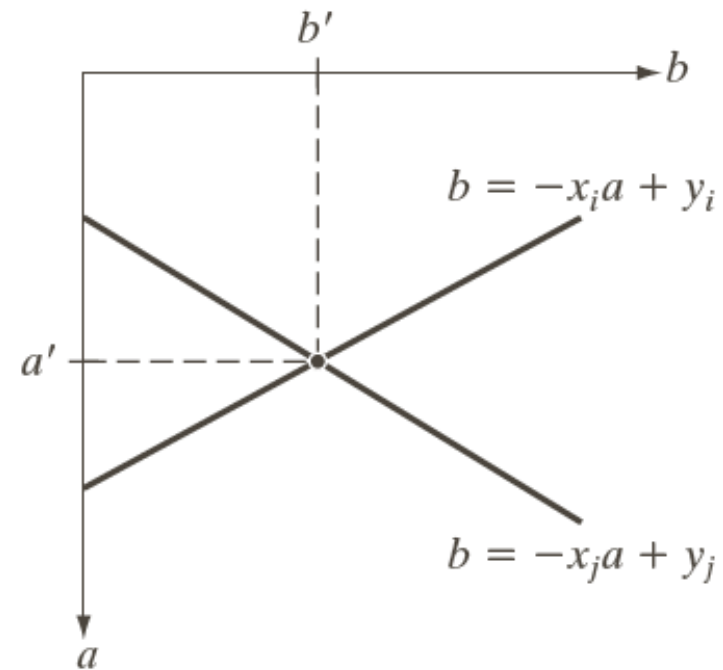
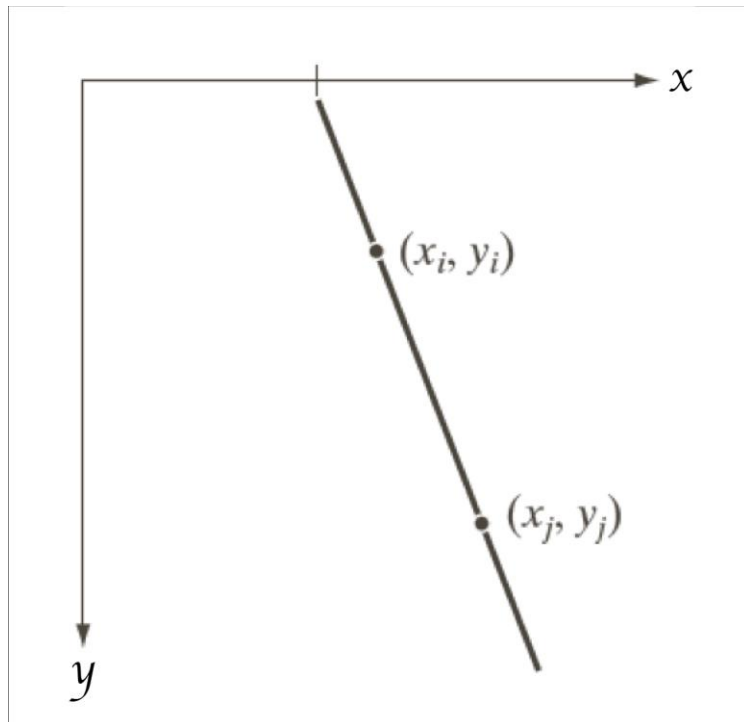


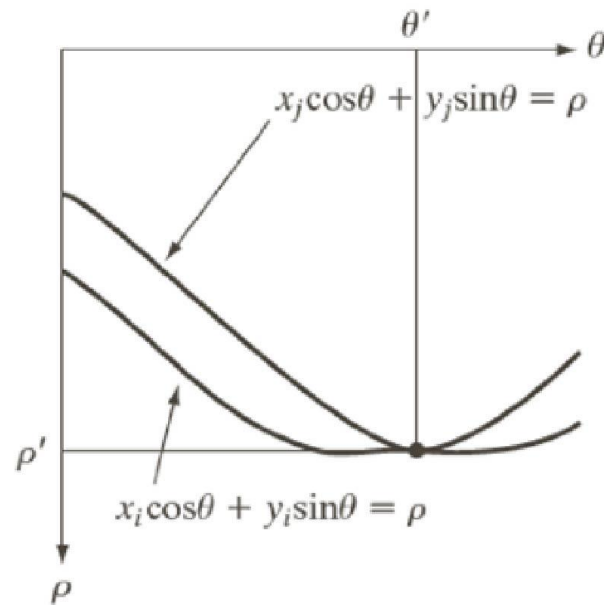
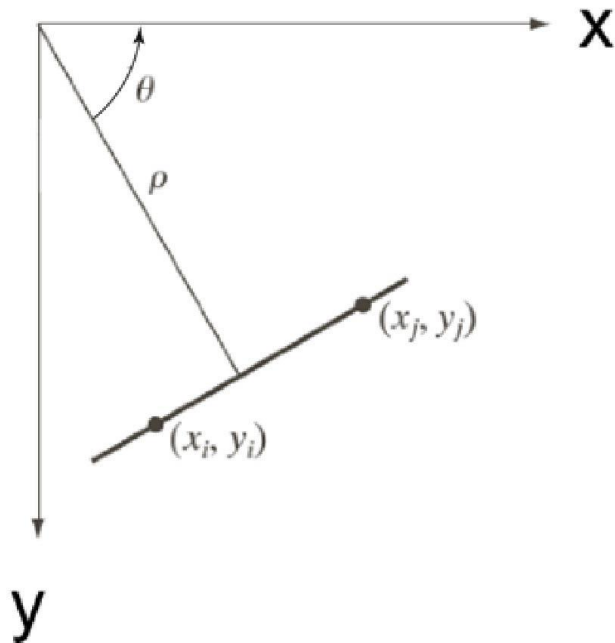
Line Detection

