H_{2} O\right]}$$

But  $\left[H^+\right] = \left[OH^-\right] = 10^{-7} \,$  mol/dm³ at 25°C and  $\left[H_2O\right] =$  constant

$$K_w = [H^+][OH^-] = 1 \times 10^{-14}$$

 $K_{\scriptscriptstyle W}$  is the water dissociation constant.

## **Examples**

- 1. Calculate the [OH ] of the 0.01M HCL
- 2. Calculate the [H <sup>+</sup>] of the 0.0001M NaCL

## (b). Hydrolysis and hydrolysis constant

when a salt of a strong acid and a strong base dissolved in water, the water remains neutral. However, when a salt formed from a strong acid and a weak base or vice versa is dissolved in water, it either make the water acidic or basic.

e.g. (a) salt of strong base-weak acid like sodium ethanoate

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(CH<sub>3</sub>COONa) react with water to give an alkaline solution.

$$CH_3COO^- + H_2O \iff CH_3COO^- + H^+ + OH^-$$
  
 $CH_3COOH + OH^-$ 

As the CH<sub>3</sub>COO <sup>-</sup> consume the H<sup>+</sup>from water to form ethanoic acid, more of the water molecules dissociate to produce more of their ions.

At equilibrium,

$$K_{a} = \frac{[HEt][OH^{-}]}{[Et^{-}][H_{2}O]}$$

**But** 

$$\frac{[HEt][OH^-]}{[Et^-]} = [H_2O]K_a = K_h$$

 $K_h$  is the hydrolysis constant, but  $K_w = [H^+][OH^-]$ 

$$\therefore \qquad \left[OH^{-}\right] = \frac{K_{w}}{\left[H^{+}\right]} = \frac{K_{w}}{K_{a}}$$

The hydrolysis constant  $K_{h i}$ s related to the aci dissociation constant by the expression

$$K_h = \frac{K_w}{K_a}$$

The degree of hydrolysis,  $\alpha$ , is the fraction of the salt which has undergone hydrolysis when equilibrium is reached and it is given by

$$\alpha = \sqrt{\frac{K_{w}}{K_{h} \times C}}$$

(b). salt of weak base-strong acid, e.g NH₄Cl.

$$NH_{4(aq)}^{+} + H_2O_{(aq)}$$
  $\longrightarrow$   $NH_4OH_{(aq)} + H_{(aq)}^{+}$ 

$$K_h = \frac{\left[NH_4OH\right]\left[H^+\right]}{\left[NH_4^+\right]}$$

but 
$$[H^+] = \frac{K_w}{[OH^-]}$$

$$\therefore K_h = \frac{K_w}{K_b}$$

The hydrolysis constant is given by

$$K_h = \frac{K_w}{K_a \times K_b}$$

and the degree of hydrolysis is given by

$$\alpha = \sqrt{\frac{K_w}{K_a \times K_b}}$$

# **Solubility Product**

When a sparingly soluble salt e.g AgCl dissolves in water at a given temperature, a stage will be reached when it will not dissolve further and both the solid and and solution will co-exist in equilibrium.

$$AgCI_{(aq)} \longrightarrow Ag^{+}_{(aq)} + CI^{-}_{(aq)}$$

$$K = \frac{\left[Ag^{+}\right]\left[Cl^{-}\right]}{\left[AgCl\right]}$$

$$K[AgCl] = [Ag^+][Cl^-] = K_{sp}$$

#### **Examples**

- 1. Calculate the hydrolysis of a base whose dissociation constant is 1.75 x 10<sup>-5</sup>.
- 2. The solubility of CuBr is found to be 2.0 x 10<sup>-4</sup> mol/L at 25°C. calculate K<sub>sp</sub> value for CuBr.
- 3. The solubility of Mg(OH)<sub>2</sub> at 25°C is 0.00764g/L. what is the value of  $K_{sp}$  for Mg(OH)<sub>2</sub>?

#### **Exercises**

- 1. Calculate the K<sub>sp</sub> of AgCl whose solubility at 25°C is 1.05x 10<sup>-5</sup> mol/L.
- 2. The solubility of BaSO<sub>4</sub> at  $18^{\circ}$ C is 0.00233g/L. what is the value of  $K_{sp}$  for BaSO<sub>4</sub>?

# **Common-ion Effect**

When a soluble salt (say, A<sup>+</sup>C<sup>-</sup>) is added to a solution of another salt (A<sup>+</sup>B<sup>-</sup>) containing a common ion (A<sup>+</sup>), the dissociation of AB will be suppressed.

$$AB \longrightarrow A^+ + B^-$$

By the addition of the salt (AC), the concentration of  $A^{\dagger}$  increases. In line with the Le-chatelier's principle, the equilibrium will shift to the left, thereby decreasing the concentration of  $A^{\dagger}$  (i.e the degree of dissociation of AB will be reduced).

Thus, the reduction of the degree of dissociation of a salt by the addition of a common-ion is called the common-ion effect.

## **Examples**

- 1. Calculate the [H<sup>+</sup>] when 0.1 mol acetic acid was treated with 0.2 mol acetate ion. The equilibrium constant is 1.8x 10<sup>-5</sup>.
- 2. Calculate the [H<sup>+</sup>] when 1 mol of sodium formate was added to 0.5 mol formic acid. Given that K= 1.8x 10<sup>-5</sup>.

**AMBASSADOR**