Find the mass in kilograms of  $7.50\times10^{24}$  atoms of arsenic, which has a molar mass of  $74.9 \mathrm{g/mol}$ .

#### 1.1 Solution

Convert atoms to moles.

$$\frac{7.50 \times 10^{24} \text{ atoms}}{6.02 \times 10^{23} \text{ atoms/mol}} = 12.458 \text{mol}$$
 (1)

Using the molar mass, convert moles to grams.

$$12.458 \text{mol} * 74.9 \text{g/mol} = 933.140 \text{g} = \boxed{0.933 \text{kg}}$$
 (2)

Oxygen gas having a volume of  $1000 \text{cm}^3$  at  $40.0^{\circ}\text{C}$  and  $1.01 \times 10^5\text{Pa}$  expands until its volume is  $1500 \text{cm}^3$  and its pressure is  $1.06 \times 10^5\text{Pa}$ . Find (a) the number of moles of oxygen present and (b) the final temperature of the sample.

#### 2.1 Solution (a)

We can use the ideal gas law for this. We apply it to the first case, converting the 40.0°C to Kelvin.

$$40^{\circ}\text{C} = 313.15\text{K}$$
 (3)

$$1000 \text{cm}^3 = 1000 \times 10^{-6} \text{m}^3 = 1 \times 10^{-3} \text{m}^3 \tag{4}$$

$$pV = nRT (5)$$

$$n = \frac{pV}{RT} = \frac{1.01 \times 10^5 \text{Pa} * 10^{-3} \text{cm}^3}{8.31 \text{J/mol} \cdot \text{K} * 313.15 \text{K}}$$
(6)

$$= \frac{1.01 \times 10^2 \text{N} \cdot \text{m}}{2602.2765 \text{J/mol}} = \boxed{0.038812 \text{mol}}$$
 (7)

#### 2.2 Solution (b)

The ideal gas law (or an equivalent) will be used here. The number of moles does not change here, neither does the gas constant R. We can use the to solve for the final value of the temperature.

$$\frac{p_1 V_1}{n_1 T_1} = \frac{p_2 V_2}{n_2 T_2} \tag{8}$$

$$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2} \tag{9}$$

$$T_2 = T_1 * \frac{p_2 V_2}{p_1 V_1} \tag{10}$$

We can substitute in values now.

$$T_2 = T_1 * \frac{p_2 V_2}{p_1 V_1} = 313.15 * \frac{1.06 \times 10^5 * 1500}{1.01 \times 10^5 * 1000}$$
 (11)

$$= 313.15 * \frac{1.06 * 1.5}{1.01} = \boxed{492.97 \text{K} \approx 220^{\circ} \text{C}}$$
 (12)

The best laboratory vacuum has a pressure of about  $1.00 \times 10^{-18}$ atm, or  $1.01 \times 10^{-13}$ Pa. How many gas molecules are there per cubic centimeter in such a vacuum at 293 K?

#### 3.1 Solution

Use the ideal gas law, the version with Boltzmann's constant. We can solve for  $\frac{N}{V}$ .

$$pV = NkT \tag{13}$$

$$\frac{N}{V} = \frac{p}{kT} \tag{14}$$

From here, we can just plug and chug, so to speak.

$$\frac{N}{V} = \frac{1.01 \times 10^{-13} \text{N/m}^2}{1.38 \times 10^{-23} \text{N} \cdot \text{m/K} * 293 \text{K}} = \frac{1.01 \times 10^{10}}{404.34} \text{m}^{-3}$$
(15)

$$= 24978978.09 \times \text{m}^{-3} = 24.979 \text{cm}^{-3}$$
 (16)

Suppose 1.80 mol of an ideal gas is taken from a volume of  $3.00~\mathrm{m}^3$  to a volume of  $1.50~\mathrm{m}^3$  via an isothermal compression at  $30^{\circ}\mathrm{C}$ . (a) How much energy is transferred as heat during the compression, and (b) is the transfer to or from the gas?

