

1 Problem 1

Find the mass in kilograms of 7.50×10^{24} atoms of arsenic, which has a molar mass of 74.9g/mol.

1.1 Solution

Convert atoms to moles.

$$\frac{7.50 \times 10^{24} \text{ atoms}}{6.02 \times 10^{23} \text{ atoms/mol}} = 12.458 \text{ mol} \quad (1)$$

Using the molar mass, convert moles to grams.

$$12.458 \text{ mol} * 74.9 \text{ g/mol} = 933.140 \text{ g} = \boxed{0.933 \text{ kg}} \quad (2)$$

2 Problem 3

Oxygen gas having a volume of 1000cm^3 at 40.0°C and $1.01 \times 10^5\text{Pa}$ expands until its volume is 1500cm^3 and its pressure is $1.06 \times 10^5\text{Pa}$. Find (a) the number of moles of oxygen present and (b) the final temperature of the sample.

2.1 Solution (a)

We can use the ideal gas law for this. We apply it to the first case, converting the 40.0°C to Kelvin.

$$40^\circ\text{C} = 313.15\text{K} \quad (3)$$

$$1000\text{cm}^3 = 1000 \times 10^{-6}\text{m}^3 = 1 \times 10^{-3}\text{m}^3 \quad (4)$$

$$pV = nRT \quad (5)$$

$$n = \frac{pV}{RT} = \frac{1.01 \times 10^5\text{Pa} * 10^{-3}\text{cm}^3}{8.31\text{J/mol} \cdot \text{K} * 313.15\text{K}} \quad (6)$$

$$= \frac{1.01 \times 10^2\text{N} \cdot \text{m}}{2602.2765\text{J/mol}} = \boxed{0.038812\text{mol}} \quad (7)$$

2.2 Solution (b)

The ideal gas law (or an equivalent) will be used here. The number of moles does not change here, neither does the gas constant R . We can use this to solve for the final value of the temperature.

$$\frac{p_1 V_1}{n_1 T_1} = \frac{p_2 V_2}{n_2 T_2} \quad (8)$$

$$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2} \quad (9)$$

$$T_2 = T_1 * \frac{p_2 V_2}{p_1 V_1} \quad (10)$$

We can substitute in values now.

$$T_2 = T_1 * \frac{p_2 V_2}{p_1 V_1} = 313.15 * \frac{1.06 \times 10^5 * 1500}{1.01 \times 10^5 * 1000} \quad (11)$$

$$= 313.15 * \frac{1.06 * 1.5}{1.01} = \boxed{492.97\text{K} \approx 220^\circ\text{C}} \quad (12)$$

3 Problem 5

The best laboratory vacuum has a pressure of about 1.00×10^{-18} atm, or 1.01×10^{-13} Pa. How many gas molecules are there per cubic centimeter in such a vacuum at 293 K?

3.1 Solution

Use the ideal gas law, the version with Boltzmann's constant. We can solve for $\frac{N}{V}$.

$$pV = NkT \quad (13)$$

$$\frac{N}{V} = \frac{p}{kT} \quad (14)$$

From here, we can just plug and chug, so to speak.

$$\frac{N}{V} = \frac{1.01 \times 10^{-13} \text{ N/m}^2}{1.38 \times 10^{-23} \text{ N} \cdot \text{m/K} * 293 \text{ K}} = \frac{1.01 \times 10^{10}}{404.34} \text{ m}^{-3} \quad (15)$$

$$= 24978978.09 \times \text{m}^{-3} = \boxed{24.979 \text{ cm}^{-3}} \quad (16)$$

4 Problem 7

Suppose 1.80 mol of an ideal gas is taken from a volume of 3.00 m³ to a volume of 1.50 m³ via an isothermal compression at 30°C. (a) How much energy is transferred as heat during the compression, and (b) is the transfer to or from the gas?

4.1 Solution (a)

Energy transfered can be thought of as work. We have a formula for work done by an ideal gas.

$$W = nRT \ln \left(\frac{V_f}{V_i} \right) \quad (17)$$

We can plug and chug into this.

$$T_K = T_C + 273.15\text{K} = 30^\circ\text{C} + 273.15\text{K} = 303.15\text{K} \quad (18)$$

$$W = (1.80\text{mol})(8.31\text{J/mol})(303.15\text{K}) \ln \left(\frac{1.5\text{m}^3}{3.0\text{m}^3} \right) \quad (19)$$

$$= 4534.5177\text{J} * (-0.693147) = -3143.088\text{J} \quad (20)$$

The energy transfered is the absolute value of this, which would be 3143.088J.

4.2 Solution (b)

This is a volume compression process. The total energy in the system would remain constant, so $Q = W$ by the first law of thermodynamics. This means $Q < 0$, so the energy is transfered from the gas as heat.

5 Problem 9

An automobile tire has a volume of $1.64 \times 10^{-2}\text{m}^3$ and contains air at a gauge pressure (pressure above atmospheric pressure) of 165 kPa when the temperature is 0.00°C . What is the gauge pressure of the air in the tires when its temperature rises to 27.0°C and its volume increases to $1.67 \times 10^{-2}\text{m}^3$? Assume atmospheric pressure is $1.01 \times 10^5\text{Pa}$.

5.1 Solution

We can here use the ideal gas law.

$$pV = nRT \quad (21)$$

$$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2} \quad (22)$$

With our equation, we solve for p_f .

$$p_f = p_i \frac{V_i T_f}{V_f T_i} \quad (23)$$

This can be “plugged-and-chugged” to find our final answer. We should also bear in mind that the gauge pressure should be added to the atmospheric pressure to find the overall pressure. Do not forget to convert to Kelvin.

$$T_{iK} = 0^\circ\text{C} + 273\text{K} = 273\text{K} \quad (24)$$

$$T_{fK} = 27^\circ\text{C} + 273\text{K} = 300\text{K} \quad (25)$$

$$p_i = p_{\text{gauge}} + p_{\text{atm}} = 165 \times 10^3\text{Pa} + 1.01 \times 10^5\text{Pa} = 266 \times 10^3\text{Pa} \quad (26)$$

$$p_f = p_i \frac{V_i T_f}{V_f T_i} = 266 \times 10^3\text{Pa} * \frac{(1.64 \times 10^{-2}\text{m}^3)(300\text{K})}{(1.67 \times 10^{-2}\text{m}^3)(273\text{K})} \quad (27)$$

$$= 266 \times 10^3\text{Pa} * \frac{492}{455.91} = 287 \times 10^3\text{Pa} \quad (28)$$

This can in turn be turned into the gauge pressure (our final answer) by subtracting the atmospheric pressure.

$$p_{\text{gauge};f} = 287 \times 10^3\text{Pa} - 1.01 \times 10^5\text{Pa} = \boxed{1.86 \times 10^5\text{Pa}} \quad (29)$$

6 Problem 11

Air that initially occupies 0.140m^3 at a gauge pressure of 103.0kPa is expanded isothermally to a pressure of 101.3kPa and then cooled at constant pressure until it reaches its initial volume. Compute the work done by the air. Gauge pressure is the difference between the actual pressure and atmospheric pressure.

