

# Lecture #3: Recap of Function Evaluation; Control

*Functions can only manipulate their local environment.*

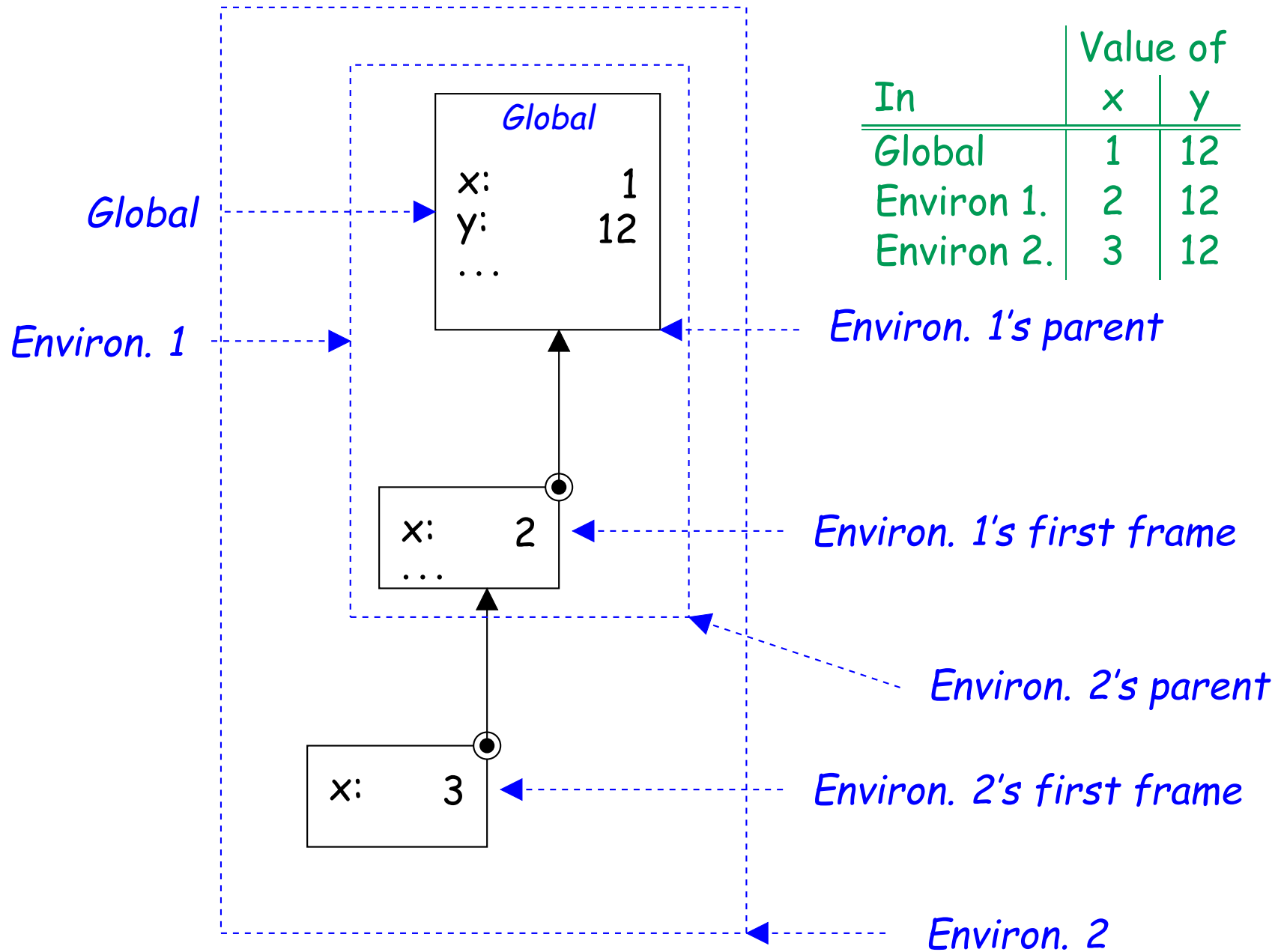
# Announcements

- Labs 1 and 2 due Tuesday (at 11:59PM).
- Homework 1 due Thursday.
- Orientations starting: lab orientations are Mondays, discussion orientations Wednesdays. These are recorded.
- Lab party on Monday, homework party on Tuesday. See Piazza @151.
- Conceptual office hours starting this week. See Piazza @174.
- Ask questions on the [Piazza thread for today's lecture](#) (@155).

