

Milestones	Steps	Tools involved	Deadline	Estimated number of hours	Effective number of hours
Understand the ϕ -FEM technique	<ol style="list-style-type: none"> Read the documents related to ϕ-FEM <ul style="list-style-type: none"> Read the introductory paper Read the Neumann boundary case 		03/11/2020	4	
The Poisson equation	<ol style="list-style-type: none"> Install FEniCS using Docker <ul style="list-style-type: none"> Install the most recent version Test the installation with the demo case provided Solve the Poisson equation using the classic FEM technique <ul style="list-style-type: none"> Use a simple domain (a unit disk) Validate this step by differentiating a known solution and verifying the results Perform the convergence study in norms L^2 and H^1 <ul style="list-style-type: none"> According to the theory, the slopes must be respectively close to 2 and 1 Solve the Poisson equation using the ϕ-FEM technique, without stabilising terms. Compare the results with the classic FEM technique <ul style="list-style-type: none"> Validate this step by comparison with the test cases in the paper Repeat the preceding test, while applying stabilizing terms <ul style="list-style-type: none"> Validate this step by comparison with the paper Repeat the exact test cases in the paper if necessary 	Docker FEniCS	10/11/2020	20	
The elasticity equation	<ol style="list-style-type: none"> Reformulate the elasticity equation using ϕ-FEM <ul style="list-style-type: none"> Take inspiration from the Poisson formulation Solve the equation using FEniCS <ul style="list-style-type: none"> The method can be validated using academic cases as done in the papers The method can also be validated on classical solid mechanics cases such as beams 	Docker FEniCS	19/01/2021	30	