

# Homework #16

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# 1 Problem 1

Two disks are mounted (like a merry-go-round) on low-friction bearings on the same axle and can be brought together so that they couple and rotate as one unit. The first disk, with rotational inertia  $3.30 \text{ kg} \cdot \text{m}^2$  about its central axis, is set spinning counterclockwise at  $450 \text{ rev/min}$ . The second disk, with rotational inertia  $6.60 \text{ kg} \cdot \text{m}^2$  about its central axis, is set spinning counterclockwise at  $900 \text{ rev/min}$ . They then couple together. (a) What is their angular speed after coupling? If instead the second disk is set spinning clockwise at  $900 \text{ rev/min}$ , what are their (b) angular speed and (c) direction of rotation after they couple together?

## 1.1 Solution

### 1.1.1 Section (a)

We have a concept called conservation of angular momentum.

$$L_i = L_f \tag{1}$$

$$L_f = l_1 + l_2 = I_1\omega_1 + I_2\omega_2 \tag{2}$$

$$\omega_f = \frac{I_1\omega_1 + I_2\omega_2}{I_1 + I_2} = \frac{3.3 * 450 + 6.6 * 900}{3.3 + 6.6} \tag{3}$$

$$= \frac{1485 + 5940}{9.9} = \boxed{750 \text{ rev/min}} \tag{4}$$

### 1.1.2 Section (b)

We just need to change a positive to a negative.

$$\omega_f = \frac{I_1\omega_1 + I_2\omega_2}{I_1 + I_2} = \frac{3.3 * 450 - 6.6 * 900}{3.3 + 6.6} \tag{5}$$

$$= \frac{1485 - 5940}{9.9} = \boxed{-450 \text{ rev/min}} \tag{6}$$

### 1.1.3 Section (c)

Since the magnitude is negative and negative angular velocity corresponds to clockwise motion, the angular motion is clockwise.

## 2 Problem 2

The Sun's mass is  $2.0 \times 10^{30}$  kg, its radius is  $7.0 \times 10^5$  km, and it has a rotational period of approximately 28 days. If the Sun should collapse into a white dwarf of radius  $3.5 \times 10^3$  km, what would its period be if no mass were ejected and a sphere of uniform density can model the Sun both before and after?

### 2.1 Solution