

HW1

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1

- (a) $Pr(Y = 1) = 0.25 + 0.1 + 0.15 = 0.5$
- (b) $Pr(X = 2 \cap Y = 1) = 0.1$
- (c) $Pr(X = 2 \cap Y = 1) = \frac{0.1}{0.5} = 0.2$
- (d) $Pr(X = 3 \cap Y = 2) = 0.2$
 $1 - (0.25 + 0.1 + 0.15 + 0.1 + 0.2) = 0.2$

2

$$\begin{aligned} E[B+H] &= E[B] + E[H] \\ E[B] &= 1 \times 0.25 + 3 \times 0.25 + 4 \times 0.25 + 7 \times 0.25 = 3.75 \end{aligned}$$

$$E[H = x] = \int_a^b x f(x) dx = \int_{-1}^4 \frac{1}{5}(x) dx = \frac{1}{5} \int_{-1}^4 x dx = \frac{1}{5} \times \frac{x^2}{2} \Big|_{-1}^4 = 1.5 \quad (1)$$

$$E[B + H] = 3.75 + 1.5 = 5.25 \text{ mi} \quad (2)$$

3

$$\mathbf{Pr}(\mathbf{M}=0) = 0.3$$

$$\begin{aligned} \sum_{x \in D} (-|M - x|/2) + |D| \ln(\frac{1}{4}) + \ln(0.3) &= (-|0 - (-1)|/2) + (-|0 - (6)|/2) + \\ &+ (-|0 - 0|/2) + (-|0 - 2|/2) + (-|0 - (-1)|/2) + (-|0 - 7|/2) + (-|0 - 7|/2) + \\ &+ (-|0 - 8|/2) + (-|0 - 4|/2) + (-|0 - (-2)|/2) + \ln(0.3) = -20.2 \end{aligned}$$

$$\mathbf{Pr}(\mathbf{M}=2) = 0.3$$

$$\begin{aligned} \sum_{x \in D} (-|M - x|/2) + |D| \ln(\frac{1}{4}) + \ln(0.3) &= (-|2 - (-1)|/2) + (-|2 - (6)|/2) + \\ &+ (-|2 - 0|/2) + (-|2 - 2|/2) + (-|2 - (-1)|/2) + (-|2 - 7|/2) + (-|2 - 7|/2) + \end{aligned}$$

$$(-|2-8|/2)) + (-|2-4|/2)) + (-|2-(-2)|/2)) + \ln(0.3) = -18.2$$

$$\mathbf{Pr}(\mathbf{M}=4) = \mathbf{0.4}$$

$$\sum_{x \in D} (-|M-x|/2) + |D| \ln(\frac{1}{4}) + \ln(0.3) = (-|4-(-1)|/2)) + (-|4-(6)|/2)) + (-|4-0|/2)) + (-|4-2|/2)) + (-|4-(-1)|/2)) + (-|4-7|/2)) + (-|4-7|/2)) + (-|4-8|/2)) + (-|4-4|/2)) + (-|4-(-2)|/2)) + \ln(0.4) = -17.9$$

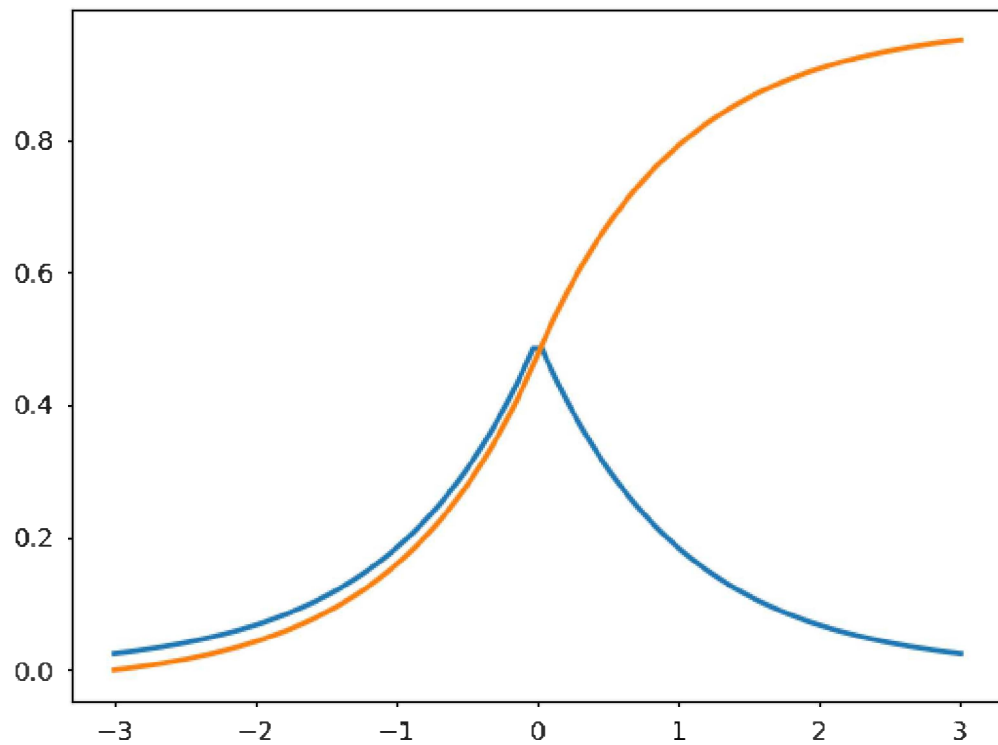
Because $M = 4$ is the largest number in the set, we can deduce that actually M is equal to 4.

```
In [2]: import matplotlib as mpl
        %matplotlib nbagg
        #mpl.use('PDF')
        import matplotlib.pyplot as plt
        import matplotlib.mlab as mlab
        from scipy.stats import laplace
        import scipy.special as sps
        import numpy as np
        import math
```

```
In [3]: mean, var, skew, kurt = laplace.stats(moments='mvsk')
```

```
In [4]: x = np.linspace(-3, 3, 100)
```

```
In [5]: plt.plot(x, laplace.pdf(x),linewidth=2.0, label='Laplace PDF')
```



```
Out[5]: [<matplotlib.lines.Line2D at 0x9c16978>]
```

```
In [6]: plt.plot(x, laplace.cdf(x) -.024893,linewidth=2.0, label='Laplace CDF')
```

```
Out[6]: [<matplotlib.lines.Line2D at 0x9dd0c88>]
```

```
In [ ]: plt.legend(bbox_to_anchor=(.35,1))
```