## CS 188 HW 8 Challenge Question

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collaborators: none

## 1 Decision Networks and HMMs

6.1)

$$\begin{cases} EU(theater) = (0.5)(100) + (0.5)(10) = 55 \\ EU(rent) = (0.5)(80) + (0.5)(40) = 60 \\ \implies MEU(\emptyset) = 60 \\ \implies \underset{A}{\operatorname{argmax}} EU(A) = rent \end{cases}$$

6.2)

Since F is unobserved, S and M are independent due to common effect  $\Longrightarrow P(M|+s) = P(M)$   $\Longrightarrow \begin{cases} EU(theater|+s) = EU(theater) = 55 \\ EU(rent|+s) = EU(rent) = 60 \end{cases}$   $\Longrightarrow MEU(\{+s\}) = MEU(\{-s\}) = 60$   $\Longrightarrow \text{Optimal action for both } + s \text{ and } - s = rent$   $\Longrightarrow VPI(S) = 60 - 60 = 0$ 

6.3)

$$\begin{split} MEU(G) &= \max_{a} \sum_{m} P(m|G) \, U(m,a) \\ EU(theater|+g) &= (0.644)(100) + (0.356)(10) = 67.96 \\ EU(rent|+g) &= (0.644)(80) + (0.356)(40) = 65.76 \\ &\Longrightarrow MEU(+g) = 67.96 \\ EU(theater|-g) &= (0.293)(100) + (0.707)(10) = 36.37 \\ EU(rent|-g) &= (0.293)(80) + (0.707)(40) = 51.72 \\ &\Longrightarrow MEU(-g) = 51.72 \\ &\Longrightarrow VPI(G) &= (67.96)(0.59) + (51.72)(0.41) - 60 = 1.3016 \end{split}$$

- 6.4) (i) A is false. VPI is nonnegative.
  - B is true.  $S \perp \!\!\! \perp M$  when F is unobserved.
  - C is false. See above.
  - D is false.

$$MEU(+f) = 81.37, MEU(-f) = 43.8$$
  
 $VPI(F) = 65.5906 - 60 = 5.5906$ 

- E is false. VPI(G) = 1.3016
- (ii) A is false. VPI is nonnegative.
  - B is potentially true. For example. M-F might be a trivial edge.
  - C is potentially true. Observing G activates the path from S to M
  - D is potentially true. Depends on the CPT.
  - E is potentially true. Same reason as above.
- (iii) A is false. VPI is nonnegative.
  - B is true. Observing F blocks the path from G to M.
  - C is false. See above.
  - D is false. VPI(F) > 0.
  - E is false. VPI(G) > 0.
- (iv) A is false. See calculated value.
  - B is true.
  - C is false.
  - D is true.
  - E is false.

- 6.5) A is equivalent. Marginalization + memoryless property.
  - B is equivalent. Same as A by memoryless property.
  - C is not equivalent. Need to eliminate  $X_T$ .
  - D is not equivalent. Same reason as above.
- 6.6) Since we want backward recursion,

$$\beta(X_t) = \sum_{x_{t+1}} \beta(X_{t+1} = x_{t+1}) P(X_{t+1} = x_{t+1} | X_t) P(E_{t+1} = e_{t+1} | X_{t+1} = x_{t+1})$$

(CEBF)

- 6.7) A is false. Cannot eliminate  $X_t$ 
  - B is false. Equals  $P(X_t, E_{1:T})$  instead
  - $\bullet$  C is true. Equivalent to  $\frac{P(X_t, E_{1:T})}{P(E_{1:T})}$
  - D is false. Missing  $E_{t+1:T}$