

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages

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Memoization

Memoization

- If a function has no side effects and does not read mutable memory, no point in computing it twice for the same arguments
 - Can keep a *cache* of previous results
 - Net win if (1) maintaining cache is cheaper than recomputing and (2) cached results are reused
- Similar to promises, but if the function takes arguments, then there are multiple “previous results”
- For recursive functions, this *memoization* can lead to *exponentially* faster programs
 - Related to algorithmic technique of dynamic programming

How to do memoization: see example

- Need a (mutable) cache that all calls using the cache share
 - So must be defined *outside* the function(s) using it
- See code for an example with Fibonacci numbers
 - Good demonstration of the idea because it is short, but, as shown in the code, there are also easier less-general ways to make **fibonacci** efficient
 - (An association list (list of pairs) is a simple but sub-optimal data structure for a cache; okay for our example)

assoc

- Example uses `assoc`, which is just a library function you could look up in the Racket reference manual:

`(assoc v lst)` takes a list of pairs and locates the first element of `lst` whose car is equal to `v` according to `is-equal?`. If such an element exists, the pair (i.e., an element of `lst`) is returned. Otherwise, the result is `#f`.

- Returns `#f` for not found to distinguish from finding a pair with `#f` in cdr