Homework #2, 4B

Donald Aingworth IV

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Chapter 21, Problem 52

52 A particle of charge Q is fixed at the origin of an xy coordinate system. At $t = 0$ a particle ($m = 0.800$ g, $q = 4.00$ μC) is located on the x axis at $x = 20.0$ cm, moving with a speed of 50.0 m/s in the positive y direction. For what value of Q will the moving particle execute circular motion? (Neglect the gravitational force on the particle.)

Chapter 21, Problem 66

66 An electron is in a vacuum near Earth's surface and located at $y = 0$ on a vertical y axis. At what value of y should a second electron be placed such that its electrostatic force on the first electron balances the gravitational force on the first electron?

Solution

In this instance, the downward gravitational force must be equal to the upwards electrostatic force, both of which we know the formulae for.

$$F_g = F_E$$
$$mg = \frac{kq_1 q_2}{r^2}$$

We can next solve for r, which would be the value of the height.

$$mg = \frac{kq_1 q_2}{r^2}$$
$$r^2 = \frac{kq^2}{mg}$$
$$r = \sqrt{\frac{kq^2}{mg}}$$

We can then plug values into this answer.

$$r = \sqrt{\frac{kq^2}{mg}} = \sqrt{\frac{(8.99 \times 10^9 \text{Nm}^2/\text{C}^2)(1.60218 \times 10^{-19}\text{C})^2}{(9.1093837 \times 10^{-31}\text{kg})(9.81\text{m/s}^2)}}$$
$$= \sqrt{25.823938\text{m}^2} = \pm 5.0817259\text{m}$$

The earth pulls the electron downwards. So=ince the electron has the same charge as the other electron, it pushes it away rather than pulling it towards itself. As such, in order to conteract the downwards force, the second electron needs to be put below the first electron. As such, it must be that y is negative, so $\boxed{y = -5.0817259\text{m}}$

Chapter 22, Question 4

4 Figure 22-25 shows four situations in which four charged particles are evenly spaced to the left and right of a central point. The charge values are indicated. Rank the situations according to the magnitude of the net electric field at the central point, greatest first.
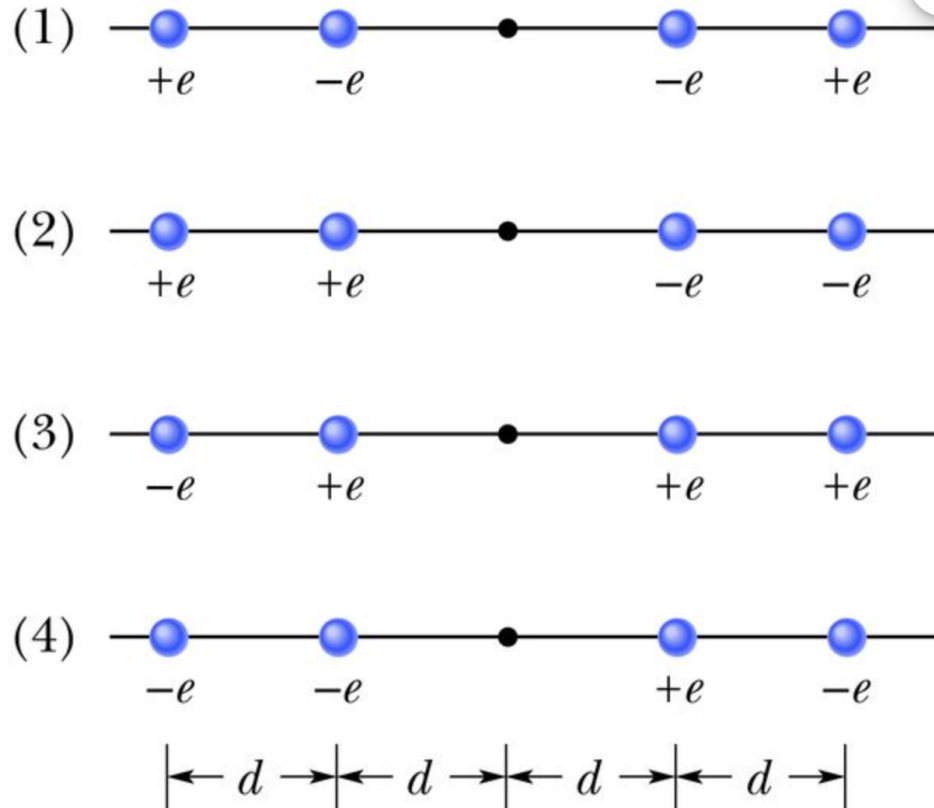
Solution

We will rank them by magnitude, which is always positive. I will rank the charges in terms of "agreeing" with the direction of the majority of electric fields and "disagreeing" with the majority of electric fields.

Number 1 has the same charges the same distances on each side, so the magnitude is zero. This means that it will be the least.

Number 2 has opposite charges on each side, so the magnitude is very big. $(2) > (1)$

Number 3 has three agreeing charges and one disagreeing charges. This means that its net electric field is greater than zero, but not as big as (2) where they all agree.

