

*. (8 points) 10 g of ice at 0°C is placed into a 35 g aluminum cup filled with 50 g of water, both initially at 30°C. The mixture is thermally isolated from its environment and allowed to come to equilibrium.

a. (4 points) What is the final temperature of the mixture?

$$\begin{aligned}
 C_w &= 1.00 \text{ cal/g·K} & C_{ice} &= \frac{C_w m_{ice}}{m_{ice}} \\
 C_{Al} &= 0.215 \text{ cal/g·K} & & = 10 \text{ cal/K} \\
 L_{w, fes} &= 79.5 \text{ cal/g} & & (\text{after melting}) \\
 \\
 C_{w+cup} &= \frac{C_w m_w + C_{Al} m_{Al}}{m_w + m_{Al}} & \text{heat out} &= \text{heat in} \\
 &= \frac{50 \text{ cal/K}}{7.525 \text{ cal/K}} & C_{w+cup} (T_{w+cup} - T_f) &= C_{ice} (T_f - T_{ice}) + L_{w, fes} \\
 &= 57.525 \text{ cal/K} & 57.525 (30 - T_f) &= 10 (T_f - 0) + 795 \\
 & & 1725.75 - 57.525 T_f &= (10 + 57.525) T_f \\
 & & \Rightarrow T_f &= \frac{1725.75}{67.525} \text{ cal} (40^\circ\text{C}) = 13.78^\circ\text{C}
 \end{aligned}$$

b. (4 points) How much ice (at 0°C) should be added to bring the final temperature of the mixture down to 0°C?

$$\begin{aligned}
 T_f &= 0^\circ\text{C} & m_{ice} &=? \\
 \text{heat out} &= \text{heat in} \\
 57.525 \frac{(30 - 0)}{\text{cal/K}} &= (79.5 \text{ cal/g}) m_{ice} \\
 &\quad \text{heat available from w+cup to melt ice} \\
 \Rightarrow m_{ice} &= \frac{1725.75 \text{ cal}}{79.5 \text{ cal/g}} \\
 &= 21.719
 \end{aligned}$$

An additional 11.719 must be added.
of ice

Note: any additional ice beyond the 21.719 total will remain as
ice after the mixture reaches 0°C.