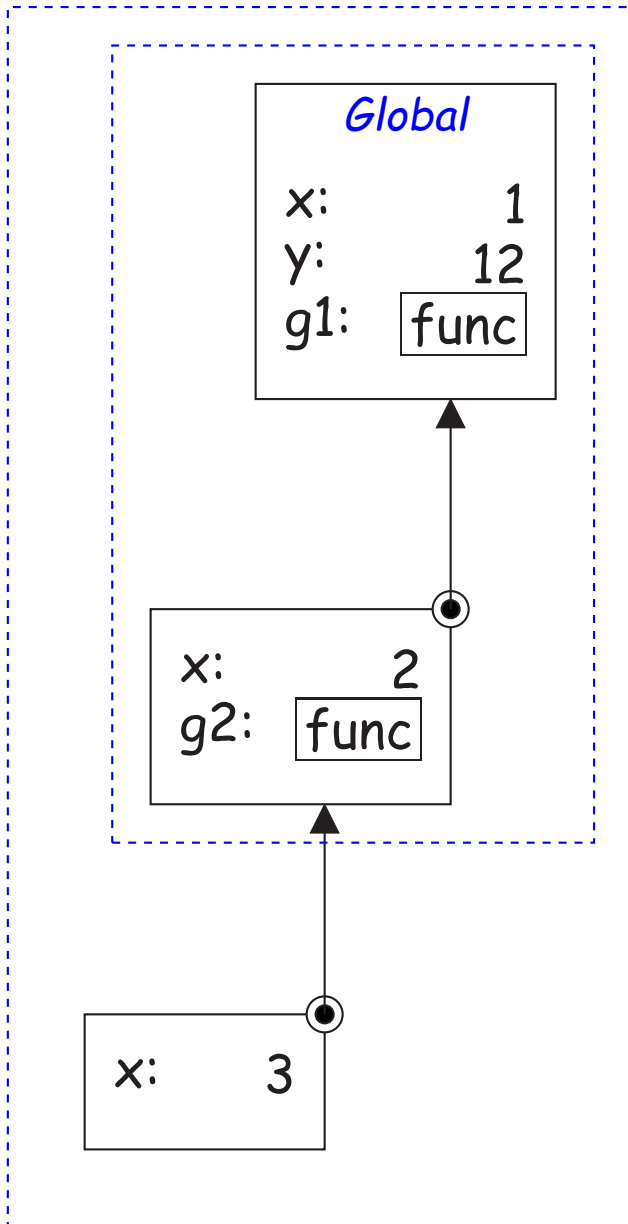
# Summary: Environments

- *Environments* map names to values.
- They consist of chains of *environment frames*.
- An environment is either a *global frame* or a first (local) frame chained to a *parent environment* (which is itself either a global frame or ...).
- We say that a name is *bound to* a value in a frame.
- The *value (or meaning) of a name* in an environment is the value it is bound to in the first frame, if there is one, ...
- ...or if not, the meaning of the name in the parent environment (recursively).
- Every expression and statement is evaluated (executed) in an environment, which determines the meaning of its names.
- Expressions and subexpressions (pieces of an expression) are evaluated in the same environment as the statement or expression containing them.

# A Sample Environment Chain



# Creating the Sample Environment Chain



Executing the following code will result in the environment on the left when execution reaches the comment.

```
x = 1
y = 12
→ def g1(x):
    def g2(x):
        # Stop here
        print(x)
        g2(x + 1)
    g1(2)
```

global Frames

x  $\ll$

y  $\ll$

g1  $\ll$

func g1(x)  
[parent = global]

