

# Homework #16

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## Question 2

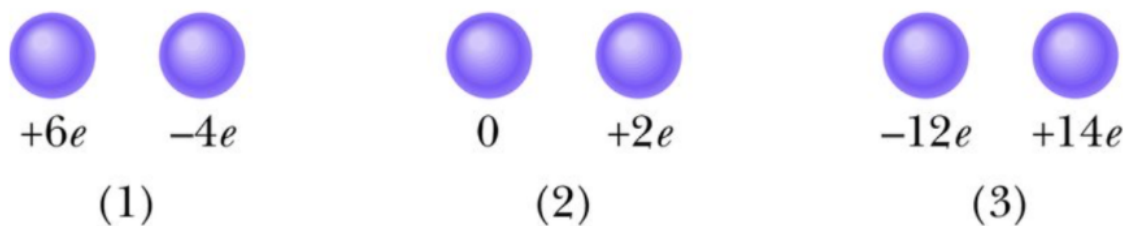


Figure 21-12 Question 2.

Figure 21-12 shows three pairs of identical spheres that are to be touched together and then separated. The initial charges on them are indicated. Rank the pairs according to (a) the magnitude of the charge transferred during touching and (b) the charge left on the positively charged sphere, greatest first.

### Solution

a)  $(3) > (1) > (2)$

In this problem, we just need to rank the differences between the charges on the balls. In instance 1, the difference is  $6 - (-4) = 10$ . In instance 2, the difference is  $2 - 0 = 2$ . In instance 3, the difference is  $14 - (-12) = 26$ . We can then rank the three, and the result is  $(3) > (1) > (2)$ .

b)  $(1) = (2) = (3)$  In this In this problem, we just need to rank the average charge of each of the two balls. In instance 1, the average is  $\frac{6+(-4)}{2} = 1$ . In instance 2, the difference is  $\frac{2+0}{2} = 1$ . In instance 3, the difference is  $\frac{14+(-12)}{2} = 1$ . We can then rank the three, and the result is  $(1) = (2) = (3)$ .

## Question 8

8 Figure 21-17 shows four arrangements of charged particles. Rank the arrangements according to the magnitude of the net electrostatic force on the particle with charge  $+Q$ , greatest first.

