cs1090a hw0

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```
[]: # Initialize Otter
import otter
grader = otter.Notebook("cs1090a_hw0.ipynb")
```

1 CS1090A Introduction to Data Science

1.1 Homework 0

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1.2 Welcome to CS1090a!

CS1090A attracts students with diverse backgrounds, interests, and goals. As a result, students' experiences with the course prerequisites can be quite varied. Some students may have extensive coding experience, but perhaps can't remember how to represent a projection with linear algebra. Others may have a strong statistics background, but are less confident when it comes to Python.

Homework 0 is a way to assess your comfort with the skills and concepts foundational to the course. It is not expected that you should be able to recall everything from memory while working through the assignment. What maters is the ability to use the context and resources available to fill in any gaps and work toward your goal. This is what we do 'in the real world' after all! However, if you do find HW0 to be too challenging, it is perhaps best to spend more time with the prerequisite material and register for CS1090A the next time around.

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1.3 HW0 User Guide

HW0 is a large document, but there isn't much coding required to complete it.

- If you already know how to create a virtual environment from the provided requirements.txt file then you can jump right to part 2 (though you should read through part 1 eventually).
- The Python content covered in part 2 will start being put to use as early as the first lab and HW assignment.
- The math topics in part 3 will begin to make an appearance by HW2.

About the automatic tests: The test cases embedded in the notebook are intended to keep students on the right track. Most are just checking things like the data type of certain variables you are asked to define. In the "poetry challenge" section there may be multiple ways to complete the prompts, so don't be discouraged if some tests are not passing for you. Passing all tests is not required for getting full credit on HW0. What is expected is that students make a good-faith attempt to complete all sections.

2 Part 1: Setting the Stage

A data scientist's toolkit is a modular collection of various technologies. Taking the time to familiarize yourself with these different components and how they work together will help you be more effective and open new possibilities to you. Students will also be provided with computing environments they can connect to through their web browser that are sufficient for completing all course work. But everyone is expected to be able to create similar environments on computer systems of their own. This is an essential skill for any data scientist.

Prerequisites for this section include: - Using a terminal application to run shell commands - Facility with the filesystem: reading/writing files, navigating the file tree, etc.

2.1 Why Python?

Our primary tool in this course is the Python programming language. It has a reputation for having a clean, readable syntax, sometimes described as being "like pseudocode you can run." Python is also distributed with a large standard library. This "batteries included" approach has made Python one of the most popular general purpose programming languages around today.

As a result, the community of Python users is enormous with many contributing to open source projects. The Python Package Index (PyPi) hosts over 465,000 different projects! And that's not all. There are also specialized repositories for scientific computing packages, such as conda-forge. And then there are all the other public projects hosted on Github, Gitlab, and elsewhere. Python gives us access to this software ecosystem.

2.2 The Shell & Terminal

Most modern operating systems make use of Python, so you likely already have some version installed on your machine!

You can check by querying your **shell**. The shell is a programming language that gives users access to the operating system's services. An interactive shell runs in a read, evaluate, print, and loop sequence (REPL). These days, we interact with the shell through a terminal emulator, which we'll simply (though not quite correctly) refer to as the **terminal**.

The terminal is the program that grants you a text interface through which you can enter commands to the interactive shell.

Note: Windows users have PowerShell, but it lacks many useful commands. This may work for most parts of the course, but please consider trying out Git Bash, or better still, Windows Subsystem for Linux (WSL) for a true UNIX shell experience!

2.2.1 Checking for Python on Your System

Let's put a (UNIX) shell command to use. PowerShell users should try the similar Get-Command.

The which command returns the path names of the files (or links) which would be executed in the current environment, had its arguments been given as commands in the shell. It does this by searching the PATH environmental variable for executable files matching the names of the arguments.

which python

You'll be shown a path like /usr/bin/python.

If it was found, you can invoke python and ask for its version.

