*Abstract*—In the context of GPS-denied navigation, many algorithms are being developed that fuse information from alternative sensors such as visible and infrared cameras, RADAR, and LIDAR. However, the vast majority of these algorithms are tied to particular combinations of sensors and platforms. This is especially common at high technology readiness levels. Therefore, in order to limit the cost of future development, testing, and integration, it is desirable to break coupled solutions into component parts that can be managed independently.

In this paper, we describe a modular framework for trajectory optimization. This framework serves three major purposes: i) To facilitate the development of new sensors and algorithms; ii) To assist system integrators in testing a variety of navigation components such that their accuracy can be characterized on a level playing field; and iii) To enable hot-swapping of navigation components that have not necessarily been tested together.

Our approach is to identify the broad structure of the problem while leaving the details to be implemented differently for each application. We derive a probabilistic objective function closely related to a graph-based SLAM formulation and then illustrate the physical interpretation of each mathematical term with concrete examples.

We present the results of trajectory optimization given real imagery and several additional simulated data sources. Novel contributions to visual processing are discussed, and a new evolutionary optimization method is proposed.

To encourage adoption of our methodology, the framework and several example components are being made available online as an Open Source project [5].

# Introduction

Trajectory optimization is a general approach to navigation, or continuous self-localization relative to a global frame, that optimally fuses information from all available sources while satisfying dynamic constraints. Algorithms that use this approach are often considered too slow for real-time applications because the general problem varies in structure and complexity with increasing time, changes in platform dynamics, and sensor availability. Therefore, a variety of approximations to the general nonlinear problem have been introduced, such as; linearization of motion dynamics, graph- or tree-based pose representation, particle representation of instantaneous states, and sensor model simplification and linearization. Some algorithms estimate motion in fewer than six Degrees of Freedom (6-DoF), providing position only, orientation only, or coordinates constrained to a local plane. Some maintain a history of motion, while others keep a current state estimate, resulting in non-uniform treatment of absolute information (e.g. GPS) versus relative information (e.g. visual feature tracking). These approximation techniques have led to a variety of tractable problems and corresponding optimization algorithms.

Many effective navigation devices are already in widespread use. However, nearly all existing implementations are tied to particular sensors and platforms, resulting in stove-piped architectures. For example, algorithms that map the environment usually require a rangefinder or camera to be available continuously. Although some systems are robust to sensor removal, we know of none that support the addition of new sensor types at runtime.

In this paper, we describe the Trajectory Optimization Manager for Multiple Algorithms and Sensors (TOMMAS) [5][7]. TOMMAS is an object-oriented framework that standardizes the all-source, all-platform, maximum likelihood navigation problem with nonlinear state evolution and measurement error distributions. It clarifies the line between abstract trajectory optimization and many specific practical implementations. It is not an algorithm, so it cannot be evaluated in terms of computational complexity. However, it facilitates rapid algorithm development, assists system integrators in testing the accuracy of algorithms and sensors on a level playing field, and enables hot-swapping of navigation components that have not necessarily been tested together in advance.

## The Framework and Its Component Parts

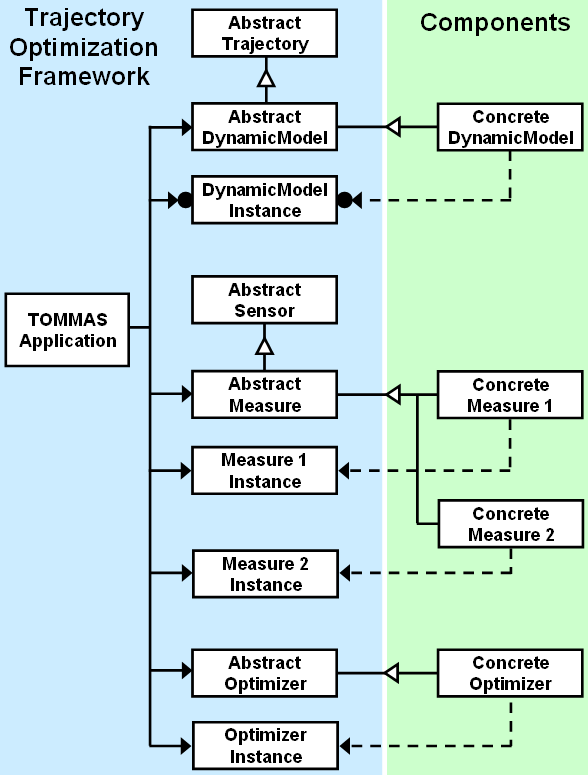


Fig. . Class inheritance diagram illustrating the use of the factory pattern to manage components. The graphical notation is from Design Patterns [8].