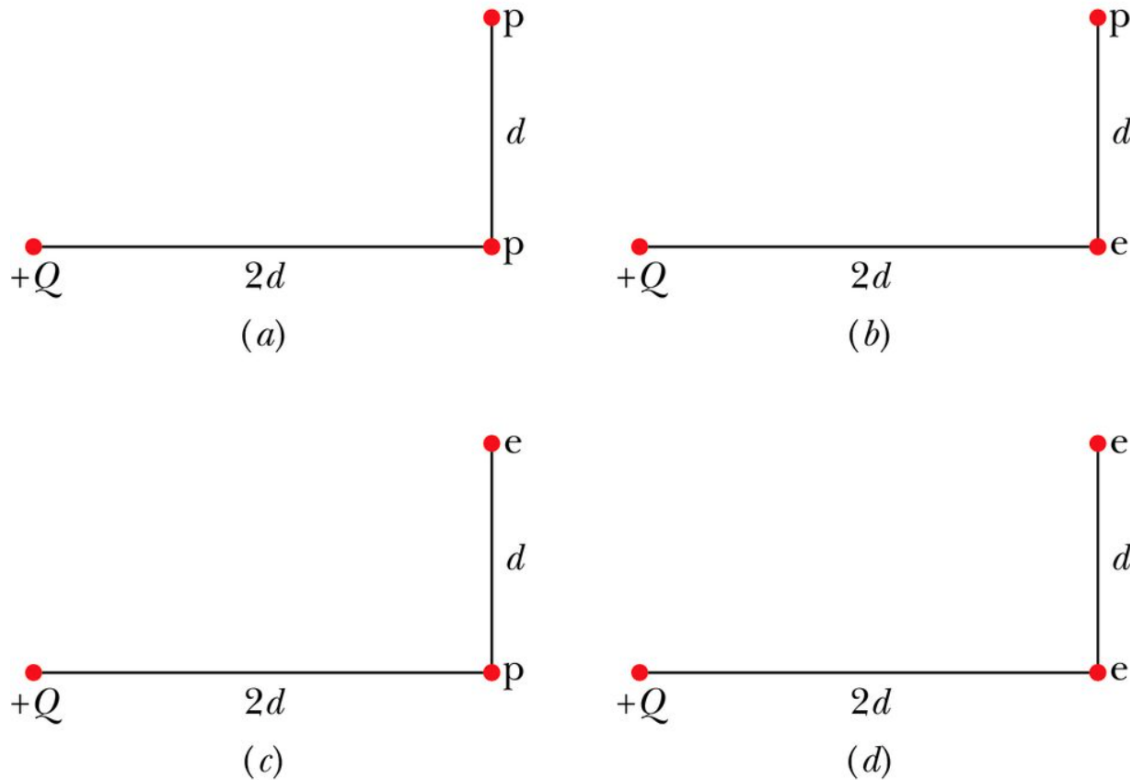


Figure 21-17 Question 8.

## Solution

0.0.1  $(a) = (d) > (b) = (c)$

For (a) and (d), the magnitude is always positive and the charge of a positron is the same as the charge of an electron, and the other particles are working together to move  $+Q$  more than separately. This means that they have the same magnitude.

For (b) and (c), the magnitude is always positive, but the two charged particles are exerting force on the  $+Q$  particle in relatively opposite directions. This means that the net force on the  $+Q$  particle is the same, but it is less than the net force on it in (a) or (d).

Hence,  $(a) = (d) > (b) = (c)$

## Question 10

**10** In Fig. 21-19, a central particle of charge  $-2q$  is surrounded by a square array of charged particles, separated by either distance  $d$  or  $d/2$  along the perimeter of the square. What are the magnitude and direction of the net electrostatic force on the central particle due to the other particles? (*Hint*: Consideration of symmetry can greatly reduce the amount of work required here.)

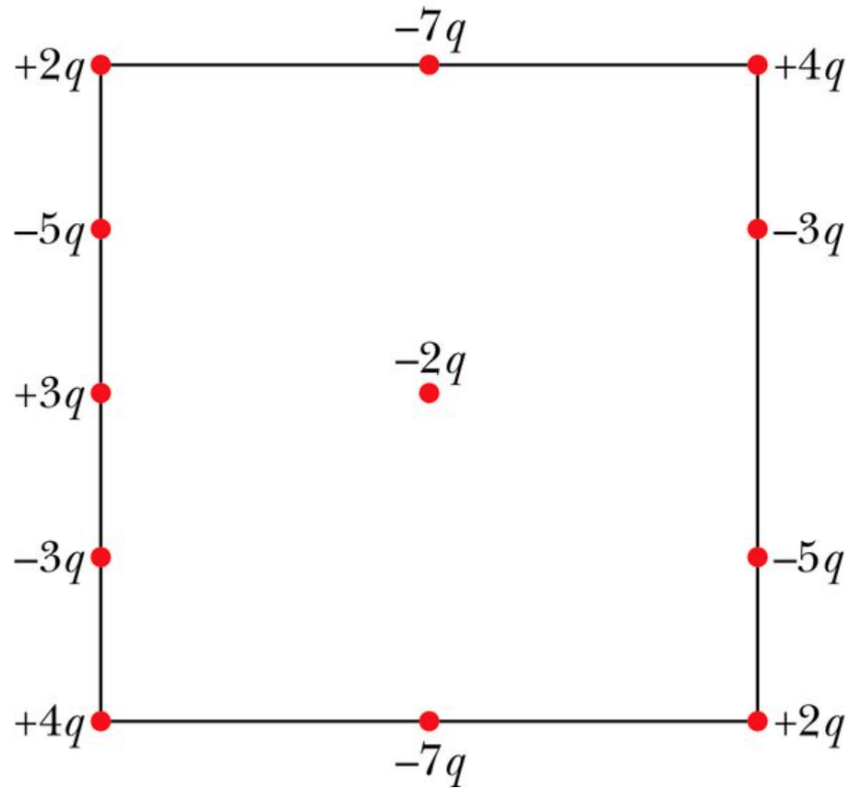
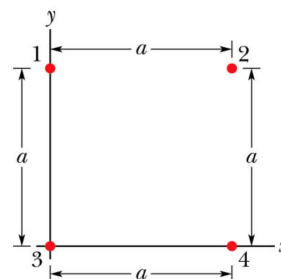