Sung Soo Hwang

- The concept of Hough transform
 - $y = ax + b \rightarrow b = -ax + y$
 - Find all combinations of (a, b) for each edge pixel
 - A combination of (a, b) which is used multiple times can be a line of an input image

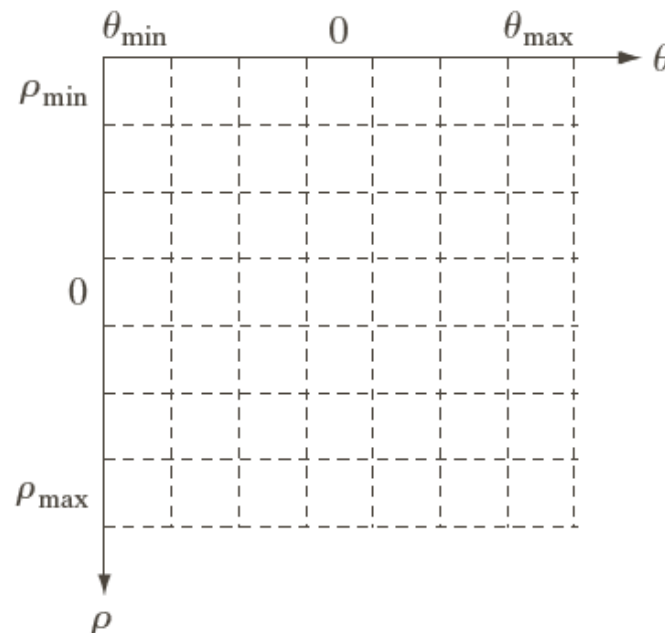


- The concept of Hough transform
 - a becomes infinity as the line approaches the vertical direction
 - Use $\rho\theta$ representation instead
 - $x\cos\theta + y\sin\theta = \rho$



Hough Transform

- Algorithm
 1. obtain a binary edge image
 2. specify subdivision in the $\rho\theta$ – plane
 3. Examine the counts of the accumulator cells for high pixel concentrations
 4. Examine the relationship (connectivity) between pixels in a chosen cell



- Circle detection
 - Hough transform is applicable to any function of the form $g(v, c)=0$, where v is a vector of coordinates and c is a vector of coefficients
 - Points lying on the circle
 - $(x - c_1)^2 + (y - c_2)^2 = c_3$
 - The result is a 3D parameter space