$(2) > (3) > (1)$

Number 4 has one disagreeing charge like number 3, but it is closer than number 3's field. This means that its field on the point has a greater impact on it because distance is inversely proportional to field strength. As such, the magnitude is less than the magnitude of (3). $\boxed{(2) > (3) > (4) > (1)}$

Chapter 22, Question 5

5 Figure 22-26 shows two charged particles fixed in place on an axis. (a) Where on the axis (other than at an infinite distance) is there a point at which their net electric field is zero: between the charges, to their left, or to their right? (b) Is there a point of zero net electric field anywhere *off* the axis (other than at an infinite distance)?
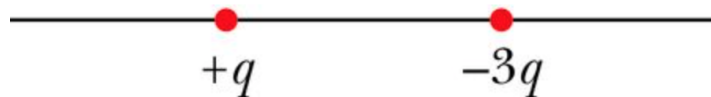

$+q$ $-3q$

Figure 22-26 Question 5.

Solution Part (a)

If the point charge is to the right, the closer charge being a greater charge will make the electric field always non-zero. In between the two charges, the $+q$ will push the electric field in the same direction as the $-3q$ charge will. To the left, the $-3q$ pushes it with an increasingly lower magnitude at a faster rate to which the $+q$ pushes it, so if there is a 0 point, it is to the left .

$$E_1 = -E_2 \frac{3kq}{r^2} = \frac{kq}{(r-1)^2} 3r^2 - 6r + 3 = r^2 2r^2 - 6r + 3 = 0r = \frac{3 \pm \sqrt{3}}{2}$$

This means that it would be $\frac{3\pm\sqrt{3}}{2}$ times the distance between the particles to the left of the $-3q$ particle.

Solution Part (b)

Yes, anywhere the distances cancel each other out where the above equation works when using the vector notation.

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Chapter 22, Problem 8

••8 **GO** In Fig. 22-36, the four particles are fixed in place and have charges $q_1 = q_2 = +5e$, $q_3 = +3e$, and $q_4 = -12e$. Distance $d = 5.0~\mu$m. What is the magnitude of the net electric field at point P due to the particles?
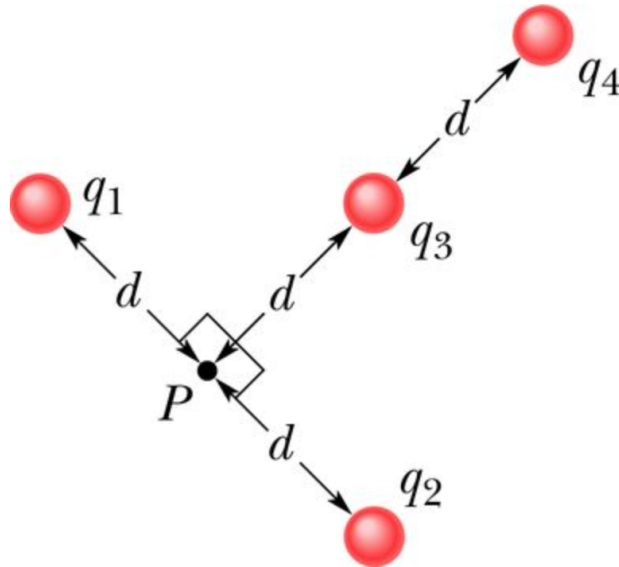

Figure 22-36 Problem 8.

Solution

First thing's first, since they're of equal charge and equaal but opposite distance on the same axis going through the point, the particles q_1 and q_2 cancel each other out, so we only need to consider particles q_3 and q_4.

$$\vec{E}_P = k \left(\frac{3e}{(5 \times 10^{-6})^2} - \frac{12e}{(2 * 5 \times 10^{-6})^2} \right)$$
$$= k \left(\frac{3e}{(5 \times 10^{-6})^2} - \frac{3e}{(5 \times 10^{-6})^2} \right)$$
$$= \frac{k * 3e}{(5 \times 10^{-6})^2} (1 - 1)$$
$$= \boxed{0\text{N/C}}$$

I suppose that the other two particles cancel each other out as well. I will be honest, that was pretty anticlimactic.

7

Chapter 22, Problem 12

••12 [GO] Figure 22-39 shows an uneven arrangement of electrons (e) and protons (p) on a circular arc of radius r = 2.00 cm, with angles θ_1 = 30.0°, θ_2 = 50.0°, θ_3 = 30.0°, and θ_4 = 20.0°. What are the (a) magnitude and (b) direction (relative to the positive direction of the x axis) of the net electric field produced at the center of the arc?
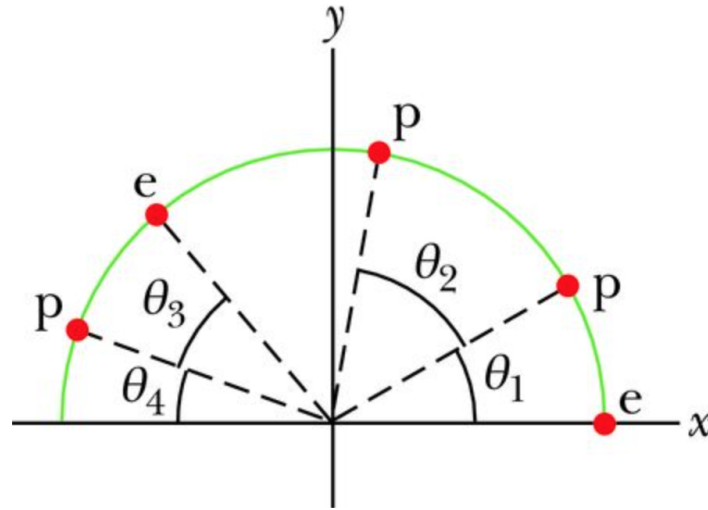

Figure 22-39 Problem 12.