6.1 Solution

Isothermal expansion means that there is no net change in energy, so $Q_{in} = W_{out}$ (a.k.a. $Q_{in} = -W_{in}$) as volume increases. There is a formula for work we can use.

$$W = \int_{V_i}^{V_f} p(V) dV \quad (30)$$

The problem outright states that it is separated into two parts: the isothermal expansion at changing pressure and the cooling at constant pressure. We can separate our equation into these two parts and find useful equations for each. The integrals will be separated at a point of $V = V_{max}$ since that is the point where the volume reaches its highest. We can call the final pressure value of 101.3kPa the value p_r , with no meaning to its name.

$$W = \int_{V_i}^{V_f} p(V) dV = \int_{V_i}^{V_{max}} p_1(V) dV + \int_{V_{max}}^{V_f} p_2(V) dV \quad (31)$$

$$= \int_{V_i}^{V_{max}} \frac{nRT_i}{V} dV + \int_{V_{max}}^{V_f} p_r dV \quad (32)$$

$$= nRT_i \ln\left(\frac{V_{max}}{V_i}\right) + \int_{V_{max}}^{V_f} p_r dV \quad (33)$$

$$= p_i V_i \ln\left(\frac{V_{max}}{V_i}\right) + p_r (V_f - V_{max}) \quad (34)$$

This requires the initial and maximum magnitudes of the volume, of which we only have one. We can use the ideal gas law to find that which we need. First solve for the final volume, given n , R , and T are constant. Do not forget to convert gauge pressure to overall pressure by adding the atmospheric pressure ($1.01 \times 10^5\text{Pa}$). We can assume that the final pressure

is not gauge pressure.

$$p_i = p_1 + p_{atm} = 103.0 \times 10^3 + 1.01 \times 10^5 \text{Pa} = 2.04 \times 10^5 \text{Pa} \quad (35)$$

$$p_f = p_2 = 101.3 \times 10^3 \text{Pa} \quad (36)$$

$$pV = nRT \quad (37)$$

$$p_i V_i = p_f V_f = p_f V_{max} \quad (38)$$

$$V_{max} = V_i * \frac{p_i}{p_f} = 0.140 \text{m}^3 * \frac{2.04 \times 10^5 \text{Pa}}{1.013 \times 10^5 \text{Pa}} = 0.281935 \text{m}^3 \quad (39)$$

This can in turn be applied to our above equation for the work done by the gas.

$$W = p_i V_i \ln \left(\frac{V_{max}}{V_i} \right) + \int_{V_{max}}^{V_f} p_r dV \quad (40)$$

$$= 0.140 \text{m}^3 * 2.04 \times 10^5 \text{Pa} * \ln \left(\frac{0.281935 \text{m}^3}{0.140 \text{m}^3} \right) + \int_{0.281935 \text{m}^3}^{0.140 \text{m}^3} 1.013 \times 10^5 \text{Pa} dV \quad (41)$$

$$= 28560 * 0.7000 + 101300 * (-0.1419) = 19992.96 \text{J} - 14378 \text{J} \quad (42)$$

$$= \boxed{5614.95 \text{J}} \quad (43)$$

7 Problem 13

A sample of an ideal gas is taken through the cyclic process $abca$ shown in Fig. 19-20. The scale of the vertical axis is set by $p_b = 7.5 \text{ kPa}$ and $p_{ac} = 2.5 \text{ kPa}$. At point a , $T = 200 \text{ K}$. (a) How many moles of gas are in the sample? What are (b) the temperature of the gas at point b , (c) the temperature of the gas at point c , and (d) the net energy added to the gas as heat during the cycle?

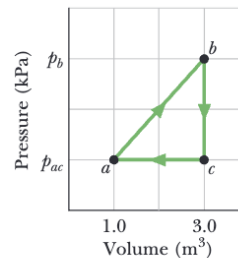


Figure 19-20 Problem 13.

7.1 Solution (a)

We can use the ideal gas law. We need to solve for n at point a .

$$pV = nRT \rightarrow n = \frac{pV}{RT} \quad (44)$$

From here, we plug in values to find n .

$$n = \frac{(2.5 \text{ kPa}) * (1.0 \text{ m}^3)}{R(200 \text{ K})} = \frac{2.5 \times 10^3 \text{ J}}{1662 \text{ J/mol}} = \boxed{1.504 \text{ mol}} \quad (45)$$

7.2 Solution (b)

We can use the ideal gas law again, this time comparing two situations and finding the final temperature.

$$\frac{p_i V_i}{T_i} = \frac{p_f V_f}{T_f} \rightarrow T_f = T_i * \frac{p_f V_f}{p_i V_i} \quad (46)$$

From here, we plug in values to find the final temperature.

$$T_f = T_i * \frac{p_f V_f}{p_i V_i} = 200 \text{ K} * \frac{7.5 \text{ kPa} * 3.0 \text{ m}^3}{2.5 \text{ kPa} * 1.0 \text{ m}^3} \quad (47)$$

$$= 200 \text{ K} * 9 = \boxed{1800 \text{ K}} \quad (48)$$

7.3 Solution (c)

Use the ideal gas law again. This time, the pressure does not change.

$$\frac{V_i}{T_i} = \frac{V_f}{T_f} \rightarrow T_f = T_i * \frac{V_f}{V_i} \quad (49)$$

Now, we plug in to find T_f .

$$T_f = T_i * \frac{V_f}{V_i} = 1800 \text{ K} * \frac{1.0 \text{ m}^3}{3.0 \text{ m}^3} = \boxed{600 \text{ K}} \quad (50)$$

7.4 Solution (d)

Let's start by calculating the total work done by the gas. We can separate it based on the phases. The phase between points b and c has no change in volume, so no work is done.

$$W = \int p(V) dV \quad (51)$$

$$= \int_{1.0\text{m}^3}^{3.0\text{m}^3} V * 2500 \text{ Pa/m}^3 dV + \int_{3.0\text{m}^3}^{3.0\text{m}^3} p_{bc} dV + \int_{3.0\text{m}^3}^{1.0\text{m}^3} 2500 \text{ Pa} dV \quad (52)$$

$$= (1250 \text{ Pa/m}^3) \left(\frac{(3.0\text{m}^3)^2 - (1.0\text{m}^3)^2}{2} \right) + 2500 \text{ Pa} * (-2.0\text{m}^3) \quad (53)$$

$$= 4 * 2500 \text{ J} - 2 * 2500 \text{ J} = 10000 - 5000 \text{ J} = 5000 \text{ J} \quad (54)$$

Since this is a cyclical process, we can apply the first law of thermodynamics.

$$\Delta E_{\text{int}} = 0 = Q_{\text{in}} - W_{\text{out}} \quad (55)$$

$$Q_{\text{in}} = W_{\text{out}} = \boxed{5000 \text{ J}} \quad (56)$$

8 Problem 17

Container A in Fig. 19-22 holds an ideal gas at a pressure of $5.0 \times 10^5 \text{ Pa}$ and a temperature of 300 K . It is connected by a thin tube (and a closed valve) to container B, with four times the volume of A. Container B holds the same ideal gas at a pressure of $1.0 \times 10^5 \text{ Pa}$ and a temperature of 400 K . The valve is opened to allow the pressures to equalize, but the temperature of each container is maintained. What then is the pressure?

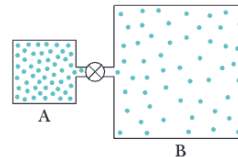


Figure 19-22 Problem 17.