■ Houghlines

```
int main() {
    Mat image, edge, result;
    float rho, theta, a, b, x0, y0;
    Point p1, p2;
    vector<Vec2f> lines;
    image = imread("chess_pattern.png");
    result = image.clone();

    cvtColor(image, image, CV_BGR2GRAY);
    Canny(image, edge, 50, 200, 3);

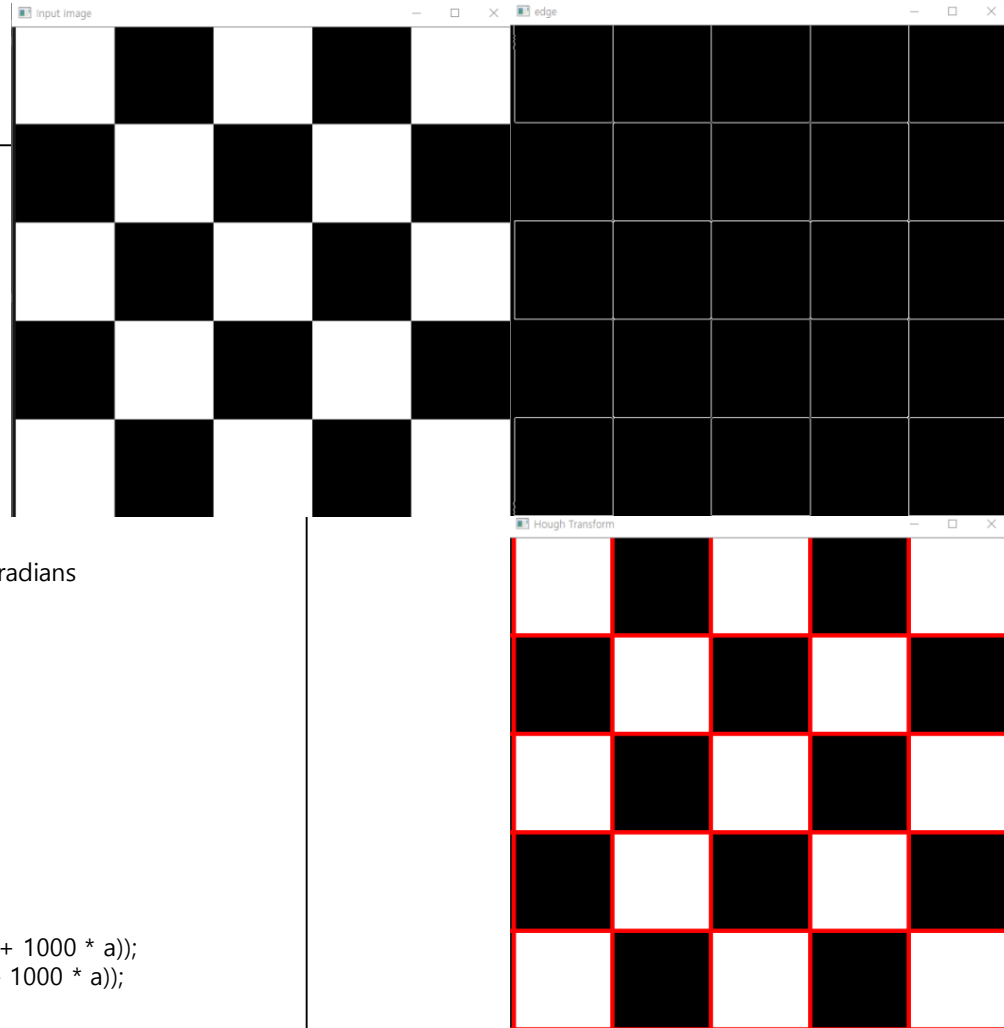
    //applying Hough Transform to find lines in the image
    //edge: input Mat, lines: output vector of lines
    //1: (rho) distance resolution of the accumulator in pixels
    //CV_PI/180: (theta) angle resolution of the accumulator in radians
    //150: (threshold) accumulator threshold parameter
    HoughLines(edge, lines, 1, CV_PI / 180, 150);

    for (int i = 0; i < lines.size(); i++) {
        rho = lines[i][0];
        theta = lines[i][1];
        a = cos(theta);
        b = sin(theta);

        x0 = a * rho;
        y0 = b * rho;

        p1 = Point(cvRound(x0 + 1000 * (-b)), cvRound(y0 + 1000 * a));
        p2 = Point(cvRound(x0 - 1000 * (-b)), cvRound(y0 - 1000 * a));

        line(result, p1, p2, Scalar(0, 0, 255), 3, 8);
    }
    imshow("Input image", image);
    imshow("edge", edge);
    imshow("Hough Transform", result);
    waitKey(0);
}
```



■ Houghlinesp

```
int main() {
    Mat image, edge, result;
    float rho, theta, a, b, x0, y0;
    Point p1, p2;
    vector<Vec4i> lines;

    image = imread("chess_pattern.png");
    result = image.clone();
    cvtColor(image, image, CV_BGR2GRAY);
    Canny(image, edge, 50, 200, 3);
    //edge: input Mat, lines: output vector of lines
    //1: (rho) distance resolution of the accumulator in pixels
    //CV_PI/180: (theta) angle resolution of the accumulator in radians
    //50: (threshold) accumulator threshold parameter
    //10: (minLineLength) minimum line length.
    //300: (maxLineGap) Maximum allowed gap between points on the
    same line to link them
    HoughLinesP(edge, lines, 1, CV_PI / 180, 50, 10, 300);

    for (int i = 0; i < lines.size(); i++) {
        Vec4i l = lines[i];
        line(result, Point(l[0], l[1]), Point(l[2], l[3]), Scalar(0, 0, 255), 3, 8);
    }

    imshow("Input image", image);
    imshow("edge", edge);
    imshow("Hough Transform", result);
    waitKey(0);
}
```