```
python --version
```

On some systems you may need to use python3 rather than python in the above commands.

You can run shell commands from within a Jupyter notebook by prepending a!

```
[]: # !command sends `command` to the shell that launched Jupyter !python --version
```

You should see some version >= 3.10

Note: If your call to which threw an error saying it couldn't find python, or if your version is < 3.10, then you're going to need to install Python.

Now you can use Python's *own* interactive shell, or "REPL," in the terminal by envoking python. You'll have access to modules from the standard Python library like datetime, math, collections, itertools, re, etc. But we'd also like to install 3rd party packages.

However, we need to take care in *how* we install packages because: 1. Some of your coding projects will require conflicting versions of the same package that can't coexist. 2. If your operating system makes use of Python, altering the system installation could have unintended consequences. 3. We

can't hope to make our results reproducible without documenting the specific software versions that produced them.

What we need is some way to easily create and manage multiple isolated Python installations, each with their own set of package dependencies.

2.3 Virtual Environments & Package Managers

A virtual environment is a self-contained directory tree that contains a Python installation for a particular version of Python, plus a number of additional packages. Just what we're looking for!

Most Python distributions will include: * venv - to create and manage virtual environments * pip - to download and manage 3rd party packages (from PyPi by default)

For more information on these tools, you can read the Python tutorial entry on virtual environments & packages

But we can generalize this idea of a Python virtual environment to *all languages*. This is useful because our data science projects may have dependencies outside of Python itself.

2.3.1 uv: Modern Python Env Management

We recommend using the uv Python package manager for this course.

First, follow the uv installation instructions.

Now you can use uv to create an environment from a requirements.txt file like the ones the course provides with each assignment. These next two commands only need to be run once for each new virtual environment you create. Be sure to run these commands inside the same directory where the requirements.txt file is located.

```
uv venv
```

uv pip install -r requirements.txt

Now you can activate your environment.

```
source .venv/bin/activate
```

Your command line prompt should change to let you know that your environment is activated. While activated, you have access to all the packages listed in the requirements.txt file.

You can deactivate your environment by running:

deactivate

pyproject.toml is actually the preferred format for uv, but we use requirements.txt as it is compatible with other package managers which students may choose to use.

2.4 Jupyter

Much of the course material, lecture supplementals, labs, exercises, assignments, etc., will be in the form of Jupyter Notebooks. They allow for the embedding of runnable code in a document of formatted text. For more about this general approach, take a look at the literate programming paradigm.

If you created your environment with the requirements.txt file included with HW0, you already have the Jupyter Lab package installed. To explore the Jupyter Lab interface, you can look at their tutorial & documentation.

If you have activated your environment, you can launch Jupyter from your terminal with:

```
jupyter lab
```

Or you can tell uv to launch jupyter lab inside the environment even without activating it:

```
uv run jupyter lab
```

The output in the terminal will display an address you can paste into your browser to access the now running Jupyter Lab server, but it should open in your default browser automatically.

You can edit your shell's config file to make interacting with these tools more comfy. A few ideas: - alias act="source .venv/bin/activate" - alias jl="jupyter lab" - alias jlr="uv run jupyter lab"

Q1 - Check your installation

Assuming this Jupyer notebook was launched from inside your new virtual environment, you should now have access to all the packages listed in the requirements.txt file.

```
[]: # See the "import ... as ..." constructs below:
# they're aliases/shortcuts for the package names. As a result,
# we can call methods such as plt.plot() instead of matplotlib.pyplot.plot()
import numpy as np
from scipy import stats
import pandas as pd
import matplotlib.pyplot as plt
```