The TOMMAS framework defines interfaces for the communication of navigation-relevant information, partitioning the navigation problem into three abstract classes of components:

1. A DynamicModel relates a set of parameters to the rigid body trajectory of a physical system such as a car, airplane, or person. This interface also provides stochastic information about the parameters known prior to data collection.
2. A Measure evaluates a given trajectory against navigation-relevant information from one or more sensors. It represents a novel concept in which algorithms, sensors, and their calibration data are packaged together. Neither raw data nor sensor-specific features are communicated through this interface.
3. An Optimizer is an algorithm that finds one or more elements in the set of maximum likelihood trajectories by intelligently generating and modifying the parameters of one or more DynamicModel instances and passing them through zero or more Measure instances.

A component implementation that meets any of the TOMMAS interface specifications is interchangeable with others of the same type at runtime. This extreme level of modularity comes at the expense of support for raw data access or cross-sensor mapping. However, TOMMAS places no limits on external interfaces beyond its use of the namespace tom.

## Benefits to System Integrators

TOMMAS simplifies system integration by leaving the details of component implementation to specialists. A system integrator interacts with the framework by specifying a set of components that inherit from base classes as in Fig. 1. These components represent the physical system and define optimality for a specific application. The framework then provides an Application Programming Interface (API) that makes it easy for the system integrator to manage components and to optimize the scalar objective function derived in a later section.

The TOMMAS interface standard creates a level playing field for evaluation and competition between components. There are no framework parameters to tune at integration time, so new components can be developed and validated independently. Furthermore, the project code and documentation are Open Source and BSD Licensed in order to encourage widespread adoption of TOMMAS, which could lead to new markets for packaged navigation sensors and algorithms.

## Related Work

Current state-of-the-art navigation algorithms include the Extended Kalman Filter (EKF) [34], Unscented Kalman Filter (UKF) [17], Ensemble Kalman Filter (EnKF) [5], other Particle Filters (PF) [29], and a variety of Simultaneous Localization and Mapping (SLAM) techniques such as Occupancy Grid Mapping [33], Atlas [1], Tree Based Network Optimization (TORO) [11], Incremental Smoothing and Mapping (iSAM) [18], and general Graph Optimization [12].

This work identifies a universal structure shared by nearly all of the above algorithms. In many ways, TOMMAS represents the wrapping in which these algorithms can be packaged. It is not a centralized repository for gathering navigation software, like OpenSLAM [32], the Carnegie Mellon Robot Navigation Toolkit (CARMEN) [24], or Willow Garage’s Robot Operating System (ROS) [28], but it has the potential to enhance interoperability within and across various software repositories.

## Comparison to Graph-Based SLAM

In order to illustrate structural similarities and differences between our problem formulation and an existing formulation in SLAM literature, we compare TOMMAS and Grisetti’s description of Graph Based SLAM (GBSLAM) [13]. Both formulations optimize trajectories in 6-DoF with respect to a graph based objective function. However, GBSLAM and TOMMAS differ in the following ways:

In GBSLAM, the solution space is a vector of parameters that describe a set of instantaneous poses in 6-DoF. In TOMMAS, the solution space is a slightly more structured set of parameters that, together with an explicit dynamic model, describe a class of 6-DoF  continuous trajectories.

Dynamic models are not explicit in GBSLAM. In contrast, TOMMAS defines an explicit dynamic model interface. From a theoretical perspective, this distinction may be trivial. However, from a design perspective, TOMMAS provides a clear placeholder for statistical knowledge and assumptions about the mobility of individual platforms. For example, if a vehicle has planar holonomic dynamics, then that self-knowledge can be packaged into a TOMMAS component that is supplied with the vehicle.

GBSLAM formulates measurements as “zero noise observations” of transformations between poses, accompanied by an information matrix for each measurement. TOMMAS defines general nonlinear measures on the trajectory space, which includes the space of velocities and orientation rates. These measures do not need to fit a quadratic form or have a unique minimum corresponding to a zero noise observation.