combination of function, code,  
parent environment  $\rightarrow$  closure  
闭包

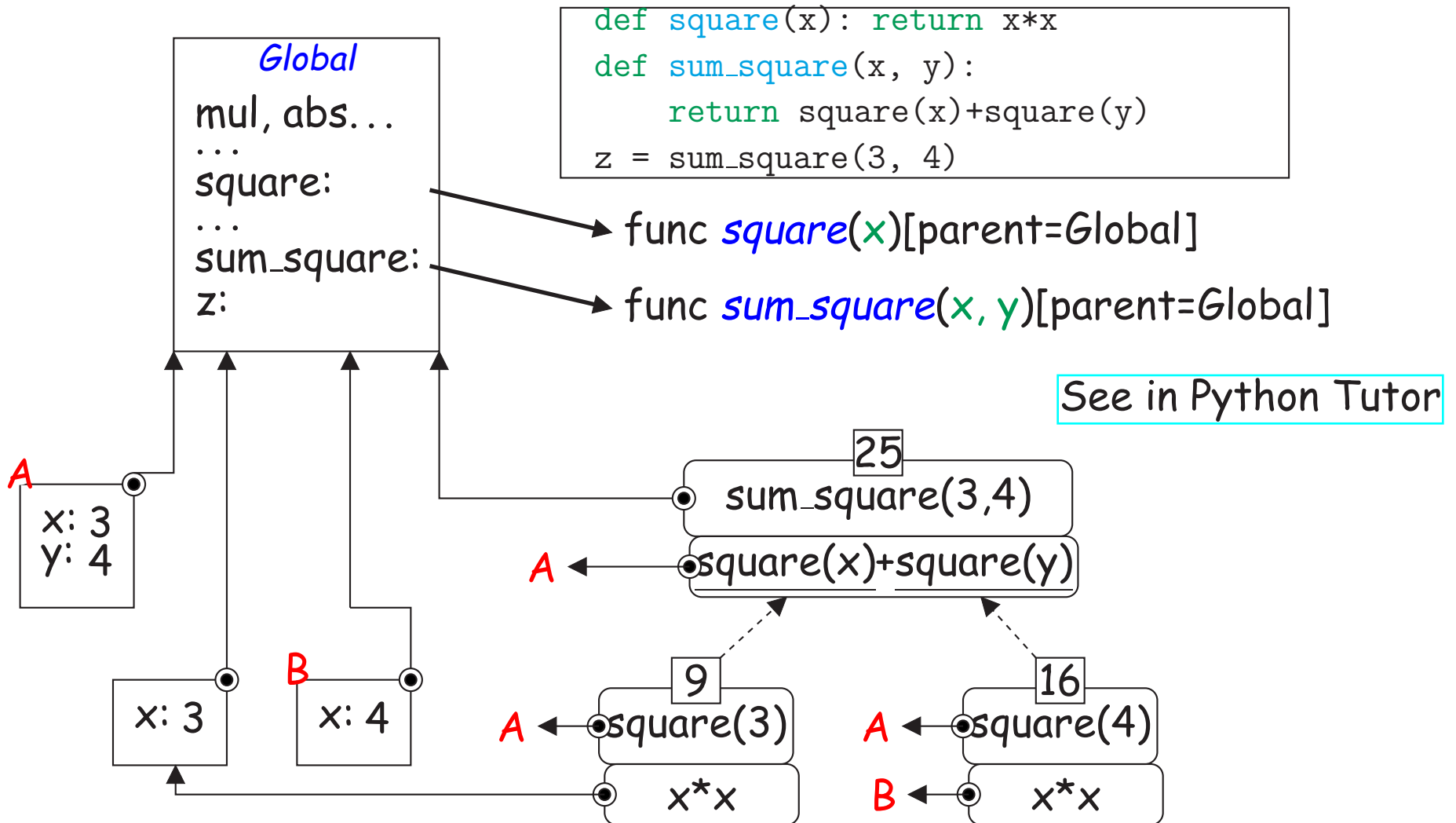
The call to print is executed in this environment. Continuing from the comment, the program would print 3.

[Execute in Python tutor](#)

# Environments: Binding and Evaluation

- *Assigning* to a variable binds a value to it in (for now) the first frame of the environment in which the assignment is executed.
- *Def statements* bind a name to a function value in the first frame of the environment in which the *def* statement is executed.
- This new function value contains a link to this same environment.
- *Calling* a user-defined function creates a new local environment frame that binds the function's *formal parameters* to the operand values (*actual parameters*) in the call.
- This new local frame is attached to an existing (parent) frame that is taken from the function value that is called, forming a new local environment in which the function's body is evaluated.