Figure 21-19 Question 10.

## Problem 10

In Fig. 21-25, four particles form a square. The charges are  $q_1 = q_4 = Q$  and  $q_2 = q_3 = q$ . (a) What is  $Q/q$  if the net electrostatic force on particles 1 and 4 is zero? (b) Is there any value of  $q$  that makes the net electrostatic force on each of the four particles zero? Explain.



## Solution

The distance between particles 1 and 4 is found by the pythagorean theorem.

$$r_{14} = r_{23} = \sqrt{a^2 + a^2} = a\sqrt{2}$$

### (a) Find $Q/q$

From this, we know that net electrostatic force on 1 from 4 in the direction of the line between 1 and 2 has to be equal to the force on 1 from 4. Roughly the same applies in the direction of the line between 1 and 3. As such, we can write a formula for the net force (which is 0).

$$\begin{aligned} F_{net} = 0 &= \frac{k |q_1| |q_2|}{r^2} - \frac{k |q_1| |q_4|}{r^2} * \cos(\theta) \\ \frac{k |q_1| |q_2|}{r^2} &= \frac{k |q_1| |q_4|}{r^2} * \cos(\theta) \\ \frac{|q_2|}{a^2} &= \frac{|q_4|}{2a^2} * \frac{\sqrt{2}}{2} \\ \frac{|q_4|}{|q_2|} &= \frac{4}{\sqrt{2}} = 2\sqrt{2} \end{aligned}$$

Since the forces must be in opposite directions, the charges must be opposite, so the ration has to be negative. This means that  $\boxed{Q/q = -2\sqrt{2}}$ .

### (b)

## Problem 11

In Fig. 21-25, the particles have charges  $q_1 = -q_2 = 100\text{nC}$  and  $q_3 = -q_4 = 200\text{nC}$ , and distance  $a = 5.0\text{cm}$ . What are the (a) x and (b) y components of the net electrostatic force on particle 3?

## Solution

## Problem 23

Fig. 21-32, particles 1 and 2 of charge  $q_1 = q_2 = +3.20 \times 10^{-19} \text{ C}$  are on a y axis at distance  $d = 17.0 \text{ cm}$  from the origin. Particle 3 of charge  $q_3 = +6.40 \times 10^{-19} \text{ C}$  is moved gradually along the x axis from  $x = 0$  to  $x = +5.0 \text{ m}$ . At what values of  $x$  will the magnitude of the electrostatic force on the third particle from the other two particles be (a) minimum and (b) maximum? What are the (c) minimum and (d) maximum magnitudes?

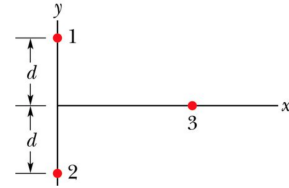


Figure 21-32 Problem 23.

## Problem 31

••31 ILW Earth's atmosphere is constantly bombarded by *cosmic ray protons* that originate somewhere in space. If the protons all passed through the atmosphere, each square meter of Earth's surface would intercept protons at the average rate of 1500 protons per second. What would be the electric current intercepted by the total surface area of the planet?



## Problem 36

•36 Electrons and positrons are produced by the nuclear transformations of protons and neutrons known as *beta decay*. (a) If a proton transforms into a neutron, is an electron or a positron produced? (b) If a neutron transforms into a proton, is an electron or a positron produced?