```
[]: grader.check("q1")
```

3 Part 2: Python Poetry Challenge

CS1090A assumes students are already familiar with the basics of Python programming.

To assess your level of Python preparedness, you'll be creating a **random poem generator** from a collection of Emily Dickinson poems made available through Project Gutenberg.

Core Python skills utilized in completing this challenge include:

- File I/O
- Data structures
 - strings
 - lists & slicing
 - dictionaries
- Logical operators
- Iteration

- Functions
- Classes
- Debugging
- Reading documentation

•

3.1 Interpreting code

A Note About Excessive Output

In this and future assignments, it is important to limit the length of the output you display. This can be done by printing only a subset of the output. If it is necessary to include all the output and it exceeds ~15 lines, then you should 'enable scrolling output' by right-clicking the cell and enabling this option.

Q2.1 - Read in the file

The document we'll be working with is a digital transcription assembling three early Emily Dickinson poetry collections for which the U.S. copyright has expired.

We've included this document with HW0 as a plain text file. The filename ispg12242.txt and it's located in the data subdirectory.

Read the contents of pg12242.txt into a variable named text. The arcane file name is a stipulation of The Project Gutenberg License included in the file.

Take the contents of the file and save the substring containing the first 10,000 characters as the variable head and the substring containing the final 25,000 characters as tail.

```
text = ...
head = ...
tail = ...
```

```
[]: # We can inspect the beginning of the content print(head)
```

```
[]: # final 25,000 characters print(tail)
```

```
[]: # entire contents
print(text)
```

```
[]: grader.check("q2.1")
```

Q2.2 - Remove non-poem content

Keeping in mind that this is a compilation of three publications (or 'series') and inspecting the head and tail sections of the text we printed above, we can identify some useful structure in the document:

- Project Gutenberg: Header Metadata
- Series 1: Preface
- Series 1: Poems
- Series 2: Preface
- Series 2: Poems
- Series 3: Preface
- Series 3: Poems
- Project Gutenberg: Footer License

Recognizing and making use of structure is a large part of data science.

Create three variables, series1, series2, and series3, each consiting of one of the 3 sections of text dedicated to the poem content, excluding prefaces and the Project Gutenberg metadata and license. Be sure to strip any trailing or leading whitespace from the final strings.

Hints: - Each preface section begins with POEMS\n - Each poem section after a preface starts with a numbered subsection beginning with I. - The Project Gutenberg License section begins with End of Project Gutenberg - You may import standard library modules such as re to help here, but this task can also be done using only Python builtins with no additional imports. - Review indexing and slicing if needed - The string .index() method returns the index of the first occurrence of a target string in a source string.

```
[]: series1 = ...
series2 = ...
series3 = ...
```

```
[]: grader.check("q2.2")
```

We will then join the three series into a single string using join. For the delimiter we use six newline characters. The reason for this choice will soon become clear.

And we can check to see that we only have the poem content.

```
[]: print(poems_text[:445])
print('\n---\n')
print(poems_text[-275:])
```

Q2.3 - Remove annotation

The first poem contains some editor annotation in square brackets.

```
[]: print(poems_text[:200], '...')
```

This is the only annotation like this in the text. You can see that these are the only two square brackets that appear in the string.

```
[]: # Confirm that brackets occur only once assert (poems_text.count("["] == 1) and (poems_text.count("]") == 1)
```

Create poems_text_clean which has this annotation (and the additional blank line below it) removed.

Hints: The string method split could be put to use here

```
[]: poems_text_clean = ...
[]: print(poems_text_clean[:100], '...')
[]: grader.check("q2.3")
```

Q2.4 - Identify sections and numbering

Now let's remove some of the other content that was *not* the work of the original author: the section titles and poem numbers. It is helpful to notice that all such lines begin with roman numerals.

Implement the startswith_rn function which we can use to identify lines that serve as section titles or poem numbering.

Note: The function does not need to be sophisticated enough to reject 'invalid' roman numerals such as 'IIIV.' We are assuming (correctly) that these sorts of strings do not occur and so the function only needs to be powerful enough to recognize those numerals that do occur at the start of headers in the text while excluding the titles and the content of any of the poems.

