```
Contents
                                                                      1. Code Templates
                                                                                                             from collections import Counter
                                                                                                             import svs
1. Code Templates
                                                  1 1.1. .bashrc. Aliases.
                                                                                                              sys.setrecursionlimit(1000000)
1.1. .bashrc
                                                     alias nv=vim
1.2. .vimrc
                                                     alias o="xdq-open ."
                                                                                                             1.5. C++ Template. A C++ template
1.3. Java Template
                                                                                                              #include <stdio.h>
                                                     1.2. .vimrc. Tabs, linenumbers, wrapping
1.4. Python Template
                                                                                                              #include <iostream>
1.5. C++ Template
                                                     set nowrap
                                                                                                             #include <algorithm>
1.6. Fast IO Java
                                                     svntax on
                                                                                                             #include <vector>
2. Data Structures
                                                     set tabstop=8 softtabstop=0
                                                                                                             #include <math.h>
2.1. Binary Indexed Tree
                                                     set expandtab shiftwidth=4 smarttab
                                                                                                             #include <cmath>
2.2. Segment Tree
                                                     set rnu
                                                                                                             using namespace std;
2.3. Lazy Segment Tree
                                                     set number
                                                                                                             int main() {
2.4. Union Find
                                                     set scrolloff=8
                                                                                                                 cout.precision(9);
2.5. Monotone Queue
                                                     language en_US
                                                                                                                 int N:
2.6. Treap
                                                     1.3. Java Template. A Java template.
                                                                                                                 cin >> N;
3. Graph Algorithms
                                                                                                                 cout << 0 << endl;</pre>
                                                     import java.util.*;
3.1. Djikstras algorithm
                                                                                                             }
                                                     import java.io.*;
3.2. Bipartite Graphs
                                                     public class A {
3.3. Network Flow
                                                                                                             1.6. Fast IO Java. Kattio with easier names
                                                         void solve(BufferedReader in) throws Exception {
4. Dynamic Programming
                                                                                                             import java.util.StringTokenizer;
4.1. Longest Increasing Subsequence
                                                                                                             import java.io.*;
4.2. Knuuth Morris Pratt substring
                                                  6
                                                                                                             class Sc {
                                                         int toInt(String s) {return Integer.parseInt(s);}
4.3. String functions
                                                                                                                public Sc(InputStream i) {
                                                         int[] toInts(String s) {
5. Etc
                                                                                                                  r = new BufferedReader(new InputStreamReader(i));
                                                             String[] a = s.split(" ");
5.1. System of Equations
                                                             int[] o = new int[a.length];
5.2. Convex Hull
                                                  7
                                                                                                                public boolean hasM() {
                                                             for(int i = 0; i<a.length; i++)</pre>
6. NP tricks
                                                  8
                                                                                                                  return peekToken() != null;
                                                                  o[i] = toInt(a[i]);
6.1. MaxClique
                                                  8
7. Coordinate Geometry
                                                  8
                                                             return o;
                                                                                                               public int nI() {
                                                  8
                                                         }
7.1. Area of a nonintersecting polygon
                                                                                                                  return Integer.parseInt(nextToken());
                                                         void e(Object o) {
7.2. Intersection of two lines
                                                             System.err.println(o);
7.3. Distance between line segment and point
                                                                                                                public double nD() {
7.4. Picks theorem
                                                                                                                  return Double.parseDouble(nextToken());
                                                         public static void main(String[] args)
                                                  9
7.5. Implementations
                                                         throws Exception {
8. Acieving AC on a solved problem
                                                 10
                                                                                                                public long nL() {
                                                             BufferedReader in = new BufferedReader
8.1. WA
                                                 10
                                                                                                                  return Long.parseLong(nextToken());
                                                                  (new InputStreamReader(System.in));
8.2. TLE
                                                 10
                                                             (new A()).solve(in);
8.3. RTE
                                                 10
                                                                                                                public String n() {
                                                 10
8.4. MLE
                                                                                                                  return nextToken():
                                                     }
                                                     1.4. Python Template. A Python template
                                                                                                                private BufferedReader r;
                                                     from collections import defaultdict
                                                                                                                private String line;
                                                     from collections import deque
                                                                                                               private StringTokenizer st;
```