# Example: Evaluation of a Call: `sum_square(3,4)`



# What Does This Do (And Why)?

```
def id(x):  
    return x  
print(id(id)(id(13)))
```

Execute this



# Answer

```
def id(x):  
    return x  
print(id(id)(id(13)))
```

- We'll denote the user-defined function value created by `def id():...` by the shorthand `id`.
- Evaluation proceeds like this:

`id(id)(id(13))`

$\Rightarrow$  `id ( id )( id ( 13 ) )`

$\Rightarrow$  `id ( id ( 13 ) )`

*(because first `id` call returns its argument).*

$\Rightarrow$  `id ( 13 )`

*(because inner `id` call returns its argument).*

$\Rightarrow$  `13`

*(because call to returned `id` value returns its argument).*

- **Important:** There is nothing new on this slide! Everything follows from what you've seen so far.

# Nested Functions

- In lecture #2, I had this example:

```
def incr(n):
    def f(x):
        return n + x
    return f
```

incr(5)(6)

- We evaluated the argument to **print** by substitution:

incr(5)  $\implies$  def f(x): return 5 + x  
return f  $\implies$  func f(x): 5 + x

incr(5)(6)  $\implies$  func f(x): 5 + x(6)  $\implies$  5 + 6  $\implies$  11

- So how does this work with environments?

Global Frame

incr  $\hookrightarrow$  func incr(n) [parent = Global]

f1: incr [parent = Global]

n = 5  
f1  $\hookrightarrow$  func f(x) [parent = f1]  
Return value  $\hookrightarrow$

f2: f [parent = f1]

