

### 3. Project [100 points]

Write a script which has the following functionality inside:

a) [35 points] Write a function which, given a vector of coefficients  $\mathbf{p}$  as well as a starting point  $a$  and an end point  $b$ , integrates the polynomial (see `np.polyval(p, x)`) from  $a$  to  $b$  and returns the value of the integral and the estimated error in two separate variables.

b) [65 points] Write a function which plots spherical Bessel functions in a 3D plot as a function of  $x$  and  $y$  with  $r = \sqrt{x^2 + y^2}$ . As input define which spherical Bessel function,  $j_n(r)$  (first kind) or  $y_n(r)$  (second kind), is being plotted and also the order  $n$ . Moreover, specify the  $x$  and the  $y$  range as input. Put axes with five ticks (and tick labels) in the  $x$  and  $y$  directions and four ticks in the  $z$  direction. Add title and proper labels. The plot shall not be displayed on the screen but be exported as a pdf file.

In the main part of the script call the functions with arbitrary test values and print input as well as output.

Happy coding!