}

private static class ST {

int li, ri;

}

```
private String token;
 private String peekToken() {
    if (token == null)
      try {
        while (st == null || !st.hasMoreTokens()) {
          line = r.readLine();
          if (line == null) return null;
          st = new StringTokenizer(line);
        token = st.nextToken();
      } catch (IOException e) { }
    return token;
  private String nextToken() {
    String ans = peekToken();
    token = null;
    return ans:
}
```

2. Data Structures

2.1. Binary Indexed Tree. Also called a fenwick tree. Builds in $\mathcal{O}(n \log n)$ from an array. Querry sum from 0 to i in $\mathcal{O}(\log n)$ and updates an element in $\mathcal{O}(\log n)$.

```
private static class BIT {
  long[] data;
  public BIT(int size) {
    data = new long[size+1];
  }
  public void update(int i, int delta) {
    while(i< data.length) {
      data[i] += delta;
      i += i&-i; // Integer.lowestOneBit(i);
    }
  }
  public long sum(int i) {
    long sum = 0;
    while(i>0) {
      sum += data[i];
      i -= i&-i;
    }
}
```

return sum:

2.2. **Segment Tree.** More general than a fenwick tree. Can adapt other operations than sum, e.g. min and max.

```
int sum: //change to max/min
  ST lN;
  ST rN;
static ST makeSqmTree(int[] A, int l, int r) {
 if(l == r) {
   ST node = new ST();
   node.li = l:
   node.ri = r:
   node.sum = A[l]; //max/min
    return node;
  int mid = (l+r)/2;
 ST lN = makeSqmTree(A,l,mid);
  ST rN = makeSqmTree(A,mid+1,r);
  ST root = new ST();
  root.li = lN.li;
  root.ri = rN.ri;
  root.sum = lN.sum + rN.sum: //max/min
  root.lN = lN;
  root.rN = rN;
  return root:
static int getSum(ST root, int l, int r) {//max/min
 if(root.li>=l && root.ri<=r)</pre>
    return root.sum; //max/min
 if(root.ri<l || root.li > r)
    return 0; //minInt/maxInt
  else //max/min
    return getSum(root.lN,l,r) + getSum(root.rN,l,r);
static int update(ST root, int i, int val) {
 int diff = 0:
 if(root.li==root.ri && i == root.li) {
    diff = val-root.sum; //max/min
    root.sum=val: //max/min
    return diff: //root.max
```

```
int mid = (root.li + root.ri) / 2;
if (i <= mid) diff = update(root.lN, i, val);
else diff = update(root.rN, i, val);
root.sum+=diff; //ask other child
return diff; //and compute max/min</pre>
```

2.3. Lazy Segment Tree. More general implementation of a segment tree where its possible to increase whole segments by some diff, with lazy propagation. Implemented with arrays instead of nodes, which probably has less overhead to write during a competition.

```
class LazySegmentTree {
 private int n;
 private int[] lo, hi, sum, delta;
 public LazySegmentTree(int n) {
   this.n = n;
   lo = new int[4*n + 1];
   hi = new int[4*n + 1];
   sum = new int[4*n + 1];
   delta = new int[4*n + 1]:
   init();
 public int sum(int a, int b) {
    return sum(1, a, b);
 private int sum(int i, int a, int b) {
   if(b < lo[i] || a > hi[i]) return 0;
   if(a \leftarrow lo[i] && hi[i] \leftarrow b) return sum(i);
   prop(i);
   int l = sum(2*i. a. b):
   int r = sum(2*i+1, a, b);
   update(i);
    return l + r;
 public void inc(int a, int b, int v) {
   inc(1, a, b, v);
 private void inc(int i, int a, int b, int v) {
   if(b < lo[i] || a > hi[i]) return;
   if(a <= lo[i] && hi[i] <= b) {
      delta[i] += v;
```

```
return;
    }
    prop(i);
    inc(2*i, a, b, v);
    inc(2*i+1, a, b, v);
    update(i);
  private void init() {
    init(1, 0, n-1, new int[n]);
  private void init(int i, int a, int b, int[] v) {
    lo[i] = a:
    hi[i] = b;
    if(a == b) {
      sum[i] = v[a];
      return:
    int m = (a+b)/2;
    init(2*i, a, m, v);
    init(2*i+1, m+1, b, v);
    update(i);
  private void update(int i) {
    sum[i] = sum(2*i) + sum(2*i+1);
 private int range(int i) {
    return hi[i] - lo[i] + 1;
  private int sum(int i) {
    return sum[i] + range(i)*delta[i];
  private void prop(int i) {
    delta[2*i] += delta[i];
    delta[2*i+1] += delta[i];
    delta[i] = 0;
}
```

