

CS 188 HW 9 Challenge Question

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Collaborator: None

1 Naive Bayes and Perceptron

7.1) C,D,E,F

$$\begin{aligned}P(Y = spam|W = \{berkeley, rules\}) &= P(Y = spam)(1/6)(1/8) = \frac{P(Y=spam)}{48} \\P(Y = ham|W = \{berkeley, rules\}) &= P(Y = ham)(1/8)(1/12) = \frac{1-P(Y=spam)}{96} \\&\implies P(Y = spam) > 1/3 \text{ to be classified as spam}\end{aligned}$$

7.2) F,F,A,E

$$\begin{aligned}N_{spam} &= 12 \\N_{ham} &= 14 \\P(W = warning|Y = spam) &= 1/12 \\P(W = social|Y = ham) &= 1/14 \\P(W = office|Y = ham) &= 0 \\P(Y = ham) &= 2/3\end{aligned}$$

7.3)

$$\begin{aligned}P(W = warning|Y = spam) &= \frac{3}{12 + 2V} \\P(W = social|Y = ham) &= \frac{3}{14 + 2V} \\P(Y = ham) &= \frac{4}{7}\end{aligned}$$

7.4) B. 0.7 is the only likely one in the list because increasing k to fix overfitting, which naturally will decrease the accuracy of model, but not to an extreme as increasing k causes all probabilities to converge uniformly (i.e., half-half split between spam and ham; hence 0.1 is not possible).

- 7.5) i) D. 2 choices for Y , V choices for W_i and W_{i-1}
 ii) C. The new model will have more accuracy on the test data because it has more evidence variables it can use for determination.
- 7.6) Since the perceptron will classify the data correctly as A (due to highest activation score of 3), no changes will be made to the weights.

$$\begin{aligned}w_A &= [1, 2] \\w_B &= [2, 0] \\w_C &= [2, -1]\end{aligned}$$

- 7.7) The perceptron will classify the data entry as B (activation score of 2), which is incorrect given the real label. Therefore, w_B and w_C will be updated

$$\begin{aligned}w_A &= [1, 2] \\w_B &= [-1, 0] - [-2, 1] = [1, -1] \\w_C &= [2, -2] + [-2, 1] = [0, -1]\end{aligned}$$

- 7.8) C. Only w_B will converge by not changing throughout the training, whereas w_A and w_C will alternate between values. This can be seen by performing 1 iteration of training on the dataset
- (a) $w_A = [1, 0], w_B = [1, 1], w_C = [3, 0]$ (initial condition)
 - (b) $w_A = [2, 1], w_B = [1, 1], w_C = [2, -1]$ (incorrectly identified A as C)
 - (c) $w_A = [2, 1], w_B = [1, 1], w_C = [2, -1]$ (correctly identified B)
 - (d) $w_A = [2, 1], w_B = [1, 1], w_C = [2, -1]$ (correctly identified C)
 - (e) $w_A = [1, 0], w_B = [1, 1], w_C = [3, 0]$ (incorrectly identified A as C; return to initial condition)