8.1 Solution

Let's put together a formulas for the number of moles of the ideal gas in each container (A and B). We can use the Ideal Gas Law for this.

$$n_A = \frac{p_A V_A}{RT_A} = \frac{5.0 \times 10^5 \text{ Pa} * V_A}{R * 300 \text{ K}} = \frac{5 \times 10^3}{3} * \frac{V_A}{R} \quad (57)$$

$$n_B = \frac{p_B V_B}{RT_B} = \frac{1.0 \times 10^5 \text{ Pa} * 4V_A}{R * 400 \text{ K}} = 1 \times 10^3 * \frac{V_A}{R} \quad (58)$$

We can combine these to find the total number of moles.

$$n_{\Sigma} = n_A + n_B = \left(\frac{5}{3} + 1 \right) \times 10^3 * \frac{V_A}{R} = \frac{8}{3} \times 10^3 * \frac{V_A}{R} \quad (59)$$

We also know the total volume that there is.

$$V_{\Sigma} = \sum V_i = V_A + V_B = V_A + 4V_A = 5V_A \quad (60)$$

We can also calculate the average temperature of the cobined system, weighted by the volumes.

$$T_{\text{avg}} = \frac{\sum V_i * T_i}{\sum V_i} = \frac{V_A * T_A + V_B * T_B}{5V_A} \quad (61)$$

$$= \frac{V_A * 300 \text{ K} + 4V_A * 400 \text{ K}}{5V_A} \quad (62)$$

$$= \frac{300 \text{ K} + 1600 \text{ K}}{5} = \frac{1900 \text{ K}}{5} = 380 \text{ K} \quad (63)$$

We have our final values for the number of moles, volume, and temperature, not to mention that R is a constant. We can put these into the ideal gas law to find the pressure at this point, assuming the pressure to be even.

$$pV = nRT \quad (64)$$

$$p = \frac{nRT}{V} = \frac{\frac{8}{3} \times 10^3 * \frac{V_A}{R} * R * 380 \text{ K}}{5V_A} \quad (65)$$

$$= \left(\frac{8}{15} \times 10^3 * 380 \right) \text{ Pa} = \boxed{2.03 \times 10^5 \text{ Pa}} \quad (66)$$

9 Problem 19

(a) Compute the rms speed of a nitrogen molecule at 20.0°C. The molar mass of nitrogen molecules (N_2) is given in Table 19-1. At what temperatures will the rms speed be (b) half that value and (c) twice that value?

9.1 Solution (a)

As stated in table 19-1, the molar mass of Nitrogen gas (N_2) molecules is $28.0 \times 10^{-3} \text{ kg/mol}$. We can use that to find the molecule's rms (root-mean-square) speed.

$$T_K = T_{\text{°C}} + 273\text{K} = 293\text{K} \quad (67)$$

$$v_{\text{rms}} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * 293 \text{ K}}{28.0 \times 10^{-3} \text{ kg/mol}}} \quad (68)$$

$$= \sqrt{\frac{7304.49}{28.0}} \times 10^3 \text{ m}^2/\text{s}^2 = \boxed{510.8 \text{ m/s}} \quad (69)$$

9.2 Solution (b)

We can use the same equation, this time solving for the temperature.

$$\frac{v_{\text{rms}}}{2} = \sqrt{\frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * T}{28.0 \times 10^{-3} \text{ kg/mol}}} \quad (70)$$

$$\frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * 293 \text{ K}}{28.0 \times 10^{-3} \text{ kg/mol}} * \frac{1}{4} = \frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * T}{28.0 \times 10^{-3} \text{ kg/mol}} \quad (71)$$

$$T = \frac{293 \text{ K}}{4} = 73.25 \text{ K} = \boxed{-199.75 \text{ °C}} \quad (72)$$

9.3 Solution (c)

The same equation can be used.

$$2v_{\text{rms}} = \sqrt{\frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * T}{28.0 \times 10^{-3} \text{ kg/mol}}} \quad (73)$$

$$\frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * 293 \text{ K}}{28.0 \times 10^{-3} \text{ kg/mol}} * 4 = \frac{3 * 8.31 \text{ J/mol} \cdot \text{K} * T}{28.0 \times 10^{-3} \text{ kg/mol}} \quad (74)$$

$$T = 4 * 293 \text{ K} = 1172 \text{ K} = \boxed{899^\circ\text{C}} \quad (75)$$

10 Problem 23

A beam of hydrogen molecules (H_2) is directed toward a wall, at an angle of 55° with the normal to the wall. Each molecule in the beam has a speed of 1.0 km/s and a mass of $3.3 \times 10^{-24}\text{ g}$. The beam strikes the wall over an area of 2.0 cm^2 , at the rate of 10^{23} molecules per second. What is the beam's pressure on the wall?

10.1 Solution

This solution may be difficult to understand because p represents both pressure and momentum. We need more letters. Maybe we could look at some language with a lot of different letters/characters. My Chinese teacher says their language has about 1500. We have a formula for pressure exerted by an ideal gas.

$$p = \frac{nMv_{\text{rms}}^2}{3V} = \frac{F}{A} \quad (76)$$

We assume that any collision of a molecule with a wall is fully elastic, so we can find a formula for the change in the vertical momentum. This would only be for a single particle and we will only be considering the horizontal velocity.

$$v_i = v_{\text{rms}} * \sin(55^\circ) \quad (77)$$

$$v_f = -v_i \quad (78)$$

$$\Delta p = p_f - p_i = mv_f - mv_i \quad (79)$$

$$= 2mv_f = -2m * v_{\text{rms}} * \cos(55^\circ) \quad (80)$$

This can be multiplied by the rate at which the molecules hit the wall to find the total force, which is itself constant.

$$F = p * \frac{dN}{dt} = -2m * v_{\text{rms}} * \cos(55^\circ) * 10^{23} \text{ s}^{-1} \quad (81)$$

We can apply this to our equation for the pressure. That would be the final equation that we can plug values into.

$$p = \frac{F}{A} = -\frac{2m * v_{\text{rms}} * \cos(55^\circ) * 10^{23} \text{ s}^{-1}}{A} \quad (82)$$

$$= -\frac{2 * 3.3 \times 10^{-27} \text{ kg} * 1000 \text{ m/s} * \cos(55^\circ) * 10^{23} \text{ s}^{-1}}{2.0 \times 10^{-4} \text{ m}^2} \quad (83)$$

$$= -1893 \text{ Pa} \quad (84)$$

Since pressure is always positive, we can finalize this by taking the absolute value to get our final answer. Said answer would be $\boxed{1893 \text{ Pa}}$.

11 Problem 25

Determine the average value of the translational kinetic energy of the gas's molecules of an ideal gas at temperatures (a) 0.00°C and (b) 100°C. What is the translational kinetic energy per mole of an ideal gas at (c) 0.00°C and (d) 100°C?

11.1 Solution (a)

The average translational kinetic energy is determined by a simple formula, which we can use here.

$$K = \frac{3}{2}kT = \frac{3}{2} * 1.38 \times 10^{-23} \text{ J/K} * 273 \text{ K} = \boxed{565.11 \times 10^{-23} \text{ J}} \quad (85)$$

11.2 Solution (b)

Same strategy.

$$K = \frac{3}{2}kT = \frac{3}{2} * 1.38 \times 10^{-23} \text{ J/K} * 373 \text{ K} = \boxed{772.11 \times 10^{-23} \text{ J}} \quad (86)$$

11.3 Solution (c)

The kinetic energy of a system (in this case a mole of atoms) would be the sum of the kinetic energy of its parts. Each mole contains Avogadro's number (N_A) atoms, each with a kinetic energy of its own, and the average translational kinetic energy of each atom is defined by the formula $K = \frac{3}{2}kT$. To get the total kinetic energy in one mole of an ideal gas, we can multiply the kinetic energy in each molecule by the number of molecules in a mole.

$$K_{\text{per mole}} = \frac{3}{2}kT \times N_A \quad (87)$$

Since $k = \frac{R}{N_A}$, we also know that $R = k * N_A$, which we can use.

$$K_{\text{per mole}} = \frac{3}{2}RT = \frac{3}{2} * 8.31 \text{ J/mol} \cdot \text{K} * 273 \text{ K} \quad (88)$$

$$= 3402.945 \text{ J/mol} = \boxed{3403 \text{ J/mol}} \quad (89)$$

11.4 Solution (d)

Same strategy.

$$K_{\text{per mole}} = \frac{3}{2}RT = \frac{3}{2} * 8.31 \text{ J/mol} \cdot \text{K} * 373 \text{ K} \quad (90)$$

$$= 4649.445 \text{ J/mol} = \boxed{4649 \text{ J/mol}} \quad (91)$$

12 Problem 27

Water standing in the open at 32.0°C evaporates because of the escape of some of the surface molecules. The heat of vaporization (539 cal/g) is approximately equal to εn , where ε is the average energy of the escaping molecules and n is the number of molecules per gram. (a) Find ε . (b) What is the ratio of ε to the average kinetic energy of H₂O molecules, assuming the latter is related to temperature in the same way as it is for gases?

