

Probabilistic Logic

Nilsson, *Artificial Intelligence*, '86

- Suppose we have set β of logical sentences, where sentence i has the probability π_i (vector Π). The first sentence is a tautology and has the probability 1. $|\beta| = L-1$.
- We want to find the probability of sentence S given β and Π . This is an entailment problem.
- Given β and S , we use a semantic tree to find all sets of possible worlds that are possible. There are K sets of possible worlds. A sentence is either true or false in a given set of worlds.
- Let V be a $L \times K$ matrix – rows representing each sentence and columns representing a set of worlds. A position in a matrix is 1 if the sentence for that row is true in the world for that column, and 0 otherwise.
- By omitting the last row of V (the row for sentence S) we obtain V' . Using V' , we can create a convex hull to determine bounds on the probability of S (i.e. the probability of S is a any point in the hull based on the probabilities assigned to the sets of worlds). Linear programming can be used for this.
- Nilsson presents two techniques to approximate the probability of the entailed sentence. One method uses the projection of the vector associated with S from V projected onto the subspace defined by the row vectors of V' . Another method find the probability for sentence S that minimizes entropy. However, these techniques are only appropriate for very small matrices.
- For larger matrices, Nilsson creates a systematic way to create a smaller matrix, V^* , that approximates V' . This is done by changing values in the vector Π . to either 0 or 1 and checking its consistency. If consistent, the column is added to V^* . The more columns that are added, the more V^* comes to resemble V' .