# 6elen018w tutorial3 2025 code

October 31, 2024

### 6ELEN018W - Tutorial 3 2025 Solutions

```
[40]: from sympy import *
from roboticstoolbox import *
from spatialmath.base import *
import numpy as np
```

#### Exercise 1

```
[53]: q1, q2, q3, q4, a1, a2, a3, a4 = symbols('q1, q2, q3, q4, a1, a2, a3, a4')

R = trot2(q1)@trans12(a1, 0)@trot2(q2)@trans12(a2, 0)@trot2(q3)@trans12(a3, u \( \doldow 0 \))@trot2(q4)@trans12(a4, 0)

simplify(R)
```

#### Exercise 2

```
[42]: import math
      def ex2(q1, q2, a1, a2):
          r1 = np.array([[cos(q1), -sin(q1), 0],
                             [\sin(q1), \cos(q1), 0],
                              [0,
                                       Ο,
                                                 1]])
          t1 = np.array([[1, 0, a1],
                             [0, 1, 0],
                             [0, 0, 1]])
          r2 = np.array([[cos(q2), -sin(q2), 0],
                             [\sin(q2), \cos(q2), 0],
                             [0, 0, 1]])
          t2 = np.array([[1, 0, a2],
                             [0, 1, 0],
                             [0, 0, 1]])
          return r1@t1@r2@t2
```

```
# calling the function
      print(ex2(math.pi, math.pi/2, 2, 3))
      # toolbox equivalent
      trot2(math.pi)@transl2(2,0)@trot2(math.pi/2)@transl2(3,0)
     [[-1.83697019872103e-16 1.000000000000 -2.0000000000000]
      [-1.0000000000000 -1.83697019872103e-16 -3.000000000000000]
      [0 0 1]]
[42]: array([[-1.8369702e-16, 1.0000000e+00, -2.0000000e+00],
             [-1.0000000e+00, -1.8369702e-16, -3.0000000e+00],
             [ 0.0000000e+00, 0.0000000e+00, 1.0000000e+00]])
[43]: def end_effector():
          tr = ex2(math.pi, math.pi/2, 2, 3)
          print(tr[0,2], tr[1,2])
      # calling the function
      end_effector()
     -2.0000000000000 -3.00000000000000
     Exercise 3
[44]: T = trot2(math.pi/2)@trans12(2,0)@trot2(math.pi)@trans12(3,0)@trot2(math.
       →pi)@trans12(4,0)
      T[0,2], T[1,2]
[44]: (7.960204194457794e-16, 3.0)
     Exercise 4
[45]: def ex4(q1, q2, a1, a2):
          # From equation (8) in the lecture slides
          J = [[-a1*sin(q1)-a2*sin(q1+q2), -a2*sin(q1+q2)],
               [a1*cos(q1)+a2*cos(q1+q2), a2*cos(q1+q2)]]
          return J
      # calling the function with desired angular velocities
      q1dot = 4
      q2dot = 5
      ex4(math.pi/2, math.pi/4, 2, 3)@np.array([q1dot, q2dot])
[45]: array([-27.0918830920368, -19.0918830920368], dtype=object)
```

#### Exercise 5

[4.000000000000001, 5.00000000000001]

## Exercise 6

```
[47]: theta = Symbol('theta')
    a = Symbol('a')

e1 = trot2(theta)@trans12(a, 0)
    e2 = trans12(a, 0)@trot2(theta)
    print(e1)
    print(e2)

[[cos(theta) -sin(theta) a*cos(theta)]
    [sin(theta) cos(theta) a*sin(theta)]
    [0 0 1]]

[[cos(theta) -sin(theta) a]
    [sin(theta) cos(theta) 0]
    [0 0 1]]
```

### Exercise 7

```
[74]: import numpy as np
from sympy import *

t = Symbol('t')
a1, a2 = symbols('a1 a2')

q1 = Function('q1')
q2 = Function('q2')
```

```
\#print(t*q1(t))
tr1 = [[cos(q1(t)), -sin(q1(t)), 0],
        [\sin(q1(t)), \cos(q1(t)), 0],
        [0,
                  0,
                          111
tr2 = [[1, 0, a1],
       [0, 1, 0],
       [0, 0, 1]]
tr3 = [[cos(q2(t)), -sin(q2(t)), 0],
        [\sin(q2(t)), \cos(q2(t)), 0],
        [0,
                0,
                        111
tr4 = [[1, 0, a2],
       [0, 1, 0],
       [0, 0, 1]]
tr1 = np.array(tr1)
tr2 = np.array(tr2)
tr3 = np.array(tr3)
tr4 = np.array(tr4)
# do the calculation for the end-effector
E = tr10tr20tr30tr4
E = simplify(E)
print(f'x = \{E[0, 2]\}')
print(f'y = \{E[1, 2]\}')
# velocities for the end-effector
v_x = diff(E[0,2], t)
v_y = diff(E[1,2], t)
print(f'\n\nvelocities for the end-effector are:\nv_x = \{v_x\}')
print(f'v_y = \{v_y\}')
x = a1*cos(q1(t)) + a2*cos(q1(t) + q2(t))
y = a1*sin(q1(t)) + a2*sin(q1(t) + q2(t))
Velocities for the end-effector are:
v_x = -a1*sin(q1(t))*Derivative(q1(t), t) - a2*(Derivative(q1(t), t) +
Derivative(q2(t), t))*sin(q1(t) + q2(t))
v_y = a1*cos(q1(t))*Derivative(q1(t), t) + a2*(Derivative(q1(t), t) +
```

```
Derivative(q2(t), t))*cos(q1(t) + q2(t))
```

Alternative Solution 2: Assuming the steps up to the calculation of E are the same:

```
[80]: Matrix([E[0, 2], E[1, 2]]).jacobian([q1(t), q2(t)]) # built-in Jacobian for⊔

→SymPy Matrix
```

Alternative Solution 3: Assuming the steps up to the calculation of E are the same:

```
[90]: # or based on the definition of the Jacobian derivatives
Jrow1 = [diff(E[0, 2], q1(t)), diff(E[0, 2], q2(t))]
Jrow2 = [diff(E[1, 2], q1(t)), diff(E[1, 2], q2(t))]
[Jrow1, Jrow2]
```

```
[90]: [[-a1*sin(q1(t)) - a2*sin(q1(t) + q2(t)), -a2*sin(q1(t) + q2(t))], [a1*cos(q1(t)) + a2*cos(q1(t) + q2(t)), a2*cos(q1(t) + q2(t))]]
```