

Homework #4, 4B

Donald Aingworth IV

February 12, 2025

1 Question 1

A surface that has the area vector $\vec{A} = (2\hat{i} + 3\hat{j}) \text{ m}^2$. What is the flux of a uniform electric field that is (a) $\vec{E} = 4\hat{i}\text{N/C}$ and (b) $\vec{E} = 4\hat{k}\text{N/C}$?

2 Question 3

Figure 23-23 shows, in cross section, a central metal ball, two spherical metal shells, and three spherical Gaussian surfaces of radii R , $2R$, and $3R$, all with the same center. The uniform charges on the three objects are: ball, Q ; smaller shell, $3Q$; larger shell, $5Q$. Rank the Gaussian surfaces according to the magnitude of the electric field at any point on the surface, greatest first.

3 Problem 6

Three infinite nonconducting sheets, with uniform positive surface charge densities σ , 2σ , and 3σ , are arranged to be parallel like the two sheets in Fig. 23-19a. What is their order, from left to right, if the electric field \vec{E} produced by the arrangement has magnitude $E = 0$ in one region and $E = 2\sigma/\epsilon_0$ in another region?

Solution

For an infinite nonconducting sheet of density σ , the electric field from it is equal to $E = \sigma/2\epsilon_0$. We can use this to provide a system of equations for electric field strengths (a, b, c) , which have unique magnitudes in the set $(\sigma/2\epsilon_0, 2\sigma/2\epsilon_0, 3\sigma/2\epsilon_0)$ or alternatively $(E, 2E, 3E)$.

$$\begin{aligned}a - b - c &= 0 \\a + b - c &= 2\sigma/\epsilon_0 = 4E \\0a + 2b + 0c &= 4E \\b &= 2E = 2\sigma/2\epsilon_0 \\a - 2E - c &= 0 \rightarrow a - c = 2E\end{aligned}$$

There is only one combination of the remaining two that this works for: $a = 3E$ and $c = E$. Thus, the order is $\boxed{\langle 3\sigma, 2\sigma, \sigma \rangle}$.

4 Problem 8

Figure 23-27 shows four solid spheres, each with charge Q uniformly distributed through its volume. (a) Rank the spheres according to their volume charge density, greatest first. The figure also shows a point P for each sphere, all at the same distance from the center of the sphere. (b) Rank the spheres according to the magnitude of the electric field they produce at point P , greatest first.

5 Problem 10

Figure 23-34 shows a closed Gaussian surface in the shape of a cube of edge length 2.00 m. It lies in a region where the nonuniform electric field is given by $\mathbf{E} = (3.00x + 4.00)\mathbf{i} + 6.00\mathbf{j} + 7.00K\mathbf{k}$ N/C with x in meters. What is the net charge contained by the cube?

6 Problem 12

Figure 23-36 shows two nonconducting spherical shells fixed in place. Shell 1 has uniform surface charge density $+6.0 \text{ } \mu\text{C}/\text{m}^2$ on its outer surface and radius 3.0 cm; shell 2 has uniform surface charge density $+4.0 \text{ } \mu\text{C}/\text{m}^2$ on its outer surface and radius 2.0 cm; the shell centers are separated by $L = 10 \text{ cm}$. In unit- vector notation, what is the net electric field at $x = 2.0 \text{ cm}$?

7 Problem 18

The electric field just above the surface of the charged conducting drum of a photocopying machine has a magnitude E of $2.3 \times 10^5 \text{ N/C}$. What is the surface charge density on the drum?

8 Problem 22

An electron is released 9.0 cm from a very long nonconducting rod with a uniform $6.0 \text{ } \mu\text{C}/\text{m}$. What is the magnitude of the electron's initial acceleration?

9 Problem 28

A charge of uniform linear density 2.0 nC/m is distributed along a long, thin, non-conducting rod. The rod is coaxial with a long conducting cylindrical shell (inner radius = 5.0 cm , outer radius = 10 cm). The net charge on the shell is zero. (a) What is the magnitude of the electric field 15 cm from the axis of the shell? What is the surface charge density on the (b) inner and (c) outer surface of the shell?

10 Problem 34

In Fig. 23-45, a small circular hole of radius $R = 1.80 \text{ cm}$ has been cut in the middle of an infinite, flat, nonconducting surface that has uniform charge density $\sigma = 4.50 \text{ pC/m}^2$. A z axis, with its origin at the hole's center, is perpendicular to the surface. In unit-vector notation, what is the electric field at point P at $z = 2.56 \text{ cm}$? (Hint: See Eq. 22-26 and use superposition.)