2.4. **Union Find.** This data structure is used in varoius algorithms, for example Kruskals algorithm for finding a Minimal Spanning Tree in a weighted graph. Also it can be used for backward simulation of dividing a set.

```
private class Node {
 Node parent;
 int h;
  public Node() {
   parent = this;
    h = 0;
  public Node find() {
   if(parent != this) parent = parent.find();
    return parent;
static void union(Node x, Node v) {
 Node xR = x.find(), yR = y.find();
 if(xR == yR) return;
 if(xR.h > yR.h)
   yR.parent = xR;
  else {
   if(yR.h == xR.h) yR.h++;
   xR.parent = yR;
 }
}
```

2.5. Monotone Queue. Used in sliding window algorithms where one would like to find the minimum in each interval of a given length. Amortized $\mathcal{O}(n)$ to find min in each of these intervals in an array of length n. Can easily be used to find the maximum as well.

```
private static class MinMonQue {
   LinkedList<Integer> que = new LinkedList<>();
   public void add(int i) {
      while(!que.isEmpty() && que.getFirst() > i)
            que.removeFirst();
      que.addFirst(i);
   }
   public int last() {
      return que.getLast();
   }
   public void remove(int i) {
      if(que.getLast() == i) que.removeLast();
   }
}
```

2.6. **Treap.** Treap is a binary search tree that uses randomization to balance itself. It's easy to implement, and gives you access to the internal structures of a binary tree, which can be used to find the k'th element for example. Because of the randomness, the average height is about a factor 4 of a prefectly balanced tree.

```
class Treap{
 int sz;
 int v;
 double v;
 Treap L, R;
 static int sz(Treap t) {
   if(t == null) return 0;
   return t.sz:
 static void update(Treap t) {
   if(t == null) return;
   t.sz = sz(t.L) + sz(t.R) + 1;
 static Treap merge(Treap a, Treap b) {
   if (a == null) return b;
   if(b == null) return a;
   if (a.y < b.y) {
      a.R = merge(a.R, b);
      update(a);
      return a;
   } else {
      b.L = merge(a, b.L);
      update(b);
      return b:
 //inserts middle in left half
 static Treap[] split(Treap t, int x) {
   if (t == null) return new Treap[2];
   if (t.v <= x) {
     Treap[] p = split(t.R, x);
     t.R = p[0]:
      p[0] = t;
      return p;
   } else {
     Treap[] p = split(t.L, x);
```

```
t.L = p[1];
    p[1] = t;
    return p;
  }
}
//use only with split
static Treap insert(Treap t, int x) {
  Treap m = new Treap();
  m.v = x:
  m.y = Math.random();
  m.sz = 1;
  Treap[] p = splitK(t, x-1);
  return merge(merge(p[0],m), p[1]);
}
//inserts middle in left half
static Treap[] splitK(Treap t, int x) {
  if (t == null) return new Treap[2];
  if (t.sz < x) return new Treap[]{t, null};</pre>
  if (sz(t.L) >= x) {
    Treap[] p = splitK(t.L, x);
    t.L = p[1];
    p[1] = t;
    update(p[0]);
    update(p[1]);
    return p;
  } else if (sz(t.L) + 1 == x){
    Treap r = t.R;
    t.R = null;
    Treap[] p = new Treap[]{t, r};
    update(p[0]);
    update(p[1]);
    return p;
  } else {
    Treap[] p = splitK(t.R, x - sz(t.L)-1);
    t.R = p[0];
    p[0] = t;
    update(p[0]);
    update(p[1]);
    return p;
//use only with splitK
```

```
static Treap insertK(Treap t, int w, int x) {
   Treap m = new Treap();
    m.v = x:
    m.y = Math.random();
    m.sz = 1;
    Treap[] p = splitK(t, w);
    t = merge(p[0], m);
    return merge(t, p[1]);
  //use only with splitK
  static Treap deleteK(Treap t, int w, int x) {
   Treap[] p = splitK(t, w);
   Treap[] q = splitK(p[0], w-1);
    return merge(q[0], p[1]);
  static Treap Left(Treap t) {
    if (t == null) return null;
    if (t.L == null) return t;
    return Left(t.L);
  static Treap Right(Treap t) {
    if (t == null) return null:
    if (t.R == null) return t;
    return Right(t.R);
}
                3. Graph Algorithms
```