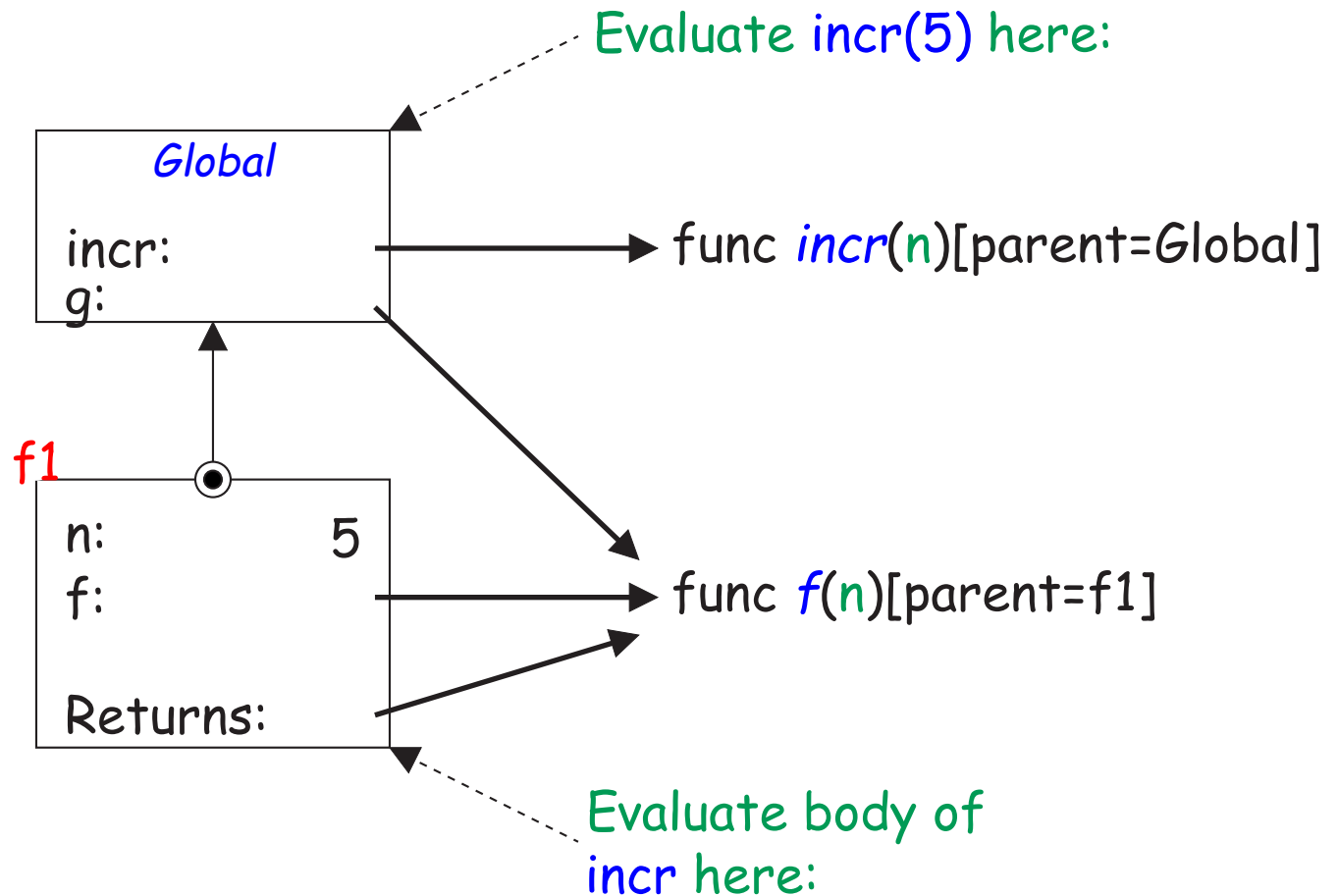
x = 6

Return value 11

# Environments for incr (I)

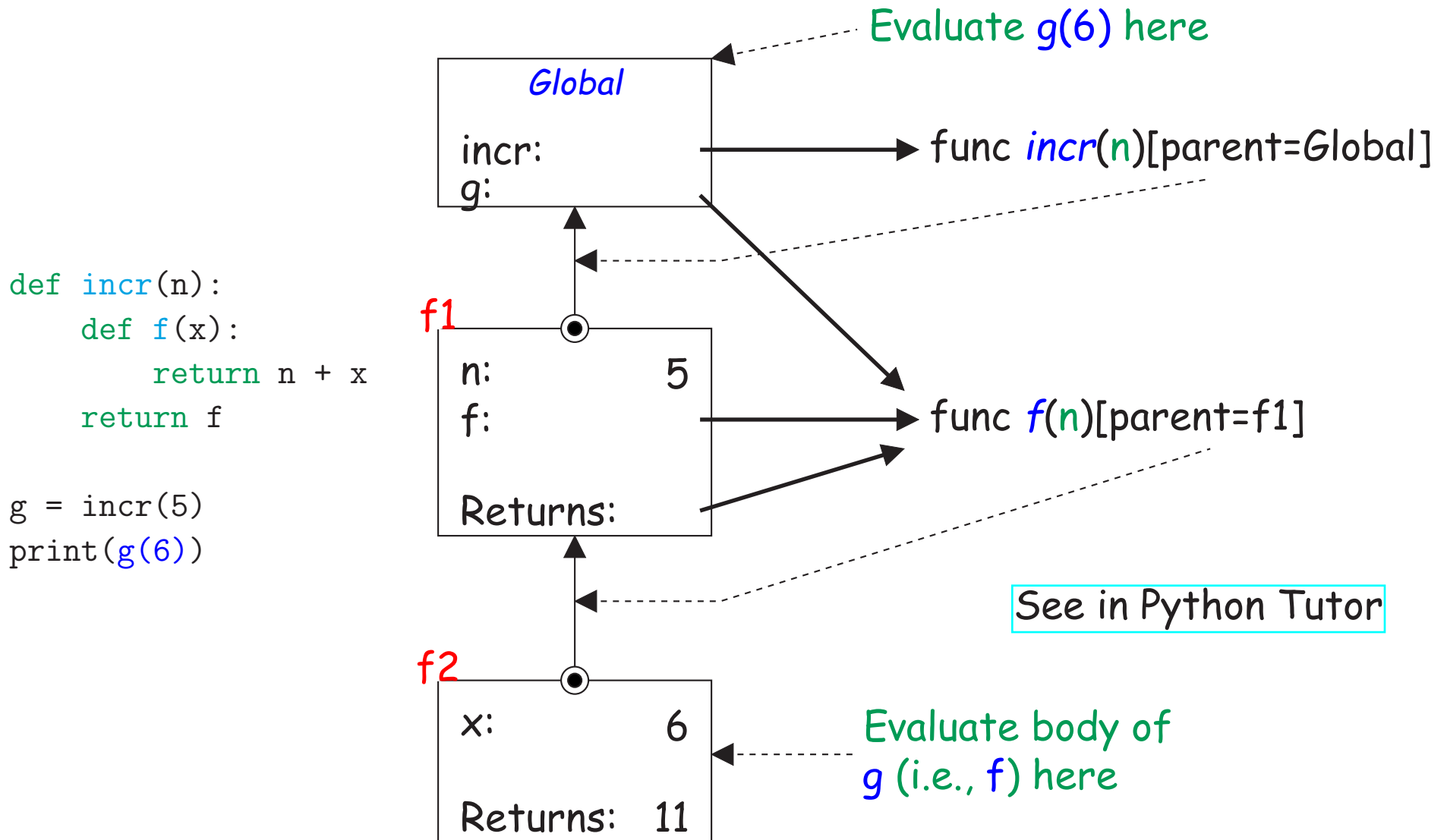
```
def incr(n):  
    def f(x):  
        return n + x  
    return f
```

```
# Break incr(5)(6)  
# into two steps:  
g = incr(5)  
print(g(6))
```