In GBSLAM, there is a single graph with uniform indexing that lumps together information from several sensors and information from an implicit dynamic model. The TOMMAS objective has a more detailed structure. It allows for multiple graphs, usually one graph per sensor, and these are separate from the dynamic model. This clarifies the distinct roles of each component. Internal to a TOMMAS optimization method, the individual graphs can be combined into a single graph if the underlying algorithm does not recognize these distinctions.

# Navigation by Cost Graph Optimization

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| --- | --- | --- |
| Table . Basic Sets |  | Table . Embellishments |
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| --- |
| Table III. Framework Variables and Functions |
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The mathematical objective of trajectory optimization is to find one or more elements in the set of maximum likelihood trajectories  given the data , as in

.

The problem can be reduced to finding one or more elements in the set of maximum likelihood parameter vectors  subject to the dynamic model constraint  given the data , as in

.

See Section III for more details about the role of dynamic models in our formulation.

The likelihood maximization problem can be converted to a cost minimization problem by taking the negative log of the distribution as follows:

.

In order to impose structure onto the problem, we divide the total probability over the parameter space into marginal parts. By assuming that the probability mass for each  is independently identically distributed and that the probability mass functions associated with each measure are independent, the application of Bayes theorem leads to the following product of terms in a graph structure:



Any arbitrary function that does not depend on  can be added to the objective without affecting its overall shape or minimizing solution(s). We take advantage of this fact to utilize partially known mass functions (ie. those that are only known over a part of their domain or those with an unknown integral). As a matter of convention, we divide each term by its infinity norm, which ensures that the minimum value of the objective will be non-negative:



Finally, we substitute the individual summands with the our notation for the prior measure  and the conditional measures , leading to the specific objective to be minimized

.

Once this problem has been solved, then the optimal trajectory can be computed by inserting the resulting parameters back through the dynamic model.

## Hints for Efficient Optimization

The framework allows an optimizer to query  and  before summation takes place in order to search for global minima in Eq. . This formulation suggests automated learning of the relationship between time indexed parameters and time indexed cost graphs. In general, neither convexity nor uniqueness of solution is guaranteed; however, specific sets of components can be designed to offer these guarantees.

## Time Domain Extension

The structure of the problem is fixed during a single optimization step, after which it is allowed to change. At that instant, the bounding indices , , , and  are refreshed to match the current structure of available information. The framework places the optimization method in control of the refresh process, so that it can poll for new information and exclude information, if necessary, as computational complexity increases.

# Dynamic Models for Deterministic Trajectory Generation

Consider the following general models for continuous or discrete nonlinear dynamic systems, where the vector-valued inputs and outputs are defined canonically (not using the notation in Table III):

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These equations have been established to model the dynamics of numerous physical systems, from Brownian particles to ground vehicles, fighter jets, and even animals. In the continuous case, the transition function  is typically placed in an integration loop, such that the instantaneous states  are computed incrementally at increasing time instants given an initial condition . The input  represents data that is known with exact precision, and the input  represents discrete parameters whose probability mass function is known. The implementation of the transition function and the integration method differ slightly in the discrete case, but the details do not affect our development.

If the modeled states include a rigid-body trajectory, and an interpolation method is specified, then the dynamics can be rewritten in functional form as follows (using the notation in Table III):

.

In this form, a dynamic model generates a rigid-body trajectory from a structured set of parameters. This serves dual purposes: It reduces the space of all continuous trajectories to a substantially smaller parameter space, and it provides a natural way to constrain navigation results to achievable platform dynamics.

A single parameter can affect the entire trajectory function. This attribute of our model has benefits and drawbacks. Benefits include guaranteed continuity of the trajectory and the ability to apply functional measures (see Section IV). The main drawback is the lack of efficient optimization techniques designed to interact with this type of model.

A dynamic model is a deterministic function that depends on stochastic parameters. Assuming that the set of all possible parameter vectors comprises a probability space, and that parameter vectors are independently and identically distributed according to the probability mass function , we identify a key component of the objective function:

.

The TOMMAS DynamicModel class standardizes the interfaces to  and . It stores and provides access to the stochastic parameters  that perturb the  continuous 6-DoF rigid-body trajectory . Motion is defined relative to the Earth-Centered Earth-Fixed (ECEF) frame and time is defined in seconds since midnight on 1980 JAN 06 (GPS standard). The class provides a general interface for specifying the structure of  and enforces that the domains of  and  grow in a consistent manner as time moves forward. Finally, in order to support optimizers that expect to manipulate real parameters, methods for converting integer parameters to real numbers and vice versa are specified.

