

MAT1856/APM466 Assignment 1

Yiqu Ding, Student #: 1004913329

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Fundamental Questions - 25 points

1.
 - (a) Governments issue bonds and not simply print more money because they want to control the total money supply and not to inflation.
 - (b) Suppose the bank plan to increase interest rates recently to attract client deposits, this will cause the yield to rise in a short period, but it is almost certain that as time goes by, the bank has had enough increased deposits and decide to decrease the rate again and the long-term yield curve will increase less rapidly.
 - (c) Quantitative easing is a monetary policy that the US Fed used during the COVID-19 Pandemic. They purchased long-term bonds from banks across the US to increase their money supply and lower the interest rate(risk-free rate) to stimulate the investment market and thus boosting the economy.
2. I am picking 10 coupons with the first one maturing in less than 6 months, the second one maturing at least 6 months later but sooner than 1 year, the third one matures in at least a year but less than 1 year plus 6 months, etc. This way my first bond will have 1 payment left, the second one has 2 payments left and etc. I can treat my first bond(maturing in less than 6 months) as a zero coupon bond because it has no coupon payment left, and use this to calculate the yield of the first coupon, then I go on and treat the second half of my second bond as a zero coupon again, I continue this process in order to get my 5 year curve.
3. The eigenvalues and eigenvectors of the covariance matrix of stochastic processes are called principle components. Just like how its name suggests, the principle components of the covariance matrix contains the most information carried in the model built, in other words we can obtain the most important results from a very complex model by only viewing its principle components. The first eigenvector indicates the correlation between curves, it captures the curve dynamics. The second eigenvector represents the steepening of the curve and the third vector represents the level of change in convexity. After that it is mainly noise.

Empirical Questions - 75 points

4. Please see the reference for the source of codes.
 - (a) Please see 1 for the plot of the yield curve.
 - (b) Please see 1 for the plot of the spots curve.
 - (c) Please see 2 for the plot of the forward curve.
5. Please see 1 and 6.

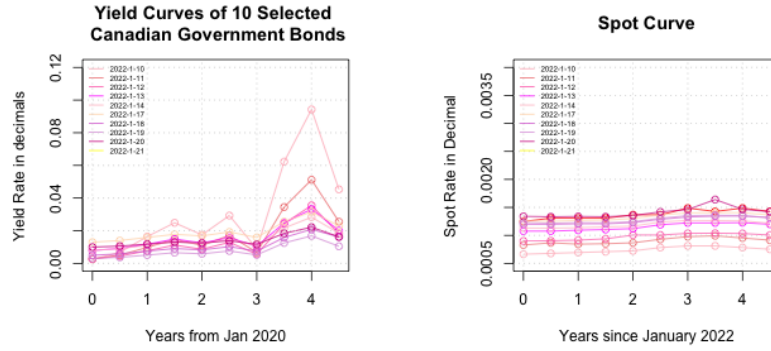


Figure 1: Q4(a) and (b)

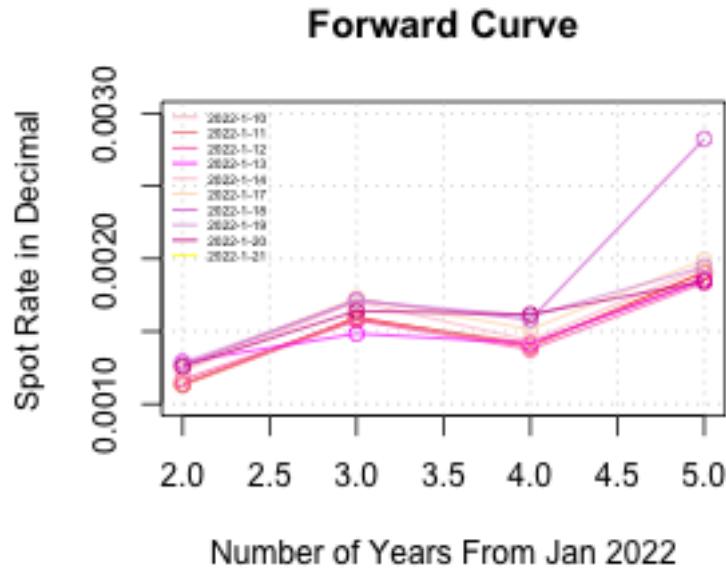


Figure 2: Q4(c)