- The parent points of `incr` is *Global* because the definition of `incr` was evaluated in the global environment.
- The parent pointer for the value of `g` (returned by `incr(5)`) is *f1*, not *Global*, because the definition of `f` was evaluated in *f1*.

# Environments for incr (II)



- **f2** gets its parent pointer from **g**'s value, since it is the local frame for evaluating a call to **g**. (Same rule for **f1**.)

# Recap

- Every expression or statement is evaluated in an environment—a sequence of frames.
- Every assignment to a variable and every **def** binds (or changes the binding) of its variable or defined name in the first frame of this environment.
- Every frame (except the global frame) is linked to a parent frame.
- Every function *value* is linked to the environment in which its **def** is evaluated.
- Every function *call* creates a new local frame that is linked to the same frame as the function value being called.
- The total effect is the same as for the substitution model, but we can also handle changes in the values of variables.
- Looking ahead, there are still two constructs—*global* and *nonlocal*—that will require additions.
- But what we have here basically covers how names work in most of Python.

## New Topic: Control

- The expressions we've seen evaluate all of their operands in the order written.
- While there are very clever ways to do everything with just this [challenge!], it's generally clearer to introduce constructs that *control* the order in which their components execute.
- A *control expression* evaluates some or all of its operands in an order depending on the kind of expression, and typically on the values of those operands.
- A *statement* is a construct that produces no value, but is used solely for its side effects.
- A *control statement* is a statement that, like a control expression, evaluates some or all of its operands, etc.
- We typically speak of statements being *executed* rather than evaluated, but the two concepts are essentially the same, apart from the question of a value.

# Conditional Expressions (I)

- The most common kind of control is *conditional evaluation* (or *execution*).

- In Python, to evaluate

*TruePart* **if** *Condition* **else** *FalsePart*

- First evaluate *Condition*.
- If the result is a "*true value*," evaluate *TruePart*; its value is then the value of the whole expression.
- Otherwise, evaluate *FalsePart*; its value is then the value of the whole expression.

- **Example:**

If x is 2:

---

$1 / x$  if  $x \neq 0$  else 1  
 $1 / x$  if  $\boxed{2} \neq 0$  else 1  
 $\Rightarrow 1 / x$  if  $\boxed{\text{True}}$  else 1  
 $\Rightarrow 1 / x$   
 $\Rightarrow \boxed{1} / \boxed{2}$   
 $\Rightarrow \boxed{0.5}$

If x is 0:

---

$1 / x$  if  $x \neq 0$  else 1  
 $1 / x$  if  $0 \neq 0$  else 1  
 $\Rightarrow 1 / x$  if  $\boxed{\text{False}}$  else 1  
 $\Rightarrow 1$   
 $\Rightarrow \boxed{1}$

# "True Values"

- Conditions in conditional constructs can have any value, not just True or False.
- For convenience, Python treats a number of values as indicating "false":
  - False
  - None
  - 0
  - Empty strings, sets, lists, tuples, and dictionaries.
- All else is a "true value" by default.
- For example:

`13 if 0 else 5 == 13 if [] else 5 == 5`

.



## Conditional Expressions (II)

- To evaluate *Left* and *Right*
  - Evaluate *Left*.
  - If it is a false value, that becomes the value of the whole expression.
  - Otherwise the value of the expression is that of *Right*.
- This is an example of something called "short-circuit evaluation." 短路原则.
- For example,
  - $5 \text{ and } \text{"Hello"} \Rightarrow \boxed{\text{"Hello"}} .$
  - $[] \text{ and } 1 / 0 \Rightarrow \boxed{[]} .$  (1/0 is not evaluated.)

