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| **Various Adder implementation on Qiskit**  **and their performance comparison** |
| Team QAS Seunghoon Choi(Team leader), Hyejin Yoon, Se-bin Kim, Sumin Jin, Youshin Chung |
| **Abstract**  **As part of IBM challenge topic 1, we have build and tested several adders including full adder and Quantum Fourier adder on Qiskit and checked their performances by checking the propriate output of 40000 input. By this processes, we have demonstrated transpiled CCX gate changed adder has most high performance among 4 adders and** | | |

**1.Introduction**

**1.1 About us**

Our team has 3 undergraduate students from GIST(Gwangju Institute of Science and Technology), 1 graduate student from Korea University, and 1 undergraduate student from Hongik University. Since this Hackathon was the encounter to Qauntum computing domain of 3 GIST members, it was big challenge for us to use Qiskit and utilize Quantum gates. But our curiosity lead us to attend IBM Quantum Challenge topic 1: Build your minimal quantum circuit - making a quantum calculator. We realized ‘adder’ is one of the most important calculators on quantum computing, so tried to optimize the numbers of quantum gate composing adders.

On first day, we tried to minimize the number of gates of various adders featured in IBM challenge. But passing several hours, we learned that it is not efficient to come up with a way to reduce size of the circuits simply by using imagination. And by getting advice from mentors, we realized that QFT adder now we are using has not so much part to minimize.

So, what we can do was narrowed by two: 1.Error correction and 2.implementing various adders. We decided to concentrate on composing various type of adders on Qiskit. Taking one step forward from the first day, we try using Qiskit ‘Unroller’, ‘Transpiler’ for decomposing and so minimizing circuits. Further, we compared their performance with original adders.

**1.2 background**

**1.2.1 Full Adder**

Full adder is a circuit that gives following operation in Table 1 for given input A, B, Cin.[1]

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| A | B | Cin | Sum | Count |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

Table 1. Truth table of full adder

For a reversible machine, a full adder using quantum gate can be described in the following way in Fig.1. This circuit is introduced in “Foundations of Physics, Springer Science and Business Media LLC. 16(6)’ by R. Feynman. We used this circuit when testing simple optimization and transpiler.

Chart

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Fig 1. Full adder circuit using cx and ccx gate.

**1.2.2 Ripple Carry Adder**

Ripple Carry adder is an extension of full adder. This adder is for larger data (Fig.2). A quantum ripple-carry addition circuit is consisted of 2 steps. Adding each input bit unit and acquiring sum for each unit and Intitailizing each resistor for further usage.

Diagram, schematic

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Fig 2. Ripple-Carry Adder for n=6

MAJ is a circuit that gives carry of ai and bi. After applying UMA circuit, we get sum of each unit and final carry. The architecture of MAJ and UMA is on Fig 3 and Fig 4.[2]

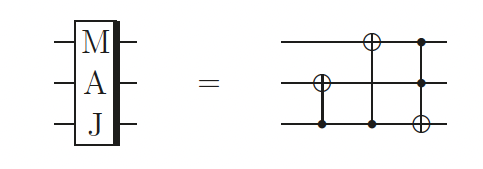


Fig 3. MAJ architecture

Diagram

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Fig 4. UMA architecture

**1.2.3 QFT Adder**

Earlier time, quantum addition algorithms mirrored their classical computers with necessary extensions for a reversible computation, but ideal addition algorithm for a quantum computer may not be similar to its classical counterpart. That’s why the quantum adder on the base of quantum Fourier Transform was invented. Fig 5. is the Diagram of QFT adder. Also, each gate can be depicted as a matrix form like Fig 6.[3]

***A picture containing text, clock, bicycle

Description automatically generated*** Fig5. The quantum addition scheme based on QFT

Diagram, schematic

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Fig 6. QFT scheme and it’s mathematical form

**2. Method and Result**

As mentioned above, our project took three steps. The driving force was that ccx gate is fatal to efficiency of a circuit. First, we tried to think of an optimized unit without any devices. Since this attempt didn’t work well, we tried unroller to convert ccx gate to basis gates; ‘id’, ‘rz’, ‘sx’, ‘x’, ‘cx’ in Qiskit expression. The reason why basis gates are used is because they support immediate executaion.[4] Using unroller, mentors advised us to use transpiler. Therefore, our final attempt, the result, is done by using transpiler.

**2.1 Full Adder**

We also diversified full adder in 4 version.