3.1. Djikstras algorithm. Finds the shortest distance be-

```
tween two Nodes in a weighted graph in \mathcal{O}(|E|\log|V|) time.
//Requires java.util.LinkedList and java.util.TreeSet
  LinkedList<Edge> edges = new LinkedList<>():
  int w;
  int id;
  public Node(int id) {
    w = Integer.MAX_VALUE;
    this.id = id;
  public int compareTo(Node n) {
    if(w != n.w) return w - n.w;
```

```
return id - n.id;
  //Asumes all nodes have weight MAXINT.
  public int djikstra(Node x) {
    this.w = 0;
    TreeSet<Node> set = new TreeSet<>();
    set.add(this);
    while(!set.isEmpty()) {
      Node curr = set.pollFirst():
      if(x == curr) return x.w;
      for(Edge e: curr.edges) {
        Node other = e.u == curr? e.v : e.u;
        if(other.w > e.cost + curr.w) {
          set.remove(other);
          other.w = e.cost + curr.w;
          set.add(other):
      }
    }
    return -1;
 }
private static class Edge {
 Node u,v;
  int cost;
  public Edge(Node u, Node v, int c) {
    this.u = u: this.v = v:
    cost = c;
}
```

4

3.2. Bipartite Graphs. The Hopcroft-Karp algorithm finds the maximal matching in a bipartite graph. Also, this matching can together with Könings theorem be used to construct a private static class Node implements Comparable<Node>{ minimal vertex-cover, which as we all know is the complement of a maximum independent set. Runs in $\mathcal{O}(|E|\sqrt{|V|})$.

```
import java.util.*;
class Node {
  int id:
 LinkedList<Node> ch = new LinkedList<>();
  public Node(int id) {
    this.id = id;
}
```

```
public class BiGraph {
                                                               if(Pair[v.id] == -1 || dfs(U[Pair[v.id]])) {
                                                                                                                          Z[v.id] = true;
 private static int INF = Integer.MAX_VALUE;
                                                                 Pair[v.id] = u.id;
                                                                                                                          if(Rm.containsKey(y.id)){
                                                                Pair[u.id] = v.id;
 LinkedList<Node> L, R;
                                                                                                                            int xx = Rm.get(y.id);
 int N, M;
                                                                 return true;
                                                                                                                            if(!Z[xx]) {
 Node[] U;
                                                              }
                                                                                                                             Z[xx] = true;
 int[] Pair, Dist;
                                                                                                                              bfs.addLast(U[xx]);
 int nild;
                                                             Dist[u.id] = INF;
 public BiGraph(LinkedList<Node> L, LinkedList<Node> R){    return false;
                                                                                                                         }
   N = L.size(): M = R.size():
                                                                                                                       }
   this.L = L; this.R = R;
                                                           public HashMap<Integer, Integer> maxMatch() {
   U = new Node[N+M];
                                                             Pair = new int[M+N];
                                                                                                                      HashSet<Integer> K = new HashSet<>();
   for(Node n: L) U[n.id] = n;
                                                            Dist = new int[M+N];
                                                                                                                      for(Node n: L) if(!Z[n.id]) K.add(n.id);
                                                                                                                      for(Node n: R) if(Z[n.id]) K.add(n.id);
   for(Node n: R) U[n.id] = n:
                                                             for(int i = 0: i < M + N: i + +) {
                                                              Pair[i] = -1;
                                                                                                                      return K;
 private boolean bfs() {
                                                               Dist[i] = INF;
                                                                                                                 }
   LinkedList<Node> Q = new LinkedList<>();
    for(Node n: L)
                                                             HashMap<Integer, Integer> out = new HashMap<>();
                                                                                                                 3.3. Network Flow. The Floyd Warshall algorithm for de-
     if(Pair[n.id] == -1) {
                                                             while(bfs()) {
