Instrumental Variables

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Debugging

- Rubber duck debugging:
 - Use when you can't figure out why your code doesn't work right
 - Find something inanimate to talk to
 - Explain what your code does, line by excruciating line
 - If you can't explain it, that's probably where the problem is.
 - This works ridiculously well.
 - You should also be able to tell your duck exactly what is stored in each variable at all times.
- Check individual elements of your code on small data such that you know what the right answer *should* be.

Introduce an Example

- We'll be working with data from a paper in the most recent issue of IO.
- Helfer, L.R. and E. Voeten. (2014) "International Courts as Agents of Legal Change: Evidence from LGBT Rights in Europe"
- The treatment we are interested in is the presence of absence of a ECtHR judgment.
- The outcome is the adoption of progressive LGBT policy.
- And there's a battery of controls, of course.
- Voeten has helpfully put all replication materials online.

Prepare example

```
require(foreign,quietly=TRUE)
d <- read.dta("replicationdataIOLGBT.dta")</pre>
```

```
#Base specification
d\( ecthrpos <- as.double(d\( ecthrpos ) -1 \)
d.lm <- lm(policy~ecthrpos+pubsupport+ecthrcountry+lgbtlaws+cond+eumember0+euemploy+coemember0
d <- d[-d.lm$na.action,]</pre>
d$issue <- as.factor(d$issue)
d$ccode <- as.factor(d$ccode)
summary(d.lm)$coefficients[1:11,]
                                Std. Error
                                              t value
                     Estimate
                                                           Pr(>|t|)
## (Intercept) -1.588605e+00 4.956355e-01 -3.2051890 1.360035e-03
## ecthrpos
                 6.500937e-02 1.056423e-02 6.1537237 8.289029e-10
## pubsupport
                 6.549488e-03 2.742967e-03 2.3877390 1.699714e-02
## ecthrcountry 1.297322e-01 3.583626e-02 3.6201389 2.979822e-04
## lgbtlaws
                 2.358238e-02 6.280655e-03 3.7547646 1.758966e-04
## cond
                 9.277344e-02 1.795954e-02 5.1656905 2.508722e-07
## eumember0
                -8.586409e-03 8.497519e-03 -1.0104607 3.123339e-01
## euemploy
                 3.659200e-03 1.269275e-02 0.2882905 7.731389e-01
## coemembe
                 2.082823e-02 7.276808e-03 2.8622754 4.227313e-03
                -7.522448e-07 4.501392e-07 -1.6711382 9.477027e-02
## lngdp
                 8.019830e-04 2.522046e-04 3.1798904 1.484223e-03
## year
```

Marginal Effects

- Blattman (2009) uses marginal effects "well" in the sense of causal inference.
- Use the builtin predict function; it will make your life easier.

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```
d.lm.interact <- lm(policy~ecthrpos*pubsupport+ecthrcountry+lgbtlaws+cond+eumember0+euemploy
frame0 <- frame1 <- model.frame(d.lm.interact)
frame0[,"ecthrpos"] <- 0
frame1[,"ecthrpos"] <- 1
meff <- mean(predict(d.lm.interact,newd=frame1) - predict(d.lm.interact,newd=frame0))
meff</pre>
```

- ## [1] 0.08197142
 - Why might this be preferable to "setting things at their means/medians"?
 - It's essentially integrating over the sample's distribution of observed characteristics.
 - (And if the sample is a SRS from the population [or survey weights make it LOOK like it is], this will then get you the marginal effect on the population of interest)

Delta Method

- Note 1: We know that our vector of coefficients are asymptotically multivariate normal.
- Note 2: We can approximate the distribution of many (not just linear) functions of these coefficients using the delta method.
- Delta method says that you can approximate the distribution of $h(b_n)$ with $\nabla h(b)'\Omega \nabla h(b)$ Where Ω is the asymptotic variance of b.
- In practice, this means that we just need to be able to derive the function whose distribution we wish to approximate.

Trivial Example

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- Maybe we're interested in the ratio of the coefficient on ecthrpos to that of pubsupport.
- Call it $\frac{b_2}{b_3}$. The gradient is $(\frac{1}{b_3}, \frac{b_2}{b_2^2})$
- Estimate this easily in R with:

```
grad<-c(1/coef(d.lm)[3],coef(d.lm)[2]/coef(d.lm)[3]^2)
grad
## pubsupport
              ecthrpos
     334.0251 8046.4669
se<-sqrt(t(grad)%*%vcov(d.lm)[2:3,2:3]%*%grad)
est<-coef(d.lm)[2]/coef(d.lm)[3]
c(estimate=est,std.error=se)
## estimate.ecthrpos
                            std.error
##
            24.08941
                             35.32946
require(car,quietly=TRUE)
deltaMethod(d.lm, "ecthrpos/pubsupport")
##
                       Estimate
                                      SE
## ecthrpos/pubsupport 24.08941 35.54775
```

Linear Functions

- But for most "marginal effects", you don't need to use the delta method.
- Just remember your rules for variances.
- $\operatorname{var}(aX + bY) = a^2 \operatorname{var}(X) + b^2 \operatorname{var}(Y) + 2ab \operatorname{cov}(X, Y)$
- If you are just looking at changes with respect to a single variable, you can just multiply standard errors.
- That is, a change in a variable of 3 units means that the standard error for the marginal effect would be 3 times the standard error of the coefficient.
- This isn't what Clarify does, though.

Instrumental Variables

•
$$\rho = \frac{\text{Cov}(Y_i, Z_i)}{\text{Cov}(S_i, Z_i)} = \frac{\frac{\text{Cov}(Y_i, Z_i)}{\text{Var}(Z_i)}}{\frac{\text{Cov}(S_i, Z_i)}{\text{Var}(Z_i)}} = \frac{\text{Reduced form}}{\text{First stage}}$$

- If we have a perfect instrument, this will be unbiased.
- But bias is a function of both violation of exclusion restriction and of strength of first stage.
- 2SLS has finite sample bias. (Cyrus showed this, but didn't dwell on it)
- In particular, it can be shown that this bias "is": $\frac{\sigma_{\eta\xi}}{\sigma_\xi^2}\frac{1}{F+1}$

where η is the error in the structural model and ξ is the error in the first stage.

- With an irrelevant instrument (F = 0), the bias is equal to that of OLS (regression of Y on X).
- There are some bias corrections for this, we might talk about this next week.

Setup IV example

- $\bullet\,$ For our example with IV, we will start with AJR (2001) Colonial Origins of Comparative Development
- Treatment is average protection from expropriation
- Exogenous covariates are dummies for British/French colonial presence
- Instrument is settler mortality
- Outcome is log(GDP) in 1995

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```
require(foreign,quietly=TRUE)
dat <- read.dta("maketable5.dta")
dat <- subset(dat, baseco==1)</pre>
```

Estimate IV via 2SLS

```
require(AER,quietly=TRUE)
first <- lm(avexpr~logem4+f_brit+f_french,dat)</pre>
iv2sls<-ivreg(logpgp95~avexpr+f_brit+f_french,~logem4+f_brit+f_french,dat)
require(car)
linearHypothesis(first,"logem4",test="F")
## Linear hypothesis test
##
## Hypothesis:
## logem4 = 0
##
## Model 1: restricted model
## Model 2: avexpr ~ logem4 + f_brit + f_french
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F
                                           Pr(>F)
## 1
        61 116.983
## 2
        60 94.013 1
                         22.969 14.659 0.0003101 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Examine First Stage

```
summary(first)
##
## lm(formula = avexpr ~ logem4 + f_brit + f_french, data = dat)
##
## Residuals:
       Min
                1Q
                    Median
                                  3Q
                                         Max
## -2.98210 -0.86954 0.05616 0.86237 2.79411
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 8.7467 0.6904 12.669 < 2e-16 ***
              -0.5344
                          0.1396 -3.829 0.00031 ***
## logem4
## f_brit
                                 1.717 0.09109 .
               0.6293
                          0.3665
               0.0474
                          0.4295
## f_french
                                  0.110 0.91249
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 1.252 on 60 degrees of freedom
## Multiple R-squared: 0.3081, Adjusted R-squared: 0.2736
## F-statistic: 8.908 on 3 and 60 DF, p-value: 5.704e-05
```

Examine Output

```
summary(iv2sls)
##
## Call:
## ivreg(formula = logpgp95 ~ avexpr + f_brit + f_french | logem4 +
      f_brit + f_french, data = dat)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -2.2716 -0.7488 0.0728 0.7544 2.4004
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.3724 1.3880 0.989
                                            0.327
                                  4.953 6.28e-06 ***
## avexpr
                1.0779
                           0.2176
## f_brit
               -0.7777
                           0.3543 -2.195
                                            0.032 *
## f_french
               -0.1170
                           0.3548 -0.330
                                            0.743
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.043 on 60 degrees of freedom
## Multiple R-Squared: 0.04833, Adjusted R-squared: 0.0007476
## Wald test: 10.07 on 3 and 60 DF, p-value: 1.822e-05
```

Sensitivity Analysis

- Conley, Hansen and Rossi (2012)
- Suppose that the exclusion restriction does NOT hold, and there exists a direct effect from the instrument to the outcome.
- That is, the structural model is:

```
Y = X\beta + Z\gamma + \epsilon
```

- If γ is zero, the exclusion restriction holds (we're in a structural framework)
- We can assume a particular value of γ , take $\tilde{Y} = Y Z\gamma$ and estimate our model, gaining an estimate of β .
- This defines a sensitivity analysis on the exclusion restriction.

• Subject to an assumption about the support of γ , they suggest estimating in a grid over this domain, and then taking the union of the confidence intervals for each value of γ as the combined confidence interval (which will cover).

Sensitivity Analysis code