# Graph-Based Trajectory Measures

Consider the following general nonlinear sensor model in canonical form (not using the notation in Table III)

,

where the function  returns an instantaneous measurement vector  whose value depends on an instantaneous state  and the error parameters . Many sensors have been modeled using this form. However, some sensors of interest simply do not produce instantaneous measurements.

A common example of a non-instantaneous sensor is a gyroscope. Although gyroscopes are often modeled as if they measure instantaneous rotation rates, they are most accurately modeled as measuring changes in orientation over discrete time periods [20].

Another example is a sensor that identifies a single feature appearing in two images taken at different times. The feature displacement in image coordinates depends on the position and orientation of the sensor when each of the images was acquired, among other factors.

## Graph-Based Measurement Model

Measurements may accumulate information over multiple times or may arise from integration over an interval of time. In general, these time intervals can overlap, leading to a functional measurement model

,

where each pair of node indices  forms an edge in an incomplete graph, as illustrated in Fig. 2. Indices and time stamps must be related by a known monotonically increasing function, such that a given pair of indices associates a single measurement with the closed time interval . The time stamps do not need to be regularly spaced or frequent.

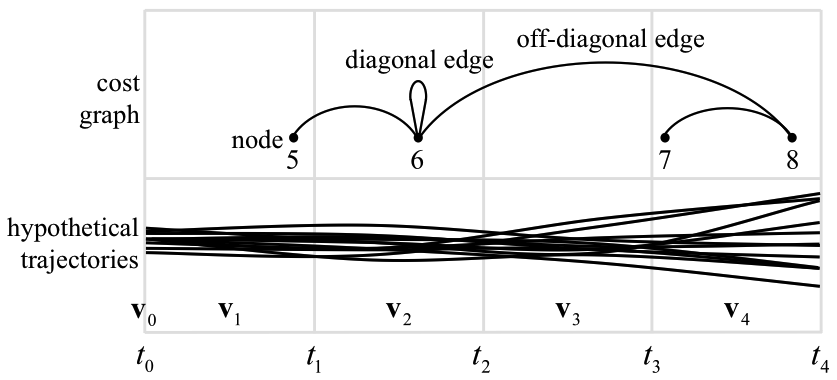


Fig. . Relationship of indices between a cost graph and a set of hypothetical trajectories. Each block corresponds to a discrete time period.

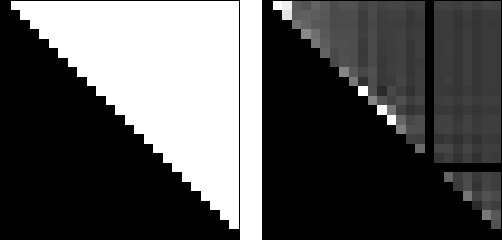


Fig. . Graph adjacency (left) and edge cost (right) for a single trajectory evaluated by a relative measure. The bright spots indicate data that is inconsistent with the trajectory. The dark horizontal and vertical lines indicate zero-cost edges associated with an invalid data node.

## From Measurements to Trajectory Measures

In order to clarify terminology, let *data* be the set of raw unfiltered numerical values recorded by all available sensors, including calibration values. The *data*  is assumed to be completely determined by the actual body *trajectory*  and a particular realization of the *error parameters* . Each *measurement*  can be any conceivable function of the *data*. We seek a *measure* of the relative likelihood of the observed *data* given any hypothetical *trajectory* .

Assuming that  is invertible with respect to , and remembering that  and  are functions of  and , the following error model is obtained:

.

This provides the basis of a trajectory measure for each algorithm or sensor and each graph edge as follows (using the notation in ):

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The TOMMAS Measure class standardizes the interface to each  without requiring explicit computation of  or . This not only has the potential to reduce processor burden, but it also makes it possible to wrap a wide variety of sensors and algorithms with a uniform interface. For example, suppose  represents a calibrated camera coupled with a sparse feature tracking algorithm, and  represents a GPS unit. Since they both possess the same interface, they can be tested and their performance can be compared on a level playing field.

# Examples of Optimizers

The most challenging aspect of TOMMAS is the development of efficient and adaptive optimization methods. We describe a few methods that we have implemented below, and we also propose future work in this field.