```
[]: grader.check("q2.4")
```

Q2.5 - Remove sections and numbering

Use your new startswith_rn function to help you remove the lines starting with roman numerals from poems_text_clean. Strip any whitespace from the ends of the final result and store the string in the variable poems_text_nonum

```
[]: poems_text_nonum = ...

[]: print(poems_text_nonum[:500])

[]: grader.check("q2.5")
```

Q2.6 - Create a list of poems

Next, we'd like to split the text up into a list of poems.

To investigate how we might do this it is important to view all the characters in the text. The pprint function from the standard library allows us to display the text with the newline characters \n while also making the output easier to read by including the line breaks as well.

```
[]: from pprint import pprint

[]: pprint(poems_text_nonum[:2000])
```

Notice how the poems are separated by multiple newline characters. Further exploration shows the minimum number of newlines between poems to be 6.

Use this information to create poem_list where the elements of the list are the poems in the order they occur in poems_text_nonum. For now, we will include the title if the editors provided one as part of the poem. Each poem should be stripped of leading and trailing whitespace.

Hint: Be sure to exclude any empty strings elements from your final poem_list.

```
[]: poem_list = ...
[]: print(poem_list[109])

[]: print(f"There are a total of {len(poem_list)} poems.")

[]: grader.check("q2.6")
```

Q2.7 - Create a poem dictionary

We now have all the poems separated, but we might want some means of accessing specific poems without having to remember their arbitrary position in the list. This is where the key-value pair structure of dictionaries will help.

We will create a dictionary, d, where the keys are the poem titles and the values are the poems themselves.

If the editors did not provide a title, we'll use the first line of the poem as the key.

Recall that some poems were given identical titles. And we know dictionary keys must be unique. Our approach will be to use incrementing numerical labels to denote poems with duplicate names beyond the first encountered. The titles should then look like: "ETERNITY.", "ETERNITY. (2)", "ETERNITY. (3)", etc.

We have provided one possible implementation that is nearly complete. Only one line needs to be filled in.

You are also welcome to create your own solution from scratch.

```
[]: # helper functions
import re

# Answers: what number should I increment to having now seen a duplicate?
def next_title_num(prev_key: str) -> int:
```

```
[]: is_editor_title = lambda x: x.endswith('.') and x.isupper()
has_editor_title = lambda x: is_editor_title(x.split('\n')[0]) # check 1st line_u

ofor editor title

d = {}
for p in poem_list:
    # first line will always be the key
    k = p[:p.index('\n')]
    if has_editor_title(p):
        # find string that should be the value (poem minus title)
        # YOUR CODE HERE
        p = ...
# add new pair to dictionary
# update function handles altering the key if necessary
# (i.e., incrementing the numerical suffix of the title)
        update(d, k, p)
```

```
[]: print(d['HOPE.'])
```

```
[ ]: grader.check("q2.7")
```

Q2.8 - Most frequent long words

We can also ask statistical questions of the data such as, "what are the most common words?"

Find the 10 most frequently used words longer than 10 characters. Ignore case and any punctuation at the end of the word when counting. Consider only the poem text and not the editor provided titles. Store the top 10 words in a list called top words in order of decreasing frequency.

You may find the punc variable below useful. It is the set of the punctuation characters occurring at the end of words in the text. You can assume that no words end with multiple punctuation

characters.

Q2.9 - Random Poem Generator

We're now ready to create our random poem generator.

Complete the PoetryCollection class below by defining a ___init__ method. It should take the author's full name and your poem dictionary as arguments and define the class attributes author, collection, and size as described in the docstring.

Then instantiate a PoetryCollection using our Emily Dickinson data and call it poems.