12.1 Solution (a)

We can assume that $\varepsilon n = 539 \text{ cal/g}$. The number of molecules per gram can be calculated by using the molar mass of the water vapor (MM = 18.0 × 10⁻³ kg/mol).

$$n = \frac{1}{\text{MM}} \times N_A = \frac{1 \text{ mol}}{18.0 \text{ g}} * 6.022 \times 10^{23} = 3.3456 \times 10^{22} \text{ g}^{-1} \quad (92)$$

Using this, we can find the value of ε .

$$\varepsilon n = 539 \text{ cal/g} \quad (93)$$

$$\varepsilon = \frac{539 \text{ cal/g}}{3.3456 \times 10^{22} \text{ g}^{-1}} = \boxed{1.611 \times 10^{-20} \text{ cal/molecule}} \quad (94)$$

12.2 Solution (b)

The average kinetic energy is calculatable by a formula.

$$K = \frac{3}{2} kT \quad (95)$$

This can be used in a ratio, bearing in mind that 32.0°C = 32.0°C + 273 K = 305 K.

$$\frac{\varepsilon}{K} = \frac{\varepsilon}{\frac{3}{2} kT} = \frac{1.611 \times 10^{-20} \text{ cal/molecule}}{\frac{3}{2} * 1.38 \times 10^{-23} \text{ J/K} * 305 \text{ K}} \quad (96)$$

$$= \frac{6.740 \times 10^{-20} \text{ J/molecule}}{\frac{3}{2} * 1.38 \times 10^{-23} \text{ J/K} * 305 \text{ K}} \quad (97)$$

$$= \boxed{10.67} \quad (98)$$

13 Problem 31

In a certain particle accelerator, protons travel around a circular path of diameter 23.0 m in an evacuated chamber, whose residual gas is at 295 K and 1.00×10^{-6} torr pressure. (a) Calculate the number of gas molecules per cubic centimeter at this pressure. (b) What is the mean free path of the gas molecules if the molecular diameter is 2.00×10^{-8} cm?

13.1 Solution (a)

The ideal gas law would be our friend, and we will assume this to be an ideal gas, where we seek to find the number of molecules per volume, better expressed as $\frac{N}{V}$. Also don't forget to convert pressure from torr to pascals.

$$p = 1.00 \times 10^{-6} \text{ torr} = 1.00 \times 10^{-6} \text{ mm Hg} \quad (99)$$

$$= 0.100 \times 10^{-6} \text{ cm Hg} = 133.30 \times 10^{-6} \text{ Pa} \quad (100)$$

$$pV = NkT \quad (101)$$

$$\frac{N}{V} = \frac{p}{kT} = \frac{133.30 \times 10^{-6} \text{ Pa}}{1.38 \times 10^{-23} \text{ J/K} * 295 \text{ K}} \quad (102)$$

$$= 3.274 \times 10^{16} \text{ molecule/m}^3 \times \frac{10 \times 10^{-6} \text{ m}^3}{1 \text{ cm}^3} \quad (103)$$

$$= \boxed{3.274 \times 10^{10} \text{ molecule/cm}^3} \quad (104)$$

13.2 Solution (b)

There's an equation for this. It's kind of ugly to be completely honest, but it's usable.

$$\lambda = \frac{1}{\sqrt{2}\pi d^2 N/V} = \frac{1}{\sqrt{2}\pi (2.00 \times 10^{-8} \text{ cm})^2 * 3.274 \times 10^{10} \text{ cm}^{-3}} \quad (105)$$

$$= 17187 \text{ cm} = \boxed{171.87 \text{ m}} \quad (106)$$

14 Problem 35

Ten particles are moving with the following speeds: four at 200m/s, two at 500m/s, and four at 600m/s. Calculate their (a) average and (b) rms speeds. (c) Is $v_{rms} > v_{avg}$?

14.1 Solution (a)

We'll just do a simple average.

$$v_{avg} = \frac{\sum_{i=1}^n v_i}{n} = \frac{4 * 200 + 2 * 500 + 4 * 600}{10} \quad (107)$$

$$= 4 * 20 + 2 * 50 + 4 * 60 \quad (108)$$

$$= 80 + 100 + 240 = \boxed{420\text{m/s}} \quad (109)$$

14.2 Solution (b)

14.2.1 Attempt 1 (Incorrect)

There's a formula for v_{rms} .

$$v_{rms} = \sqrt{\frac{3RT}{M}} \quad (110)$$

$$v_{rms}^2 = \frac{3RT}{M} \quad (111)$$

I don't know about you, but it reminds me of a formula for the average velocity.

$$v_{avg} = \sqrt{\frac{8RT}{\pi M}} \quad (112)$$

$$v_{avg}^2 = \frac{8RT}{\pi M} = \frac{8}{3\pi} \cdot \frac{3RT}{M} \quad (113)$$

$$\frac{3RT}{M} = \frac{3\pi}{8} v_{avg}^2 \quad (114)$$

We could use the transitive property on this.

$$v_{rms}^2 = \frac{3\pi}{8} v_{avg}^2 = \frac{3\pi}{8} * (420 \text{ m/s})^2 = 22050 * 3\pi = 66150\pi \text{ m}^2/\text{s}^2 \quad (115)$$

$$v_{rms} = \sqrt{66150\pi \text{ m}^2/\text{s}^2} = 455.9 \text{ m/s} \quad (116)$$

The error made here was assuming the gas to be an ideal gas, which is required for some of our equations.

14.2.2 Attempt 2

Just brute force it.

$$v_{\text{rms}}^2 = \frac{4 * 200^2 + 2 * 500^2 + 4 * 600^2}{10} \quad (117)$$

$$= \frac{4 * 40000 + 2 * 250000 + 4 * 360000}{10} \quad (118)$$

$$= \frac{160000 + 500000 + 1440000}{10} \quad (119)$$

$$= \frac{2100000 \text{ m}^2/\text{s}^2}{10} = 210000 \text{ m}^2/\text{s}^2 \quad (120)$$

$$v_{\text{rms}} = \boxed{458 \text{ m/s}} \quad (121)$$

14.3 Solution (c)

It's just by a difference of 38 m/s, but \boxed{yes} .

15 Problem 37

Figure 19-23 shows a hypothetical speed distribution for a sample of N gas particles (note that $P(v) = 0$ for speed $v > 2v_0$). What are the values of (a) av_0 , (b) v_{avg}/v_0 , and (c) v_{rms}/v_0 ? (d) What fraction of the particles has a speed between $1.5v_0$ and $2.0v_0$?

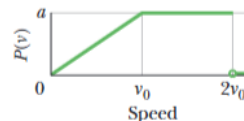


Figure 19-23 Problem 37.