## Linear Kalman Filter

This component implements a parameter update step that is equivalent to the linear least squares update in a Kalman filter. It queries the Jacobian and Hessian of the cost function in the vicinity of the current trajectory hypothesis using finite differences and it uses these terms to derive the first and second moments of the equivalent normal distributions. These parameters go into the standard linear Kalman filter equations to compute new dynamic model parameters. This algorithm is efficient and optimal when the objective is quadratic, but it can be far from optimal otherwise.

## Matlab Genetic Algorithm

The MATLAB Genetic Algorithm and Direct Search (GADS) toolbox contains several functional optimization methods, one of which is a customizable Genetic Algorithm (GA). To use the MATLAB GA, we needed to implement two transformations; one that converts a set of dynamic model parameters into a bit string, and another that converts a bit string back into a set of parameters. In terms of configuration, we selected built-in uniform functions for initial population creation, parent selection, and mutation, along with single-point crossover and proportional fitness scaling. This optimization method is guaranteed to converge to the optimal solution, but it is relatively slow.

## Evolutionary Optimization with Linkage Learning

Using TOMMAS as a rapid development tool, we have begun to explore optimization techniques from the field of evolutionary computation, with a focus on linkage learning [10][3]. Linkage learning is a technique for implicitly discovering and exploiting correlations between various parameter inputs to the objective function and the resulting costs. The cost graph structure in the TOMMAS framework provides explicit information about these correlations that can be utilized in linkage learning. In addition, most dynamic models introduce an implicit correlation between the values of individual parameters and the resulting trajectory during limited intervals of time.

To build a foundation for discovering and exploiting these correlations, we review Holland’s fundamental theories of evolutionary computation below [13].

***The K-Armed Bandit Argument:*** Given a probabilistic decision between *K* options, it is a near-optimal strategy to allocate exponentially increasing numbers of trials to the observed best alternatives.

***The Schema Theorem:*** A Genetic Algorithm (GA) assigns exponentially increasing number of copies to combinations of parameter values that are consistently observed to be better, if those combinations also survive recombination and mutation operators with high probability. We call such highly survivable combinations of parameters building blocks.

***Implicit Parallelism:*** By processing a number of individuals using GA operators, a vastly larger number of building block combinations are implicitly processed in the near-optimal fashion discussed above.

***The Building Block Hypothesis:*** The core heuristic of the GA approach is that for many problems and encodings, recombination of building blocks yields high-quality solutions.

One way to apply these ideas is to design the objective function such that highly correlated parameters appear relatively close to one another in a string. As a population of strings are spliced and recombined at randomly selected crossover points, those parameters that are close together in the encoding will be more likely to survive than those that are far apart, thereby acting as building blocks. To some extent, this technique is already implicit in the TOMMAS definition of the dynamic model, because its input parameters are ordered by a time index.

Linkage learning offers a more advanced concept of building blocks in which parameter proximity only plays a minor role. In linkage learning algorithms, metrics and procedures are used to determine combinations of parameters whose values are correlated with better solutions. This information is used to alter the genetic operators to ensure that these combinations survive with high probability. Often, a linkage model, such as a map of the strength of pair-wise parameter correlations, is built to aid in biasing the survivability of parameter combinations .

A straightforward method of testing this theory is as follows: When crossing-over two individuals, the probability of taking a parameter from one of the two parents can be taken in proportion to the relative (inverse) magnitude of the costs on the edge(s) of the cost graph that are most affected by that parameter. Over generations of the evolutionary optimization process, this will tend to preserve sets of parameters that consistently lower overall costs as building blocks, since these will tend to be taken from a single parent.

In our future work, we will explore this simple scheme for using cost graphs to directly affect linkage, as well as methods that exploit more complex statistical analysis of cost graphs to build linkage models.

# Examples of Dynamic Models

The following examples are components that derive from the framework base classes. Components are polymorphic in the sense that any class that derives from the same base class can be substituted for any other.

## Bounded Markov Dynamic Model

As the name implies, this component implements a Markov motion model. It is a simple second order model of a free body in 6-DoF that is driven by a forcing function. The body has unit inertia in translation and rotation. The forcing function is piecewise constant and bounded in the range , where the scale  can be configured for a particular application. The cost function  is uniformly zero everywhere.

## Brownian Planar Dynamic Model

This component is based on the dynamics of a free body restricted to planar 3-DoF motion under the effect of bounded forces in the range . We call it Brownian because the probability of the force taking on any particular value is modeled by a truncated normal distribution. Therefore, the cost function  is convex, quadratic, and minimized when all elements of  lie in the middle of their range.