```
[]: class PoetryCollection():
         HHHH
         Attributes
         _____
         author: str
             full name of author
         collection : dict
             dictionary of (title, poem) key-value pairs
         size : int
             number of poems in collection
         Methods
         random_poem(seed: int = None) -> str
             returns random poem; use seed for reproducibility (default seed=None)
         HHHH
         . . .
         def random_poem(self, seed : int = None) -> str:
             rng = np.random.default_rng(seed)
             return str(rng.choice(list(self.collection.values())))
[]: poems = ...
```

```
[]: print('Author:', poems.author)
```

```
[]: print('Number of poems in collection:', poems.size)
[]: print(poems.random_poem(seed=109))
     grader.check("q2.9")
[]:
        Part 3 - Math and Statistics
     4.0.1 Linear Algebra
     Q3.1.1 - Matrix Multiplication (Dimensions)
     Suppose you have two matrices, A is of shape (4, 7), and B is of shape (7, 5).
     Let C = AB.
     What are the dimensions of C?
     Fill in your answers as a tuple object (e.g., (1,2)).
[]: C_dim = ...
[]: grader.check("q3.1.1")
     Q3.1.2 - Matrix Transpose
     Let A be a 4 \times 7 matrix.
     Answer the following questions: - What are the dimensions of A^{\top}, AA^{\top}, and A^{\top}A respectively?
     - Which of the following products are not conformable (i.e., cannot be computed)?
     Provide your answer as a list of the option letters (order does not matter).
     Options:
     - A. AA
     - \mathbf{B}.\ A^{\top}A^{\top}
     - C. A(A^{T}A)
     - D. (A^{\top}A)A^{\top}
[]: AT_dim = ...
     AAT_dim = ...
     ATA_dim = ...
     non_conformable = ...
[]: grader.check("q3.1.2")
     Q3.1.3 - Matrix Inversion (Dimensions)
     A is 6 \times 6, and A is invertible. What is the shape of A^{-1}?
[ ]: Ainv_dim = ...
[]: grader.check("q3.1.3")
```

In data science we frequently encounter problems that can be represented (or approximated) by a system of linear equations.

In this toy example, you've started to collect data about some books in your collection:

Title	New/Cover Price (\$)	Years Since Publication	Has Underlining (Yes/No)	Used Price (\$)
Perceptrons (Expanded) Social Empiricism Philosophical Investigations	35	35	1	15
	20	21	0	11
	42	13	1	27

Has Underlining is 1 if the book is marked up with notes and 0 otherwise.

We will (very naïvely) assume that a book's used price is a linear combination of the three recorded features which capture information about the book's original price, age, and condition.

That is, there exist coefficients β_1 , β_2 , and β_3 such that:

 β_1 · new price + β_2 · years since publication + β_3 · has underlining = used price

If you knew the coefficient values then these three features could be used to *predict* the used price of a book for which that data is unavailable, or perhaps to check if a newly observed used price is fair.

If we represent the set of unknown coefficients as a column vector

$$\beta = \left[\begin{array}{c} \beta_1 \\ \beta_2 \\ \beta_3 \end{array} \right]$$

and represent the three features of our books as a matrix, X, and the used prices as a column vector, y

$$X = \begin{bmatrix} 35 & 35 & 1 \\ 20 & 21 & 0 \\ 42 & 13 & 1 \end{bmatrix} y = \begin{bmatrix} 15 \\ 11 \\ 27 \end{bmatrix}$$

then we can calculate the linear combinations for all rows in X with a single matrix multiplication:

$$X\beta = y$$

Or, written out with the full matrices and vectors:

$$\begin{bmatrix} 35 & 35 & 1 \\ 20 & 21 & 0 \\ 42 & 13 & 1 \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \\ \beta_3 \end{bmatrix} = \begin{bmatrix} 15 \\ 11 \\ 27 \end{bmatrix}$$

Q3.2 - Arrays & Matrices with Numpy

Use Numpy's ndarray constructor, np.array() to create the X matrix and y column vector as shown above. It is common to pass the constructor a list or list-of-lists as an argument. Don't be afraid to check the documentation. >Hint: Remember, y is a column vector. You can check the dimensions of an ndarray with the .shape attribute. y's shape should be (3,1). The array's .reshape() method is one way to address this. When in doubt, a quick internet search will often turn up Stack Overflow answers to similar questions.

$$\begin{bmatrix} x = \dots \\ y = \dots \end{bmatrix}$$

Q3.3 - Matrix inverse

We'd like to solve for β algebraically, and we are in luck! Because our X matrix is square and full rank we can take its inverse, denoted X^{-1} .

A matrix multiplied by its inverse is the identity matrix of the same shape: $A_{n,n}^{-1}A_{n,n}=I_{n,n}$

And of course, multipling a vector or matrix by the identity matrix leaves it unchanged (provided the shapes allow for a valid matrix multiplication): IA = A

This is all we need to solve for β . Just multiply both sides of the equation by X^{-1} on the left and simplify:

$$X\beta = y$$

$$X^{-1}X\beta = X^{-1}y$$

$$I\beta = X^{-1}y$$

$$\beta = X^{-1}y$$

With the information presented above, use Numpy to find β and store it in **beta**. >**Hints:** Numpy has a **linalg** sub-module containing many useful functions related to linear algebra. You'll need (1) a method to take the inverse of a matrix and (2) a means of calculating a matrix product. The documention is very thorough.

