Input: y is a sequence of T characters, V is a subword vocabulary, m is the maximum subword length **Output:** Segmentation z with highest posterior probability.

for k = 1 to T do

 $\beta_k \leftarrow \max_{\left\{j \in [k-m,k-1] \mid \boldsymbol{y}_{j,k} \in V\right\}} \beta_j + \log P_{\theta}(\boldsymbol{y}_{j,k} | y_1,..,y_j)$

$$\begin{array}{l} \text{Argmax} \left\{ j \in [k-m,k-1] \mid \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j}), \\ \leftarrow \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y}_{j,k}), \\ \text{argmax} \left\{ \boldsymbol{y}_{j,k} \in V \right\} \neq j + \log P_{\theta}(\boldsymbol{y}_{j,k} \mid \boldsymbol{y$$

Algorithm 2 Dynamic Programming Encoding (DPE) for Subword Segmentation

 $b_k \leftarrow \operatorname{argmax}_{\{j \in [k-m,k-1] \mid \boldsymbol{y}_{j,k} \in V\}} \beta_j + \log P_{\theta}(\boldsymbol{y}_{j,k} | y_1, ..., y_j)$

$$= \underset{m}{\operatorname{argmax}} \left\{ j \in [k-m,k-1] \mid oldsymbol{y}_{j,k} \in V
ight\} oldsymbol{\mathcal{D}}_j + \log F_{oldsymbol{ heta}}(oldsymbol{y}_{j,k}) \right\}$$