**(1) Original Full adder**

We brought full adder source from Feynman’s article[1] and composed it on Qiskit. By giving 4000 times input of ‘10’, we get 2669 times ‘10’(which is propriate).

Diagram, schematic

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Fig 5. original full adder

**(2) CCX changed Full adder**

From (1), we changed CCX gate into CH-CZ-CH gates on Qiskit, and this time gived 4000 times input of ‘00’ and get 2741 times ‘00’(whick is propriate).

Chart, box and whisker chart

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Fig 6. ccx gate changed original full adder

**(3) Transpiled original full adder**

This time, we transpiled original full adder(2) on Qiskit. By giving 4000 times input of ‘10’, we get 3023times ‘10’(which is propriate).

Diagram, schematic

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Fig 7. Transpiled original full adder

**(4) Transpiled CCX changed full adder**

Lastly, we transpiled CCX changed adder(1) on Qiskit. By giving 4000 times input of ‘00’, we get 3173 times ‘00’(which is propriate).

Table

Description automatically generated with medium confidence

Fig 8. Transpiled ccx changed full adder

Table 2 is the table showing all the result from full adder section.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | (1) | (2) | (3) | (4) |
| rank | 4 | 3 | 2 | 1 |
| performance | 2669 | 2741 | 3023 | 3173 |

Table 2. Performance comparison in 4 cases of full adder

We have done 5 times of simulation for each adder with same input everytime. And we plotted performances of each desired case for every trials. Fig 9 is the plotted graph.

**Chart, line chart

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Fig 9. Attempt to decompose u3 gate

**2.2 Ripple-Carry Adder**

Before looking at the result, we want to explain path to acquiring final circuits that we are comparing. At first, using unroller, we constructed Ripple Carry Adder with unitary gate (Fig 10).

Chart

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Fig 10. ccx replaced into u3 gate in ripple-carry adder

Though this is expected to be more efficient than circuit in (Fig ), we wanted to change unitary gate into basis gate. Since it was unable to decompose u3 gate into basis gate in unroller, we attempted to change it by hand. Fig 11. shows this process.

Diagram, engineering drawing

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Fig 11. Attempt to decompose u3 gate

Transpiler made it easier to decompose ripple-carry circuit into basis gates. This function selects more efficient decomposed circuit than given circuit. Therefore, we decided to use Transpiler for the final circuits compared.

Timeline

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Fig 12. Rewriting steps of transpiler

The circuit that is a subject to transpiler process was following ripple-carry circuits: original circuit (Fig), transpiled original ripple-carry circuit circuit (Fig), modified ripple-carry circuit (Fig ), transpiled modified ripple-carry circuit(Fig ). We compared efficiency of these four circuits with 6 qubit input. Especially, the fourth circuit was expected to perform better than the other two, because this circuit is a circuit that has already gone through pass 2 in Fig 12.

**(1) Original ripple-carry circuit**

Chart, line chart

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Fig 13. Original Ripple-carry circuit

**(2) Modified ripple-carry circuit**

Chart

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Fig 14. Modified Ripple-carry circuit

**(3) Transpiled Original ripple-carry circuit**

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Fig 15. Transpiled Original Ripple-carry circuit

**(4) Transpiled modified ripple-carry circuit**

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Fig 16. Modified Ripple-carry circuit

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | (1) | (2) | (3) | (4) |
| rank | 4 | 3 | 2 | 1 |
| performance | 1234 | 1092 | 1594 | 2501 |

Table 3. Performance comparison in 4 cases of full adder

Chart, line chart

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Fig 17. Compating Ripple-Carry Adder Circuit

**2.3 QFT Adder**

**3. Conclusion**

**3.1 Result**

We found Transpiled CCX(CCX to CH-CZ-CH) changed QFT adder and transpiled ccx changed adder has most high performances on each group. From this, it seems transpiling is well working function for minimizing circuit. And by that

**3.2 Future implication**

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**4. References**

**[1] R. Feynman (1986). Foundations of Physics. Springer Science and Business Media LLC. 16 (6): 507–531.**

**[2] V. Vedral, A. Barenco, A. Ekert (1995). Quantum Networks for Elementary Arithmetic Operations.**

**[3]A.V.Cherkas and S.A. Chivilikhin, Quantum Adder of Classical Numbers, 2016 J.Phys.: Conf. Ser. 735.**

**[4] Qiskit Development Team, Transpiler, 2022.06.28.,** **https://qiskit.org/documentation/apidoc/transpiler.html**