Solution

We have the superposition principle and six charges, which I will number in reverst clockwise order. I will be using vector notation. We will keep the charge of a proton as $e = 1.60217663 \times 10^{-19}$C and the charge of an electron as $-e = -1.60217663 \times 10^{-19}$C.

$$\vec{E}_{net} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3 + \vec{E}_4 + \vec{E}_5 + \vec{E}_6 = \frac{k}{r^2} \sum_{i=1}^{6} -q_i \hat{r}_i$$

$$= \frac{k}{2^2} \left(-\frac{-e}{2} \begin{pmatrix} \cos(0°) \\ \sin(0°) \end{pmatrix} - \frac{e}{2} \begin{pmatrix} \cos(30°) \\ \sin(30°) \end{pmatrix} - \frac{e}{2} \begin{pmatrix} \cos(50°) \\ \sin(50°) \end{pmatrix} \right.$$

$$\left. -\frac{-e}{2} \begin{pmatrix} \cos(150°) \\ \sin(150°) \end{pmatrix} - \frac{e}{2} \begin{pmatrix} \cos(160°) \\ \sin(160°) \end{pmatrix} \right)$$

$$\vec{E}_{net} = \frac{ke}{2^3} \left(\begin{pmatrix} \cos(0°) \\ \sin(0°) \end{pmatrix} - \begin{pmatrix} \cos(30°) \\ \sin(30°) \end{pmatrix} - \begin{pmatrix} \cos(50°) \\ \sin(50°) \end{pmatrix} + \begin{pmatrix} \cos(150°) \\ \sin(150°) \end{pmatrix} - \begin{pmatrix} \cos(160°) \\ \sin(160°) \end{pmatrix} \right)$$

$$= \frac{ke}{2^3} \begin{pmatrix} 1 - \frac{\sqrt{3}}{2} - 0.6427876 - \frac{\sqrt{3}}{2} + 0.9396926 \\ 0 - \frac{1}{2} - 0.7660444 + \frac{1}{2} - 0.3420201 \end{pmatrix} = \frac{ke}{2^3} \begin{pmatrix} -0.4351458 \\ -1.1080646 \end{pmatrix}$$

$$= \frac{(8.99 \times 10^9)(1.60217663 \times 10^{-19})}{8} \begin{pmatrix} -0.4351458 \\ -1.1080646 \end{pmatrix}$$

$$= \begin{pmatrix} -7.834565 \times 10^{-11} \\ -1.9950104 \times 10^{-10} \end{pmatrix} \text{N/C}$$

(a) Magnitude

For the magnitude, we use the Pythagorean theorem.

$$\sqrt{(-7.834565 \times 10^{-11}) + (-1.9950104 \times 10^{-10})} = \boxed{2.1433 \times 10^{-10} \text{N/C}}$$

(b) Direction

For the direction, we use an arctangent, keeping in mind that the vector would be in the third quadrant.

$$\theta = \arctan\left(\frac{-1.9950104 \times 10^{-10}}{(-7.834565 \times 10^{-11})} \right) = 68.5597° = \boxed{248.5597°}$$

Chapter 22, Problem 46

•**46** An electron is accelerated eastward at 1.80×10^9 m/s^2 by an electric field. Determine the field (a) magnitude and (b) direction.

Solution

The formula we have from Newton's second law is $\vec{F}_{net} = m\vec{a}$. We already have the acceleration, that being 1.80×10^9m/s^2 eastward. We can also apply the mass of the electron ($9.1093837 \times 10^{-31}$kg), also keeping in mind the charge of an electron ($-1.60217663 \times 10^{-19}$C). We can also keep in mind that $\vec{F}_{net} = q\vec{E}_{net}$

$$\vec{F}_{net} = m\vec{a} = q\vec{E}_{net}$$
$$\vec{E}_{net} = \frac{m\vec{a}}{q} = \frac{(9.1093837 \times 10^{-31}\text{kg}) * (1.80 \times 10^9\text{m/s}^2)}{-1.60217663 \times 10^{-19}\text{C}}$$
$$= -1.02341342103 \times 10^{-2}\text{N/C}$$

a) Since we are looking for the magnitude, we take the absolute value, which is (approximately) $\boxed{1.0234 \times 10^{-2}\text{N/C}}$.

b) Since the original charge was going eastward and the electric field is in the opposite direction, the direction is $\boxed{\text{westward}}$.