15.1 Solution (a)

We know that the total area under the curve is equal to 1. The area of a right triangle (like $P(v)$ in the range of $[0, v_0]$) is $\frac{1}{2}wh$ (in this case $\frac{1}{2}av_0$), while the area of a rectangle (like $P(v)$ in the range of $[v_0, 2v_0]$) is wh (in this case av_0). The total area under the curve would be the two of these added together, which we know an alternative value of.

$$\frac{3}{2}av_0 = \int_0^\infty P(v) dv = 1 \quad (122)$$

Divide both sides by av_0 (which we assume not to be equal to zero, which it appears not to be) and solve for av_0 .

$$\frac{\frac{3}{2}av_0}{av_0} = \frac{3}{2} = \frac{1}{av_0} \quad (123)$$

$$\boxed{av_0 = \frac{2}{3}} \quad (124)$$

15.2 Solution (b)

There's a formula for this. It can be separated by sections.

$$v_{\text{avg}} = \int_0^\infty v P(v) dv = \int_0^{v_0} v^2 * \frac{a}{v_0} dv + \int_{v_0}^{2v_0} v * a dv + \int_{2v_0}^\infty v * 0 dv \quad (125)$$

$$= \left[\frac{v^3}{3} \cdot \frac{a}{v_0} \right]_0^{v_0} + \left[\frac{v^2}{2} \cdot a \right]_{v_0}^{2v_0} + [0]_{2v_0}^\infty \quad (126)$$

$$= \frac{av_0^2}{3} + \frac{3av_0^2}{2} = \frac{2v_0}{9} + v_0 = \frac{11}{9}v_0 \quad (127)$$

$$v_{\text{avg}}/v_0 = \frac{11}{9} = \boxed{1.22} \quad (128)$$

15.3 Solution (c)

There's a similar integral for the root-mean-square speed. It once again can be separated into three sections.

$$v_{rms}^2 = \int_0^{\infty} v^2 P(v) dv \quad (129)$$

$$= \int_0^{v_0} v^3 * \frac{a}{v_0} dv + \int_{v_0}^{2v_0} v^2 * a dv + \int_{2v_0}^{\infty} v^2 * 0 dv \quad (130)$$

$$= \left[\frac{v^4}{4} \cdot \frac{a}{v_0} \right]_0^{v_0} + \left[\frac{v^3}{3} \cdot a \right]_{v_0}^{2v_0} + [0]_{2v_0}^{\infty} \quad (131)$$

$$= \frac{av_0^3}{4} + \frac{7av_0^3}{3} = av_0^3 \left(\frac{1}{4} + \frac{7}{3} \right) = v_0^2 * \frac{2}{3} \left(\frac{3}{12} + \frac{28}{12} \right) \quad (132)$$

$$= v_0^2 * \left(\frac{62}{36} \right) \quad (133)$$

$$\frac{v_{rms}}{v_0} = \frac{v_0}{v_0} * \frac{\sqrt{62}}{6} = \boxed{1.31} \quad (134)$$

15.4 Solution (d)

Another integral is in order. This stuff is really just statistics at this point. I honestly wish that CCSF had a Probability and Statistics class that used calculus. Unfortunately, it doesn't. MATH80 doesn't require Calculus. It barely even used Algebra. That being said, it was a great tour of what a calculator like a TI-84 Plus can do.

$$\int_{1.5v_0}^{2v_0} a dv = [av]_{1.5v_0}^{2v_0} = a(2v_0 - 1.5v_0) = \frac{1}{2}av_0 = \boxed{\frac{1}{3}} \quad (135)$$

16 Problem 39

At what temperature does the rms speed of (a) H_2 (molecular hydrogen) and (b) O_2 (molecular oxygen) equal the escape speed from Earth (Table 13-2)? At what temperature does the rms speed of (c) H_2 and (d) O_2 equal the escape speed from the Moon (where the gravitational acceleration at the surface has magnitude $0.16g$)? Considering the answers to parts (a) and (b), should there be much (e) hydrogen and (f) oxygen high in Earth's upper atmosphere, where the temperature is about 1000 K ?

16.1 Solution (a)

The escape speed of earth given in table 13-2 of Halliday & Resnick's book is 11.2 km/s . The molar mass of H_2 given by table 19-1 of the same textbook is $2.02 \times 10^{-3}\text{ kg/mol}$. This can be used in the equation for v_{rms} to find the necessary temperature for that velocity to be achieved.

$$v_{rms} = \sqrt{\frac{3RT}{M}} \quad (136)$$

$$T = \frac{Mv_{rms}^2}{3R} = \frac{2.02 \times 10^{-3}\text{ kg/mol} \cdot (11.2 \times 10^3\text{ m/s})^2}{3 \cdot 8.31\text{ J/mol} \cdot \text{K}} \quad (137)$$

$$= \frac{253388.8\text{ J/mol}}{24.93\text{ J/mol}} \cdot \text{K} = \boxed{10164\text{ K}} \quad (138)$$

16.2 Solution (b)

The molar mass of O_2 given by table 19-1 of the same textbook is $32.0 \times 10^{-3}\text{ kg/mol}$. This can be used in the equation for v_{rms} to find the necessary temperature for escape velocity to be achieved.

$$v_{rms} = \sqrt{\frac{3RT}{M}} \quad (139)$$

$$T = \frac{Mv_{rms}^2}{3R} = \frac{32.0 \times 10^{-3}\text{ kg/mol} \cdot (11.2 \times 10^3\text{ m/s})^2}{3 \cdot 8.31\text{ J/mol} \cdot \text{K}} \quad (140)$$

$$= \frac{4014080\text{ J/mol}}{24.93\text{ J/mol}} \cdot \text{K} = \boxed{161014\text{ K}} \quad (141)$$

16.3 Solution (c)

The escape speed of earth's moon given in table 13-2 of Halliday & Resnick's book is 2.38 km/s. The molar mass of H₂ given by table 19-1 of the same textbook is 2.02×10^{-3} kg/mol. This can be used in the equation for v_{rms} to find the necessary temperature for escape velocity to be achieved.

$$v_{rms} = \sqrt{\frac{3RT}{M}} \quad (142)$$

$$T = \frac{Mv_{rms}^2}{3R} = \frac{2.02 \times 10^{-3} \text{ kg/mol} \cdot (2.38 \times 10^3 \text{ m/s})^2}{3 \cdot 8.31 \text{ J/mol} \cdot \text{K}} \quad (143)$$

$$= \frac{1142.088 \text{ J/mol}}{24.93 \text{ J/mol}} \cdot \text{K} = \boxed{458.9686 \text{ K}} \quad (144)$$

16.4 Solution (d)

The molar mass of O₂ given by table 19-1 of the same textbook is 32.0×10^{-3} kg/mol. This can be used in the equation for v_{rms} to find the necessary temperature for escape velocity to be achieved.

$$v_{rms} = \sqrt{\frac{3RT}{M}} \quad (145)$$

$$T = \frac{Mv_{rms}^2}{3R} = \frac{32.0 \times 10^{-3} \text{ kg/mol} \cdot (2.38 \times 10^3 \text{ m/s})^2}{3 \cdot 8.31 \text{ J/mol} \cdot \text{K}} \quad (146)$$

$$= \frac{181260.8 \text{ J/mol}}{24.93 \text{ J/mol}} \cdot \text{K} = \boxed{7270.79 \text{ K}} \quad (147)$$

16.5 Solution (e)

Calculate the expected rms velocity at 1000 K.

$$v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3 \cdot 8.31 \cdot 1000}{2.02 \times 10^{-3}}} \quad (148)$$

$$= \sqrt{\frac{24.93 \times 10^6}{2.02}} = \sqrt{12.34 \times 10^6} \quad (149)$$

$$= 3.51 \times 10^3 \text{ m/s} \quad (150)$$

There should be some hydrogen up there, but a lot of it would have likely escaped since 3.51 is not excessively smaller than 11.2. The answer is no.

16.6 Solution (f)

Calculate the expected rms velocity at 1000 K.

$$v_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3 * 8.31 * 1000}{32.00 \times 10^{-3}}} \quad (151)$$

$$= \sqrt{\frac{24.93 \times 10^6}{32.00}} = \sqrt{0.779 \times 10^6} \quad (152)$$

$$= 0.88 \times 10^3 \text{m/s} \quad (153)$$

There should be a fair amount of hydrogen up there, even if a little of it would have escaped since 0.88 is much smaller than 11.2. The answer is yes.