```
[]: beta = ...
```

[]: # display resulting betas beta

[]: grader.check("q3.3")

Q3.4 - Making a prediction

Now let's use your β vector to predict the used price of a book not in our original data.

Title	New/Cover	Years Since	Has	Used
	Price	Publication	Underlining	Price
Linear Algebra Done Right	44	7	0	?

Create the ndarray new_book to represent the three feature values of the book. Then multiply it by beta and store the results in pred_price.

```
[]: new_book = ...
pred_price = ...
[]: print(f'Predicted Price: ${pred_price[0]:.2f}')
[]: grader.check("q3.4")
```

We will almost never be so lucky as to be working with a square data matrix in a problem like this. And our assumption that used prices *are indeed* linear combinations of the feature values, with no variation, is far too strong. In the course we will see ways of relaxing both these assumptions.

4.0.2 Multivariate Calculus

Q3.5 - Partial Derivatives for Optimization

Calculus is a powerful tool for optimization. For example, imagine we have a "loss" or "cost" function, f(x, y), where x and y are parameters we can control. The goal is to find the values of x and y that minimize f.

$$\arg\min_{x,y} f(x,y)$$

We know that a function's derivative is zero at extrema (provided it is differentiable there). Taking the partial derivatives of f with respect to each of the parameters, setting them equal to zero, and solving for the respective parameter values can then provide us with potential minima. We can confirm that a set of parameter values correspond to a minima if we can also show that the 2nd derivatives evaluated at those values are all > 0 (again, provided the original function is twice differentiable there).

Your goal is to use this strategy to find the x and y that minimize the loss function:

$$f(x,y) = xy + (y+1)^2 + 2x^2 + 4$$

You can also do this using the gradient operator, ∇ .

One of the main benefits of working with jupyter notebooks is the ability to display nicely formatted mathematical notation. Use \LaTeX in a markdown cell(s) below to show your work. Then store the x and y values you find that minimize f in the variables $\texttt{x_min}$ and $\texttt{y_min}$ respectively.

You can find an intro tutorial here if your LATEX is a bit rusty.

Type your answer here, replacing this text.

```
[]: x_min = ...
y_min = ...
[]: grader.check("q3.5")
```

4.0.3 Probability & Statistics

As we move through the course we will look at a probabilistic method for modeling data. There, we assume that the value of interest, y, for each observation, x, is a random variables described by a specific family of probability distributions (e.g., Gaussian, binomial, etc.), and that the parameter(s) of these distributions, such as the mean, is related to the values in x. We then try and learn what this relationship is.

But before we get there we should remind ourselves about how to work with probabilities.

Q3.6 - Joint probabilities

First, let's think about the joint probability of several i.i.d. random variables.

What is the probability of rolling three 3's in a row with a fair 6-sided die? Save the result in dice_prob.

