**CSc 841: Computer Performance Evaluation HOMEWORK: Exponential queuing models** 

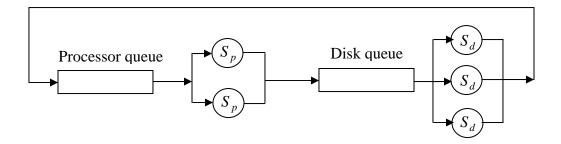


Figure. 1 A queueing model of a computer system with two processors and three disk units

- 1. Multiprogrammed computer system with 2 processors and 3 disks processes 4 identical programs. We assume that the processors and disks can be modeled as shown in Fig. 1. Each program needs 10 CPU minutes. Processor service time  $S_p$  and the disk service time  $S_d$  satisfy the relation  $S_d = 2S_p$ .
- (a) Show the state-transition-rate diagram and compute the utilization of each processor.
- (b) Compute the response time (i.e. the time for processing the workload of 4 programs in the multiprogrammed environment).
- (c) Suppose that one processor is down and the system works with only one active processor. What is the processor utilization? What is the response time?
- 2. A network server has 2 processors and processes transactions coming from 6 workstations. The average think time is Z=8 sec, and the average processor service time is S=2 sec.
- (a) Show the queueing model, the state-transition-rate diagram, and solve the balance equations. Compute the processor utilization, U, and the average response time R.
- (b) Compute U and R for a system having a single, but two times faster, processor. What is better: (a) or (b), and why? Compare the curves of response time R(n) for (a) and (b).
- (c) In the case (b) what is the critical number of users  $n^*$  and what is the response time for n=30?