17 Problem 43

The temperature of 3.00 mol of an ideal diatomic gas is increased by 40.0 C° without the pressure of the gas changing. The molecules in the gas rotate but do not oscillate. (a) How much energy is transferred to the gas as heat? (b) What is the change in the internal energy of the gas? (c) How much work is done by the gas? (d) By how much does the rotational kinetic energy of the gas increase?

17.1 Solution (a)

We have an equation for the energy transferred to the gas as heat.

$$C_P = C_V + R = 20.8 \text{ J/mol} \cdot \text{K} + 8.31 \text{ J/mol} \cdot \text{K} = 29.11 \text{ J/mol} \cdot \text{K} \quad (154)$$

$$Q = nC_P\Delta T = 3.00 \text{ mol} * 29.11 \text{ J/mol} \cdot \text{K} * 40 \text{ K} \quad (155)$$

$$= \boxed{3493.2 \text{ J}} \quad (156)$$

17.2 Solution (b)

We have an equation for the work done on the gas.

$$W = -nR\Delta T = -3.00 \text{ mol} * 8.31 \text{ J/mol} \cdot \text{K} * 40.0 \text{ K} \quad (157)$$

$$= -997.2 \text{ J} \quad (158)$$

The first law of thermodynamics can guide us from here.

$$\Delta E_{int} = Q_{in} + W_{in} = 3493.2 \text{ J} - 997.2 \text{ J} \quad (159)$$

$$= \boxed{2496 \text{ J}} \quad (160)$$

17.3 Solution (c)

The work done by the gas is the aforementioned $\boxed{997.2 \text{ J}}$

17.4 Solution (d)

The rotational kinetic energy is the kinetic energy added that would not be translational. There is a formula for the translational kinetic energy, and we

already know the change in the total energy.

$$\Delta E_{int} = \Delta K_{rot} + \Delta K_{tra} \quad (161)$$

$$\Delta K_{rot} = \Delta E_{int} - \Delta K_{tra} = 2496 \text{ J} - \frac{3}{2} N k * 40 \text{ C}^\circ \quad (162)$$

$$= 2496 \text{ J} - \frac{3}{2} (n * N_A) k * 40 \text{ C}^\circ \quad (163)$$

$$= 2496 \text{ J} - \frac{3}{2} * 1.38 \times 10^{-23} * 3.0 * 6.022 \times 10^{23} * 40 \text{ K} \quad (164)$$

$$= 2496 \text{ J} - 1496 \text{ J} = \boxed{1000 \text{ J}} \quad (165)$$

18 Problem 45

The mass of a gas molecule can be computed from its specific heat at constant volume c_V (note that this is not C_V). Take $c_V = 0.075 \text{ cal/g} \cdot \text{C}^\circ$ for argon and calculate (a) the mass of an argon atom and (b) the molar mass of argon.

18.1 Solution (a)

There is a formula we know involving specific heat (c_V).

$$Q = c_V m \Delta T \quad (166)$$

There also exists a formula for the molar specific heat.

$$C_V = \frac{Q}{n \Delta T} \quad (167)$$

We can assume that the argon is a monoatomic gas, so $C_V = \frac{3}{2}R = 12.5 \text{ J/mol} \cdot \text{K}$. Our equation for thermal energy can be substituted into our equation for the molar specific heat. We can also convert the specific heat to $\text{J/g} \cdot \text{C}^\circ$

$$C_V = \frac{c_V m \Delta T}{n \Delta T} \rightarrow m = \frac{n C_V}{c_V} \quad (168)$$

$$c_v = 0.075 \text{ cal/g} \cdot \text{C}^\circ * 4.184 \frac{\text{J}}{\text{cal}} = 0.3138 \text{ J/g} \cdot \text{C}^\circ \quad (169)$$

We can insert values into this and assume only one mole of argon. In the process of going from here to the mass of one atom, we will find the molar mass of argon.

$$m = \frac{12.5 \text{ J/mol} \cdot \text{K}}{0.3138 \text{ J/g} \cdot \text{C}^\circ} * 1 \text{ mol} = 39.83 \text{ g/mol} * \frac{1 \text{ mol}}{6.022 \times 10^{23} \text{ molecule}} \quad (170)$$

$$= \boxed{6.615 \times 10^{-23} \text{ g}} \quad (171)$$

18.2 Solution (b)

As established in part (a), the molar mass of argon is $\boxed{39.83 \text{ g/mol}}$.

18.3 Note on the problem

This problem did a good job at integrating previous chapters. It has a good premise and a decent pathway to the solution, but I probably would have put it under “Additional Problems”.

19 Problem 47

The temperature of 2.00mol of an ideal monatomic gas is raised 15.0 K at constant volume. What are (a) the work W done by the gas, (b) the energy transferred as heat Q , (c) the change ΔE_{int} in the internal energy of the gas, and (d) the change ΔK in the average kinetic energy per atom?

19.1 Solution (a)

The volume is constant, so the net work done by the gas would be $\boxed{0 \text{ J}}$.

19.2 Solution (b)

The heat transferred can be calculated by using the change in temperature.

$$Q = nC_V\Delta T = 2 \text{ mol} * 12.5 \text{ J/mol} \cdot \text{K} * 15.0 \text{ K} \quad (172)$$

$$= \boxed{375 \text{ J}} \quad (173)$$

19.3 Solution (c)

Since the change in internal energy in thermodynamics is the sum of the work done on and the heat inserted into the system, the total change in energy would be this sum. Since no work is done on (or by) the gas, the total change in energy would be the amount of thermal energy inserted, so $\boxed{375 \text{ J}}$.

19.4 Solution (d)

We just divide the total change in internal energy (see above) by the number of molecules ($2 * 6.022 \times 10^{23}$) to get the average change in kinetic energy in each molecule.

$$\Delta K_{\text{avg}} = \frac{375 \text{ J}}{12.044 \times 10^{23}} = \boxed{3.11 \times 10^{-22} \text{ J}} \quad (174)$$

20 Problem 51

When 1.0 mol of oxygen (O_2) gas is heated at constant pressure starting at 0°C , how much energy must be added to the gas as heat to double its volume? The molecules rotate but do not oscillate.

20.1 Solution

Since the molecules rotate but do not oscillate, they do not have any translational degrees of freedom. This limits them to 2 degrees of freedom. This settles us with a value for the molar specific heat.

$$C_V = \left(\frac{f}{2}\right) R = \frac{5}{2}R \quad (175)$$

$$C_P = \frac{5}{2}R + R = \frac{7}{2}R \quad (176)$$

We have an indeterminate value for the initial volume and a related one for the final volume. We can use these to find an equation for the change in temperature by using the work.

$$W = p\Delta V = nR\Delta T = pV_0 \quad (177)$$

$$\Delta T = \frac{pV_0}{nR} \quad (178)$$

There's also an equation for the heat added.

$$Q = nC_P\Delta T = n * \frac{7}{2}R \frac{pV_0}{nR} = \frac{7}{2}pV_0 \quad (179)$$

The ideal gas law has an equation for the (initial) pressure times the volume. We can use that.

$$pV_0 = nRT_0 = 1 \text{ mol} * 8.31 \text{ J/mol} \cdot \text{K} * 273 \text{ K} \quad (180)$$

$$= 2268.63 \text{ J} \quad (181)$$

This can be substituted into our equation for the heat to be added to get the answer.

$$Q = \frac{7}{2}pV_0 = \frac{7}{2} * 2268.63 \text{ J} \quad (182)$$

$$= \boxed{7940.205 \text{ J}} \quad (183)$$

21 Problem 55

A certain gas occupies a volume of 4.3 L at a pressure of 1.2 atm and a temperature of 310 K. It is compressed adiabatically to a volume of 0.76 L. Determine (a) the final pressure and (b) the final temperature, assuming the gas to be an ideal gas for which $\gamma = 1.4$.