6. Please see 3 for the eigenvectors. The corresponding eigen values are $(1.646460, 2.716362e-02, 1.530982e-03, 5.252046e-04, 5.215349e-05)$ and $(5.446583e-01, 3.203774e-02, 1.915300e-17, 4.276895e-18, 3.604313e-18, 1.918414e-18, 1.353332e-18, 4.562149e-19, 4.327970e-19, -1.082219e-16)$. We observe the largest eigen vectors have similar entries for the log return and for the forward rate, and are all positive, as the first principle component which captures the most of the motion in the market, this means the two rates are positively correlated.

References and GitHub Link to Code

Please refer to <https://github.com/dding33/Fixed-Income-Market-Yield-Analysis> for a reproducible repository. The data used in the analysis was scraped at <https://markets.businessinsider.com/>.

	log_return1	log_return2	log_return3	log_return4	log_return5
log_return1	0.92	0.66	0.30	0.30	0.19
log_return2	0.66	0.49	0.23	0.22	0.15
log_return3	0.30	0.23	0.11	0.11	0.07
log_return4	0.30	0.22	0.11	0.10	0.07
log_return5	0.19	0.15	0.07	0.07	0.05

Table 1: Log Return Covariance Matrix

	fwd1	fwd2	fwd3	fwd4	fwd5	fwd6	fwd7	fwd8	fwd9	fwd10
fwd1	0.07	0.06	0.06	0.07	0.04	0.07	0.07	0.08	0.05	0.03
fwd2	0.06	0.06	0.06	0.06	0.03	0.07	0.06	0.07	0.04	0.03
fwd3	0.06	0.06	0.06	0.06	0.03	0.07	0.06	0.07	0.04	0.03
fwd4	0.07	0.06	0.06	0.06	0.04	0.07	0.06	0.07	0.04	0.03
fwd5	0.04	0.03	0.03	0.04	0.02	0.04	0.03	0.05	0.02	0.01
fwd6	0.07	0.07	0.07	0.07	0.04	0.08	0.07	0.08	0.05	0.04
fwd7	0.07	0.06	0.06	0.06	0.03	0.07	0.06	0.07	0.04	0.03
fwd8	0.08	0.07	0.07	0.07	0.05	0.08	0.07	0.11	0.05	0.03
fwd9	0.05	0.04	0.04	0.04	0.02	0.05	0.04	0.05	0.03	0.02
fwd10	0.03	0.03	0.03	0.03	0.01	0.04	0.03	0.03	0.02	0.02

Table 2: Forward Covariance Matrix

	1	2	3	4	5
1	0.74	0.59	0.20	-0.24	-0.03
2	0.54	-0.28	-0.32	0.70	0.18
3	0.25	-0.52	0.43	-0.02	-0.70
4	0.25	-0.34	-0.66	-0.62	-0.04
5	0.16	-0.44	0.48	-0.26	0.69

	1	2	3	4	5	6	7	8	9	10
1	-0.36	-0.10	0.71	0.00	0.00	0.00	0.00	0.00	0.00	-0.60
2	-0.33	-0.16	0.43	0.31	-0.04	-0.11	0.10	0.11	0.00	0.74
3	-0.32	-0.19	-0.04	-0.54	-0.25	0.43	-0.20	-0.14	-0.48	0.17
4	-0.34	-0.05	-0.17	0.25	0.55	0.14	-0.40	-0.53	0.15	0.01
5	-0.20	0.34	-0.02	-0.26	0.62	-0.21	0.38	0.16	-0.42	0.03
6	-0.38	-0.09	-0.30	0.15	-0.08	0.46	0.65	0.04	0.27	-0.11
7	-0.33	-0.13	-0.13	-0.56	0.03	-0.36	-0.13	0.21	0.59	0.07
8	-0.41	0.75	-0.13	0.19	-0.36	-0.04	-0.26	0.12	-0.02	-0.04
9	-0.24	-0.27	-0.28	0.14	-0.30	-0.62	0.19	-0.38	-0.30	-0.14
10	-0.17	-0.38	-0.28	0.30	0.14	0.01	-0.31	0.67	-0.24	-0.17

Table 3: Eigenvectors for the Yield Cov Matrix and for the Forwards Matrix