## Strapdown Inertial Integration Model

(To be completed by the date of publication.)



# Examples of Measures

We have implemented several components that inherit from the Measure class. Each of our examples corresponds to a single sensor, although it is possible to create a measure that extracts information from multiple sensors.

## Distance to the Nearest McDonalds

For the sake of illustration, consider a simplistic measure based on the verbal cue “I am near a McDonalds” and a database of locations of McDonalds restaurants in the contiguous United States. Suppose that the verbal phrase is interpreted as a mathematical measure of the shortest distance along the Earth’s surface between an observer and the stated landmark. shows what the function  might look like based on this information.



Fig. 4. Illustration of the distance to the nearest McDonalds within the contiguous United States [35].

## Visual Measure of Epipolar Tracking Error

We have developed a novel visual measure based on epipolar tracking error. This measure evaluates a trajectory given a pair of images. It finds salient point features in each image and matches them using either the Kanade-Lucas-Tomasei (KLT) Optical Flow algorithm or the Speeded Up Robust Features (SURF) algorithm. The KLT tracker exploits sparsity of features to expedite the matching process, while SURF offers greater robustness at a higher computational burden. Each feature match is returned as a pair of ray vectors  in the camera frame, derived from the image data and the camera projection in .

Given a trajectory that contains the position  and orientation  of the body frame, and assuming for the sake of discussion that the camera frame is coincident with the body frame, vectors in the camera frame can be rotated into the world frame as follows:



where  converts rotation from quaternion to matrix form, and the indices of matched visual features are . The two ray vectors in the world frame are then compared to the trajectory using

 ,

which is the sine of the angular difference between each feature ray vector and its corresponding epipolar plane. In practice, division by zero can be avoided by multiplying both sides by the denominator and propagating that scale factor through the rest of the development.

In order to assemble a visual measure, the characteristic distribution of  must be modeled using experimental data that includes ground truth. Tracker error is difficult to characterize, but for the sake of argument, we assume that each value of  is independently normally distributed according to .

If there is only one visual feature, such that , then the two parameters of the normal distribution are all that is needed to implement Eq. .

When there are multiple visual features, such that , the probability density over the set of all feature locations can be modeled by various statistics. Both the Sum of Absolute Differences (SAD) and the normalized Sum of Squared Differences (SSD) are plausible, and we know of no theoretical reason to choose one over the other. However, we could find no closed-form solution for the probability density function of , so we chose the normalized SSD statistic, which follows a chi-squared distribution

,

where  is the gamma function. In order to form the visual measure for two or more features, we need to know the maximum value of this distribution. In cases when , the maximum of the chi-squared distribution occurs when , and its corresponding value is

.

(This section will be updated to reflect the latest version of the algorithm by the date of publication.)

## Visual SfM-Based Measure

This measure computes camera motion given any pair of images from which at least eight matching point features can be extracted. It solves for the extrinsic transformations between camera poses (egomotion) up to a translation scale factor, and it also solves for scene structure up to an initial offset and scale. The transformations between camera poses are then stored in order to evaluate subsequent trajectory hypotheses relative to them.

Our algorithm is an adaptation of recent work on Structure from Motion (SfM) similar to [15], [27] and [31]. Like other TOMMAS components, this measure is intended as a starting point for further development, also known as a reference implementation. It is publicly available and licensed under GPL.

***SfM Algorithm:*** The algorithm begins by finding SURF interest points in a pair of images. Matching points are identified by extracting a SURF feature vector at each point and evaluating pairs using the nearest neighbor criterion [1].

Following the description in [15], RANSAC [8] detects and removes matches that are not mutually consistent with a set of known intrinsic calibration parameters while simultaneously fitting a geometric model to the data. This process iteratively employs the eight-point algorithm [14] to estimate the essential matrix in a linear least squares sense.

The linear estimate of the essential matrix is then further refined as follows: The essential matrix is factored into the product of a skew symmetric matrix and a rotation matrix, resulting in four possible solutions for the extrinsic transformation. Then, each pair of matched points is triangulated using each of the four solutions, and the solution which results in a positive depth for the highest number of pairs is selected. This solution is then recomposed into a projection matrix that becomes the initial condition for Sparse Bundle Adjustment (SBA) [21], which refines the estimate via local nonlinear optimization.

***Eight-Point Algorithm:*** Given a pair of matched interest points  in homogenous image coordinates observed at two times  and , the geometric epipolar constraint can be defined as

,

where  is the calibration matrix containing the camera intrinsic parameters, and  is the essential matrix.