21.1 Solution (a)

There's an equation for this.

$$p_1 V_1^\gamma = p_2 V_2^\gamma \quad (184)$$

$$p_2 = p_1 \frac{V_1^\gamma}{V_2^\gamma} = 1.2 \text{ atm} * \left(\frac{4.3 \text{ L}}{0.76 \text{ L}} \right)^{1.4} \quad (185)$$

$$= 1.2 \text{ atm} * 11.32 = \boxed{13.58 \text{ atm}} \quad (186)$$

21.2 Solution (b)

This is an ideal gas, so the ideal gas law governs it.

$$p_1 V_1 = nRT_1 \quad (187)$$

$$p_2 V_2 = nRT_2 \quad (188)$$

$$\frac{p_1 V_1}{p_2 V_2} = \frac{nRT_1}{nRT_2} = \frac{T_1}{T_2} \quad (189)$$

From here, we can solve for the final temperature (T_2).

$$T_2 = T_1 \frac{p_2 V_2}{p_1 V_1} = 310 \text{ K} * \frac{13.58 * 0.76}{1.2 * 4.3} \quad (190)$$

$$= \boxed{620 \text{ K}} \quad (191)$$

22 Problem 57

The volume of an ideal gas is adiabatically reduced from 200 L to 74.3 L. The initial pressure and temperature are 1.00 atm and 300 K. The final pressure is 4.00 atm. (a) Is the gas monatomic, diatomic, or polyatomic? (b) What is the final temperature? (c) How many moles are in the gas?

22.1 Solution (a)

We can find this by finding the value of γ . By its nature, $\gamma = C_P/C_V$. There are three possibilities of final values.

Monatomic:

$$\gamma = \frac{\frac{5}{2}R}{\frac{3}{2}R} = \frac{5}{3} \quad (192)$$

Diatomic:

$$\gamma = \frac{\frac{7}{2}R}{\frac{5}{2}R} = \frac{7}{5} = 1.4 \quad (193)$$

Polyatomic:

$$\gamma = \frac{4R}{3R} = \frac{4}{3} \quad (194)$$

From here, we can use our equation for ideal gas under adiabatic volume change.

$$p_i V_i^\gamma = p_f V_f^\gamma \quad (195)$$

$$\frac{p_i}{p_f} = \left(\frac{V_f}{V_i} \right)^\gamma \quad (196)$$

$$\frac{1}{4} = \left(\frac{74.3}{200} \right) \quad (197)$$

$$\gamma = \log_{0.3715}(0.25) \approx 1.4 \quad (198)$$

This solidifies that the gas is *diatomic*.

22.2 Solution (b)

We can use our friend the ideal gas law.

$$p_i V_i = nRT_i \quad (199)$$

$$p_f V_f = nRT_f \quad (200)$$

$$\frac{p_i V_i}{p_f V_f} = \frac{nRT_i}{nRT_f} = \frac{T_i}{T_f} \quad (201)$$

From here, we can solve for the final temperature.

$$T_f = T_i \frac{p_f V_f}{p_i V_i} = 300 \text{ K} * \frac{4 * 74.3}{1 * 200} = 300 \text{ K} * \frac{297.2}{200} \quad (202)$$

$$= 300 \text{ K} * 1.486 = \boxed{445.8 \text{ K}} \quad (203)$$

22.3 Solution (c)

The right move here is to convert atmospheres to pascals and liters to cubic meters. We then use the ideal gas law. I will do this by using the initial conditions.

$$p = 1.00 \text{ atm} \times \frac{101325 \text{ Pa}}{1 \text{ atm}} = 101325 \text{ Pa} \quad (204)$$

$$V = 200 \text{ L} \times \frac{0.001 \text{ m}^3}{1 \text{ L}} = 0.2 \text{ m}^3 \quad (205)$$

$$pV = nRT \quad (206)$$

$$n = \frac{pV}{RT} = \frac{101325 \text{ Pa} * 0.2 \text{ m}^3}{8.31 \text{ J/mol} \cdot \text{K} * 300 \text{ K}} \quad (207)$$

$$= \frac{20265}{2493} \text{ mol} = \boxed{8.13 \text{ mol}} \quad (208)$$

23 Problem 59

Figure 19-26 shows two paths that may be taken by a gas from an initial point i to a final point f . Path 1 consists of an isothermal expansion (work is 50 J in magnitude), an adiabatic expansion (work is 40 J in magnitude), an isothermal compression (work is 30 J in magnitude), and then an adiabatic compression (work is 25 J in magnitude). What is the change in the internal energy of the gas if the gas goes from point i to point f along path 2?

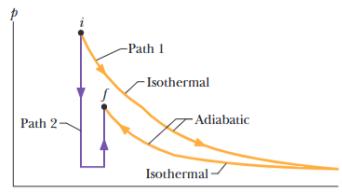


Figure 19-26 Problem 59.

23.1 Solution

We can assign letters to the four processes from a to d based on their ordering between i and f . Along the pressure-volume scale, the change in internal energy is path independent, so the energy change from i to f would be the same along either path. There are two types of expansions/compressions along the path: adiabatic (no change in thermal energy; $Q = 0$) and isothermal (constant temperature; $\Delta T = 0$). For the adiabatic processes, there is a formula for their change in internal energy.

$$\Delta E_{\text{int};b} = W_{\text{in}} = -40 \text{ J} \quad (209)$$

$$\Delta E_{\text{int};d} = W_{\text{in}} = 25 \text{ J} \quad (210)$$

For isothermal processes, the work in is equal to the negative of the heat drawn in. We can use this to find the change in energy for paths (a) and (c).

$$\Delta E_{\text{int};a} = Q_{\text{in}} + W_{\text{in}} = Q_{\text{in}} - Q_{\text{in}} = 0 \quad (211)$$

$$\Delta E_{\text{int};c} = Q_{\text{in}} + W_{\text{in}} = Q_{\text{in}} - Q_{\text{in}} = 0 \quad (212)$$

Adding up all of these, we can get the total change in internal energy.

$$\Delta E_{\text{int}} = \Delta E_{\text{int};a} + \Delta E_{\text{int};b} + \Delta E_{\text{int};c} + \Delta E_{\text{int};d} \quad (213)$$

$$= 0 - 40 \text{ J} + 0 + 25 \text{ J} = \boxed{-15 \text{ J}} \quad (214)$$

24 Problem 63

Figure 19-27 shows a cycle undergone by 1.00 mol of an ideal monatomic gas. The temperatures are $T_1 = 300$ K, $T_2 = 600$ K, and $T_3 = 455$ K. For $1 \rightarrow 2$, what are (a) heat Q , (b) the change in internal energy ΔE_{int} , and (c) the work done W ? For $2 \rightarrow 3$, what are (d) Q , (e) ΔE_{int} , and (f) W ? For $3 \rightarrow 1$, what are (g) Q , (h) ΔE_{int} , and (i) W ? For the full cycle, what are (j) Q , (k) ΔE_{int} , and (l) W ? The initial pressure at point 1 is 1.00 atm ($= 1.013 \times 10^5$ Pa). What are the (m) volume and (n) pressure at point 2 and the (o) volume and (p) pressure at point 3?

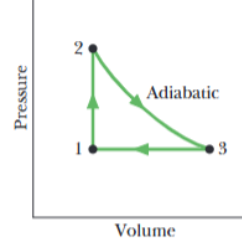


Figure 19-27 Problem 63.