#### 4.1 Solution (a)

Energy transferred can be thought of as work. We have a formula for work done by an ideal gas.

$$W = nRT \ln \left(\frac{V_f}{V_i}\right) \tag{17}$$

We can plug and chug into this.

$$T_K = T_C + 273.15 \text{K} = 30^{\circ} \text{C} + 273.15 \text{K} = 303.15 \text{K}$$
 (18)

$$W = (1.80 \text{mol})(8.31 \text{J/mol})(303.15 \text{K}) \ln \left(\frac{1.5 \text{m}^3}{3.0 \text{m}^3}\right)$$
(19)

$$= 4534.5177J * (-0.693147) = -3143.088J$$
 (20)

The energy transferred is the absolute value of this, which would be  $\boxed{3143.088J}$ .

### 4.2 Solution (b)

This is a volume compression process. The total energy in the system would remain constant, so Q = W by the first law of thermodynamics. This means Q < 0, so the energy is transferred from the gas as heat.

An automobile tire has a volume of  $1.64 \times 10^{-2} \mathrm{m}^3$  and contains air at a gauge pressure (pressure above atmospheric pressure) of 165 kPa when the temperature is  $0.00^{\circ}\mathrm{C}$ . What is the gauge pressure of the air in the tires when its temperature rises to  $27.0^{\circ}\mathrm{C}$  and its volume increases to  $1.67 \times 10^{-2}\mathrm{m}^3$ ? Assume atmospheric pressure is  $1.01 \times 10^{5}\mathrm{Pa}$ .

Air that initially occupies 0.140 m3 at a gauge pressure of 103.0 kPa is expanded isothermally to a pressure of 101.3 kPa and then cooled at constant pressure until it reaches its initial volume. Compute the work done by the air. (Gauge pressure is the difference between the actual pressure and atmospheric pressure.)

A sample of an ideal gas is taken through the cyclic process abca shown in Fig. 19-20. The scale of the vertical axis is set by pb=7.5 kPa and pac=2.5 kPa. At point a, T=200 K. (a) How many moles of gas are in the sample? What are (b) the tem- perature of the gas at point b, (c) the temperature of the gas at point c, and (d) the net energy added to the gas as heat during the cycle?

Container A in Fig. 19-22 holds an ideal gas at a pressure of  $5.0 \times 105 Pa$  and a temperature of 300 K. It is connected by a thin tube (and a closed valve) to container B, with four times the volume of A. Container B holds the same ideal gas at a pressure of  $1.0 \times 105 Pa$  and a temperature of 400 K. The valve is opened to allow the pressures to equalize, but the temperature of each container is maintained. What then is the pressure?

(a) Compute the rms speed of a nitrogen molecule at  $20.0^{\circ}$ C. The molar mass of nitrogen molecules ( $N_2$ ) is given in Table 19-1. At what temperatures will the rms speed be (b) half that value and (c) twice that value?

Determine the average value of the translational kinetic energy of the gas's molecules of an ideal gas at temperatures (a) 0.00°C and (b) 100°C. What is the translational kinetic energy per mole of an ideal gas at (c) 0.00°C and (d) 100°C?

In a certain particle accelerator, protons travel around a circular path of diameter 23.0 m in an evacuated chamber, whose residual gas is at 295 K and  $1.00 \times 10^{-6}$  torr pressure. (a) Calculate the number of gas molecules per cubic centimeter at this pressure. (b) What is the mean free path of the gas molecules if the molecu- lar diameter is  $2.00 \times 10^{-8}$ cm?

Ten particles are moving with the following speeds: four at 200m/s, two at 500m/s, and four at 600m/s. Calculate their (a) average and (b) rms speeds. (c) Is  $v_{rms} > v_{avg}$ ?

The temperature of 3.00 mol of an ideal diatomic gas is increased by 40.0 C° without the pressure of the gas changing. The molecules in the gas rotate but do not oscillate. (a) How much energy is transferred to the gas as heat? (b) What is the change in the internal energy of the gas? (c) How much work is done by the gas? (d) By how much does the rotational kinetic energy of the gas increase?

When 1.0 mol of oxygen  $(O_2)$  gas is heated at constant pressure starting at 0°C, how much energy must be added to the gas as heat to double its volume? The molecules rotate but do not oscillate.

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