To obtain a linear estimate of the elements of the essential matrix, this equation can be rearranged as

,

where is a column vector made up of the entries of in row-major order, and  is a row vector made up of the remaining values. Each pair of matched points gives rise to one equation. Therefore, the linear least squares estimate of  is the null space of the matrix formed by stacking at least eight constraint equations in rows.

The numerical stability of this method can be improved by forcing the essential matrix to have exactly two equal singular values. This can be done by replacing its singular values as follows

,

where and are the orthonormal matrices obtained by singular value decomposition (i.e).

***Proposed Measure:*** Assuming that the camera frame and body frame are coincident, the essential matrix is related to the body motion as follows



where  converts rotations from quaternion to matrix form, and the bracket notation  converts its argument to the matrix operator form of the cross product.

(To be completed by the data of publication)

Therefore, the recovered motion can be directly compared to the candidate trajectory which is represented as a relative quaternion and a relative translation. Hence, we compute the residual of as

.

# Simulation Results

(To be completed by the date of publication.)

# Open Source Implementation

In order to encourage widespread adoption, TOMMAS is provided online as an Open Source and BSD Licensed project [5]. The learning curve for creating a framework component is easily accessible to an individual engineer versed in navigation concepts and either ANSI C++ or MATLAB.

## Software Engineering Considerations

TOMMAS utilizes several features of object-oriented programming. In particular, it uses class abstraction, encapsulation, inheritance, namespaces or packages, and passing data by value and by reference. Most importantly, modularity is accomplished through polymorphic inheritance from abstract interface classes that implement the factory design pattern.

The stack diagram in Fig. 5 shows the minimal requirements for TOMMAS to run on an embedded system. We selected ANSI C++ for our reference interface because the language is strongly typed, and because it can be compiled on a large variety of platforms across the size, weight, and power (SWaP) spectrum.

All TOMMAS class definitions are mirrored in a weakly typed MATLAB interface. In addition, MEX code is provided that automatically wraps native ANSI C++ components with a MATLAB interface. This special feature bridges the gap between the two languages and greatly simplifies unit testing, as shown in Fig. 6.

Adopting the ANSI C++ version of TOMMAS imposes no computational overhead. As a pure virtual interface, TOMMAS guides system development and integration. Yet, most compilers will optimize (inline) its functions such that the interface adds zero processor cycles to the implementation. In other words, the computational burden is completely determined by the components that are selected at runtime.

TOMMAS has been successfully tested on several versions of Windows, Linux, and Mac using MSVC, g++, Xcode, and MATLAB.

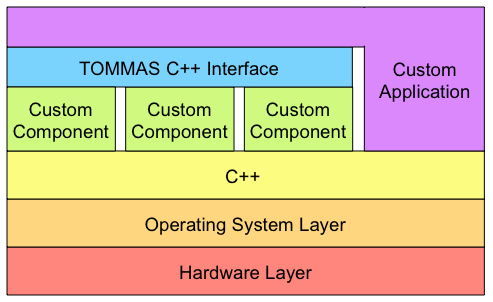


Fig. 5. Stack diagram for embedded TOMMAS components and applications.

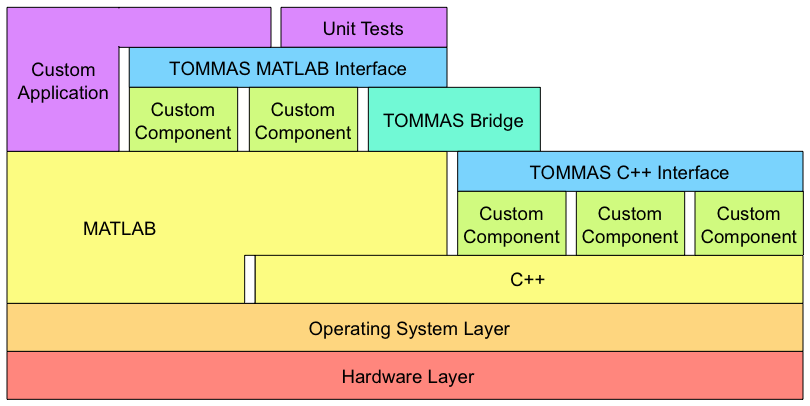


Fig. 6. Stack diagram for rapid development and testing of components through the TOMMAS Bridge between C++ and MATLAB.

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