24.1 Solution (a), (b), (c)

The process here is isochoric because there is no change in volume *at all*. This means that there is no net work. Meanwhile, the heat is equivalent to the change in all internal energy, which has a formula to it.

$$\Delta E_{\text{int}} = Q = nC_V \Delta T = 1 \text{ mol} * \frac{3}{2} R * 300 \text{ K} \quad (215)$$

$$= 3739.5 \text{ J} \quad (216)$$

(a)	(b)	(c)
Q	ΔE_{int}	W
3739.5J	3739.5J	0J

24.2 Solution (d), (e), (f)

The process being adiabatic, the change in thermal energy (heat) is zero. This in turn would mean that $\Delta E_{\text{int}} = W$. The change in energy is defined by its own formula.

$$\Delta E_{\text{int};23} = nC_V \Delta T = 1 \text{ mol} * \frac{3}{2} R * (-145 \text{ J}) \quad (217)$$

$$= -1807.425 \text{ J} \quad (218)$$

(d)	(e)	(f)
Q	ΔE_{int}	W
0J	-1807.425 J	-1807.425 J

24.3 Solution (g), (h), (i)

The process here is isobaric. The heat and work both come with formulas in this case.

$$Q = nC_P\Delta T = 1 \text{ mol} * \frac{5}{2}R * (-155 \text{ K}) \quad (219)$$

$$= -3220.125 \text{ J} \quad (220)$$

$$W = -p\Delta V = -nR\Delta T = -1 \text{ mol} * R * (-155 \text{ K}) \quad (221)$$

$$= 1288.05 \text{ J} \quad (222)$$

$$\Delta E_{\text{int};31} = Q + W = -3220.125 \text{ J} + 1288.05 \text{ J} \quad (223)$$

$$= -1932.075 \text{ J} \quad (224)$$

(g)	(h)	(i)
Q	ΔE_{int}	W
-3220.125 J	-1932.075 J	1288.05 J

24.4 Solution (j), (k), (l)

The way to go about this is by adding up values.

$$Q = Q_{12} + Q_{23} + Q_{31} = 3739.5 + 0 - 3220.125 = 519.375 \text{ J} \quad (225)$$

$$\Delta E_{\text{int}} = \Delta E_{12} + \Delta E_{23} + \Delta E_{31} = 3739.5 - 1807.425 - 1932.075 = 0 \text{ J} \quad (226)$$

$$W = W_{12} + W_{23} + W_{31} = 0 - 1807.425 + 1288.05 = -519.375 \text{ J} \quad (227)$$

The fact that $\Delta E_{\text{int}} = 0$ makes sense. Looking at the overall graph, the whole process is cyclical, which would naturally have a net zero internal energy change. This leads well into the fact that $Q = -W$.

(g)	(h)	(i)
Q	ΔE_{int}	W
519.375 J	0 J	-519.375 J

24.5 Solution (m)

The volume at point 1 would be the same as at point 2. We can use the ideal gas law here.

$$pV = nRT \quad (228)$$

$$V = \frac{nRT}{p} = \frac{1 \text{ mol} * 8.31 \text{ J/mol} \cdot \text{K} * 300 \text{ K}}{1.013 \times 10^5} \quad (229)$$

$$= \boxed{0.0246 \text{ m}^3} \quad (230)$$

24.6 Solution (n)

This creates an equivalence from the ideal gas law.

$$pV = nRT \rightarrow \frac{p}{T} = \frac{nR}{V} \rightarrow \frac{p_1}{T_1} = \frac{p_2}{T_2} \quad (231)$$

$$p_2 = p_1 \frac{T_2}{T_1} = 1.013 \times 10^5 \text{ Pa} * \frac{600 \text{ K}}{300 \text{ K}} \quad (232)$$

$$= \boxed{2.026 \times 10^5 \text{ Pa}} \quad (233)$$

24.7 Solution (o)

We can use the same ideal gas law, this time with changing volume and constant pressure.

$$pV = nRT \rightarrow \frac{V}{T} = \frac{nR}{p} \rightarrow \frac{V_1}{T_1} = \frac{V_2}{T_2} \quad (234)$$

$$V_2 = V_1 \frac{T_2}{T_1} = 0.226 \text{ m}^3 * \frac{455 \text{ K}}{300 \text{ K}} \quad (235)$$

$$= \boxed{0.343 \text{ m}^3} \quad (236)$$

24.8 Solution (p)

The pressure at point 3 is the same as that at point 1, so it would be $\boxed{1.013 \times 10^5 \text{ Pa}}$.

25 Problem 69

The envelope and basket of a hot-air balloon have a combined weight of 2.45 kN, and the envelope has a capacity (volume) of $2.18 \times 10^3 \text{ m}^3$. When it is fully inflated, what should be the temperature of the enclosed air to give the balloon a *lifting capacity* (force) of 2.67 kN (in addition to the balloon's weight)? Assume that the surrounding air, at 20.0°C, has a weight per unit volume of 11.9 N/m³ and a molecular mass of 0.028 kg/mol, and is at a pressure of 1.0 atm.

25.1 Solution

The total upwards force would have to be greater than (or equal to) the sum of the lifting capacity and the earlier combined weight.

$$F_{\text{total}} = F_{\text{weight}} + F_{\text{lifting}} = 2.45 \times 10^3 + 2.67 \times 10^3 = 5.12 \times 10^3 \text{ N} \quad (237)$$

This would be the necessary net force, which would be the net force from the internal gas upwards and the outer gas downwards. We can assume that the air outside has the same (immutable) properties as that on the inside. We can find the buoyant force, being the force of or on the air opposing the gravitational force.

$$F_b = \rho g V = 11.9 \text{ N/m}^3 * 2.18 \times 10^3 \text{ m}^3 \quad (238)$$

$$= 25942 \text{ N} \quad (239)$$

The buoyant force is one of the two forces that would act on the balloon. The other force in question would be the weight of the hot air. This weight could be calculated by the ideal gas law.

$$F_{\text{total}} = F_b - F_{\text{weight}} \quad (240)$$

$$pV = nRT \quad (241)$$

$$n = \frac{PV}{RT} \quad (242)$$

$$m = MM * n = \frac{PV * MM}{RT} \quad (243)$$

$$F_{\text{weight}} = g * m = g * \frac{PV * MM}{RT} \quad (244)$$

Our unknown here is the temperature (T), which we can find using our equation. The air pressure outside would be 1 atm, which is equivalent to $1.013 \times 10^5 \text{ Pa}$.

$$F_{\text{total}} = F_b - F_{\text{weight}} \quad (245)$$

$$F_b - F_{\text{total}} = g * \frac{PV * MM}{RT} \quad (246)$$

$$\frac{R(F_b - F_{\text{total}})}{g * P * V * MM} = \frac{1}{T} \quad (247)$$

$$T = \frac{g * P * V * MM}{R(F_b - F_{\text{total}})} = \frac{9.81 * 1.013 \times 10^5 * 2.18 \times 10^3 * 0.028}{R(25942 - 5.12 \times 10^3)} \quad (248)$$

$$= \frac{0.60659 \times 10^8}{8.31 * 20822} = \boxed{350.566 \text{ K}} \quad (249)$$

26 Problem 75

The temperature of 3.00 mol of a gas with $C_V = 6.00 \text{ cal/mol} \cdot \text{K}$ is to be raised 50.0 K. If the process is at constant volume, what are (a) the energy transferred as heat Q , (b) the work W done by the gas, (c) the change ΔE_{int} in internal energy of the gas, and (d) the change ΔK in the total translational kinetic energy? If the process is at constant pressure, what are (e) Q , (f) W , (g) ΔE_{int} , and (h) ΔK ? If the process is adiabatic, what are (i) Q , (j) W , (k) ΔE_{int} , and (l) ΔK ?

26.1 Solution

27 Problem 77

Figure 19-28 shows a hypothetical speed distribution for particles of a certain gas: $P(v) = Cv^2$ for $0 < v \leq v_0$ and $P(v) = 0$ for $v > v_0$. Find (a) an expression for C in terms of v_0 , (b) the average speed of the particles, and (c) their rms speed.

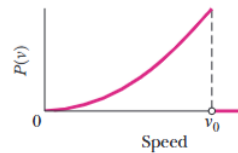


Figure 19-28 Problem 77.

27.1 Solution

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