```
[]: dice_prob = ...
dice_prob
```

```
[]: grader.check("q3.6")
```

Q3.7 - A 'branching' example

Here's a slightly more involved scenario:

In your pocket you have two coins: a **fair coin** and a **biased coin** that is twice as likely to land heads than tails.

You take a coin from your pocket at random and flip it 4 times. You see:

Given that you were equally likely to choose either coin, what was the probability of this series of outcomes?

Save your result in coin_prob.

```
[]: coin_prob = ...
coin_prob

[]: grader.check("q3.7")
```

Q3.8 - Conditional Probability

What is the probability of observing H, H, H conditional on having pull the biased coin from your pocket? Recall that this coin is twice as likely to land heads than tails.

That is, calculate P(H, H, H|B) where B is the event of drawing the biased coin from your pocket.

This time, rather than calculating the value programatically, show your work with LATEX in a markdown cell below.

Type your answer here, replacing this text.

Q3.9 - Sampling from a PDF with Numpy

Numpy also gives us the ability to sample from probability distributions through its Random Generator class, which can be created with the np.random.default_rng() constructor.

```
[]: # instantiate random generator /w seed of 109
rng = np.random.default_rng(seed=109)
```

Let X be a normally distributed random variable with a mean of 4 and a standard deviation of 2. That is:

$$X \sim \mathcal{N}(4,2)$$

Sample N realizations of X using rng.normal() and store them in the variable sample. Next, calculate the mean and standard deviation of the sample and store the results in the variables mean and std.

Try several values for N. Start with just 10 and increase the sample size until the sample mean and standard deviation are within 0.1 of those of the data generating distribution.

Hint: check the documentation on the generators normal() method.

```
[]: # number of samples
N = ...

# N samples from normal distribution /w mean=4 & std=2
sample = ...
```

```
[]: mean = ...
std = ...
print(f"sample mean: {mean:.2f}")
print(f"sample standard deviation: {std:.2f}")
```

The histogram below visualizes the empirical distribution of your sample as well as the sample mean and standard deviation.

This uses the Matplotlib library which will be one of our main visualization tools in this course.

```
[]: # provided plotting code
plt.hist(sample)
plt.axvline(mean, c='r', label=f'mean = {mean:.2f}')
plt.axvline(mean+std, c='k', ls='--', label=f'stdev = {std:.2f}')
plt.axvline(mean-std, c='k', ls='--')
plt.title(rf'{N} Samples of $X \sim \mathcal{{N}}(4, 2)$')
plt.ylabel('count')
plt.xlabel(r"$X$ value")
plt.legend();
```

```
[]: grader.check("q3.9")
```

Q3.10 - Normal Distribution — Analytic vs. Empirical Probability

```
Let X \sim N(4,2).
```

Compute P(X > 7) in two different ways:

- 1. **Analytically** using the CDF of the normal distribution (via an online calculator, statistical tables, or scipy.stats.norm).
- 2. **Empirically** by simulating 10^6 draws from N(4,2) and computing the proportion of samples greater than 7.

Report both probabilities, and confirm they are close to each other.

Hints: - The convention with scipy is to import individual submodules. The stats module was imported for you earlier in the notebook. - When simulating draws, be sure to use a random seed so your results are reproducible.

```
[]: P_greater_than_7_Analytic = ...
P_greater_than_7_Empirical = ...

print("Analytic:", P_greater_than_7_Analytic)
print("Empirical:", P_greater_than_7_Empirical)
```

```
[]: grader.check("q3.10")
```

4.1 Reflection

Please let us know how long it took you to complete HW0 and answer the following questions in a few sentences:

Do you feel you struggled with HW0?

Which section was the hardest for you, and why?

```
[]: # Let us know how long it took you hours_to_complete = ...
```

your answer here

This concludes HW0. Thank you!