# Conditional Expressions (III)

- To evaluate  
*Left or Right*
  - Evaluate *Left*.
  - If it is a true value, that becomes the value of the whole expression.
  - Otherwise the value of the expression is that of *Right*.
- Another example of "*short-circuit evaluation*."
- For example,

$5 \text{ or } \text{"Hello"} \implies \boxed{5} .$

$[] \text{ or } \text{"Hello"} \implies \boxed{\text{"Hello"}} .$

$[1, 2] \text{ or } 1 / 0 \implies \boxed{[1, 2]} .$

$[] \text{ or } 1 / 0 \implies \boxed{\text{ERROR}} .$

# Conditional Statement

- Finally, this all comes in statement form:

```
if Condition1:  
    Statements1  
elif Condition2:  
    Statements2  
...  
else:  
    Statementsn
```

- Execute (only) *Statements*<sub>1</sub> if *Condition*<sub>1</sub> evaluates to a true value.
- Otherwise execute *Statements*<sub>2</sub> if *Condition*<sub>2</sub> evaluates to a true value (**elif**s are optional parts).
- ...
- Otherwise execute *Statements*<sub>n</sub> (**else** is an optional part).

# Examples

## # Alternative Definitions

```
def signum(x):  
    if x > 0:  
        return 1  
    elif x == 0:  
        return 0  
    else:  
        return -1
```

```
def max(x, y):  
    if x > y:  
        return x  
    else:  
        return y
```

```
def min(x, y):  
    if x < y:  
        return x  
    return y
```

```
def signum(x):  
    return 1 if x > 0 else 0 if x == 0 else -1
```

```
def max(x, y):  
    return x if x > y else y
```

```
def min(x, y):  
    return x if x < y else y
```

## Side Trip: Suites and Sequences

- The sequence of indented statements after the colon in

```
if x >= 0:
    print(x)
    y = x
```

is called a *suite*. In effect it is a single statement formed from two.

- Executing the suite itself means executing each of its statements in sequence (unless one of them says otherwise).
- Every statement in the suite has the same indentation, and it ends at the next statement that is indented to a previous level:

```
x = 0
if x > 1:
    print(">1")
    if x < 6:
        print("<6")
    print("x =", x)
# Prints nothing
```

```
x = 0
if x > 1:
    print(">1")
    if x < 6:
        print("<6")
    print("x =", x)
# Prints "x = 0"
```

- Every language has some way of *grouping* statements like this.
- Few do it like Python. (Interesting story behind this.)

# Iteration

- Suppose you would like to compute  $1^2 + 2^2 + \dots + 100^2$ .
- (Yes, I know there is a formula for this. Humor me.)
- You'd probably prefer not to write

```
print(1 ** 2 + 2 ** 2 + ... + 100 ** 2)
```

- Actually, we already know enough to do this:

```
def add_sq(accum, k, n):  
    """Return ACCUM + K ** 2 + (K+1)**2 + ... + N**2."""  
    if k > n:  
        return accum  
    else:  
        return add_sq(accum + k ** 2, k + 1, n)  
print(add_sq(0, 1, 100))
```

- Go ahead: [try it in on a small case in the Python Tutor](#).
- This is an example of a *recursive function*. We'll come back to such functions later in the course.

# While Statements

- Usually, though, programmers deal with problems like this summation using some kind of *looping construct*, which explicitly executes statements repeatedly.
- The **while** statement gives us *indefinite repetition*, meaning repetition until some condition is met (or as long as some condition is met). *can't tell how many times it's going to execute*
- For our example, (also see a small case in the Python Tutor):

```
accum = 0
k = 1
n = 100
while k <= n:
    accum = accum + k ** 2
    k += 1    # Another way to write k = k + 1
print(accum)
```

- Meaning of the **while** loop:
  - A. Test the *loop condition* (here,  $k \leq n$ ).
  - B. If it's true, execute the suite that follows (the *loop body*), and then repeat from step A.
  - C. Otherwise, end the loop (and continue to the print call).

## Example: Finding Prime Factors

- A *prime number* is an integer greater than 1 whose only factors are 1 and the number itself (e.g., 3, 5, 7, 11).
- So how do make this function fulfill its comment?

```
def is_prime(n):  
    """Return True iff N is prime."""  
    return n > 1 and smallest_factor(n) == n
```

```
def smallest_factor(n):  
    """Returns the smallest value k>1 that evenly divides N."""  
    ???
```

```
def print_factors(n):  
    """Print the prime factors of N."""  
    ???
```

- Try filling these in. (See Demo and also 03.py).