```
gamma <- seq(-1,1,.25)
ExclSens <- function(g) {
   newY <- dat$logpgp95 - g*dat$logem4
   coef(ivreg(newY~avexpr+f_brit+f_french,~logem4+f_brit+f_french,cbind(dat,newY)))[2]
}
sens.coefs <- sapply(gamma,ExclSens)
names(sens.coefs)<- round(gamma,3)
round(sens.coefs,3)

##   -1  -0.75  -0.5  -0.25      0      0.25      0.75      1
## -0.793 -0.326      0.142      0.610      1.078      1.546      2.013      2.481      2.949</pre>
```

More IV Stuff

- We're going to be looking at Ananat (2011) in AEJ
- This study looks at the effect of racial segregation on economic outcomes.
- Outcome: Poverty rate & Inequality (Gini index)
- Treatment: Segregation
- Instrument: "railroad division index"
- Main covariate of note: railroad length in a town
- I'm dichotomizing treatment and instrument for simplicity.
- And my outcomes are for the Black subsample

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```
require(foreign)
d<-read.dta("aej_maindata.dta")
d$herf_b<-with(d,ifelse(herf >= quantile(herf,.5),1,0))
d$dism1990_b<-with(d,ifelse(dism1990 >= quantile(dism1990,.5),1,0))
first.stage <- lm(dism1990~herf+lenper,d)
first.stage.b <- lm(dism1990_b~herf_b+lenper,d)
require(AER)
gini.iv <- ivreg(lngini_b~dism1990+lenper,~herf+lenper,d)
gini.iv.b <- ivreg(lngini_b~dism1990_b+lenper,~herf_b+lenper,d)
pov.iv <- ivreg(povrate_b~dism1990+lenper,~herf+lenper,d)
pov.iv.b <- ivreg(povrate_b~dism1990_b+lenper,~herf_b+lenper,d)</pre>
```

Base Results

```
round(summary(first.stage)$coefficients[2,],3)
##
     Estimate Std. Error
                             t value
                                       Pr(>|t|)
##
        0.357
                   0.081
                               4.395
                                           0.000
round(summary(first.stage.b)$coefficients[2,],3)
     Estimate Std. Error
                                       Pr(>|t|)
##
                             t value
##
        0.372
                   0.083
                               4.481
                                          0.000
round(summary(gini.iv)$coefficients[2,],3)
##
     Estimate Std. Error
                                       Pr(>|t|)
                             t value
##
        0.875
                   0.302
                               2.895
                                           0.005
round(summary(gini.iv.b)$coefficients[2,],3)
##
     Estimate Std. Error
                             t value
                                       Pr(>|t|)
##
        0.211
                   0.081
                               2.615
                                          0.010
round(summary(pov.iv)$coefficients[2,],3)
##
     Estimate Std. Error
                             t value
                                       Pr(>|t|)
##
        0.258
                   0.144
                               1.798
                                          0.075
round(summary(pov.iv.b)$coefficients[2,],3)
##
     Estimate Std. Error
                                       Pr(>|t|)
                             t value
##
        0.059
                   0.039
                               1.543
                                           0.125
```

Abadie's κ

- Recall from the lecture that we can use a weighting scheme to calculate statistics on the compliant population.
- $E[g(Y, D, X)|D_1 > D_0] = \frac{1}{p(D_1 > D_0)} E[\kappa g(Y, D, X)]$ $\kappa = 1 \frac{D_i(1 Z_i)}{p(Z_i = 0|X)} \frac{(1 D_i)Z_i}{p(Z_i = 1|X)}$ $E[\kappa|X] = E[D_1 D_0|X] = E[D|X, Z = 1] E[D|X, Z = 0]$

- Take $w_i = \frac{\kappa_i}{E[D_1 D_0|X_i]}$

- Use this in calculating any interesting statistics (means, variance, etc)
- This let's you explore the units composing your LATE.

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```
getKappaWt<-function(D,Z) {
   pz <- mean(Z)
   pcomp <- mean(D[Z==1]) - mean(D[Z==0])
   if(pcomp < 0) stop("Assuming p(D|Z) > .5")
   kappa <- 1 - D*(1-Z)/(1-pz) - (1-D)*Z/pz
   # Note that pcomp = mean(kappa)
   kappa / pcomp
}
w <- with(d,getKappaWt(D=dism1990_b,Z=herf_b))
varlist <- c("closeness","area1910","ctyliterate1920","hsdrop_b","manshr","ctymanuf_wkrs1920
samp.stats<-sapply(varlist,function(v) mean(d[,v],na.rm=TRUE))
comp.stats<-sapply(varlist,function(v) weighted.mean(d[,v],w,na.rm=TRUE))</pre>
```

Examine Complier Statistics

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -2.511 -2.429 2.470 1.000 2.470 2.470

rbind(sample=samp.stats,compliers=comp.stats)

## closeness area1910 ctyliterate1920 hsdrop_b manshr
## sample -362.4348 14626.43 0.9585012 0.2516300 0.1891766
## compliers -299.1428 18012.56 0.9514523 0.2423754 0.2109807
## ctymanuf_wkrs1920 ngov62
## sample 0.4618666 55.55072
## compliers 0.4266065 83.65072
```