                                                                                                                 termining the maximum flow through a graph can be used
                                                              for(Node n: L) if(Pair[n.id] == -1)
       Dist[n.id] = 0;
                                                                                                                 for a lot of unexpected problems. Given a problem that can
       Q.add(n);
                                                                 dfs(n);
                                                                                                                 be formulated as a graph, where no ideas are found trying, it
     }else
                                                                                                                 might help trying to apply network flow. The running time is
       Dist[n.id] = INF;
                                                             for(Node n: L) if(Pair[n.id] != -1)
                                                                                                                 \mathcal{O}(C \cdot m) where C is the maximum flow and m is the amount
                                                               out.put(n.id, Pair[n.id]);
                                                                                                                 of edges in the graph. If C is very large we can change the
   nild = INF:
                                                             return out;
                                                                                                                 running time to \mathcal{O}(\log Cm^2) by only studying edges with a
   while(!Q.isEmpty()) {
                                                                                                                 large enough capacity in the beginning.
     Node u = Q.removeFirst();
                                                           public HashSet<Integer> minVTC() {
     if(Dist[u.id] < nild)</pre>
                                                            HashMap<Integer, Integer> Lm = maxMatch();
                                                                                                                 import java.util.*;
        for(Node v: u.ch) if(distp(v) == INF){
                                                            HashMap<Integer, Integer> Rm = new HashMap<>();
                                                                                                                  class Node {
         if(Pair[v.id] == -1)
                                                             for(int x: Lm.keySet()) Rm.put(Lm.get(x), x);
                                                                                                                   LinkedList<Edge> edges = new LinkedList<>();
            nild = Dist[u.id] + 1;
                                                             boolean[] Z = new boolean[M+N];
                                                                                                                   int id:
          else {
                                                            LinkedList<Node> bfs = new LinkedList<>():
                                                                                                                   boolean visited = false;
            Dist[Pair[v.id]] = Dist[u.id] + 1;
                                                             for(Node n: L) {
                                                                                                                   Edge last = null:
            Q.addLast(U[Pair[v.id]]);
                                                              if(!Lm.containsKey(n.id)) {
                                                                                                                   public Node(int id) {
         }
                                                                Z[n.id] = true;
                                                                                                                      this.id = id;
       }
                                                                 bfs.add(n);
                                                              }
                                                                                                                   public void append(Edge e) {
   return nild != INF;
                                                                                                                      edges.add(e);
                                                             while(!bfs.isEmpty()) {
 private int distp(Node v) {
                                                              Node x = bfs.removeFirst();
   if(Pair[v.id] == -1) return nild;
                                                               int nono = -1;
                                                                                                                  class Edge {
   return Dist[Pair[v.id]];
                                                              if(Lm.containsKey(x.id))
                                                                                                                   Node source, sink;
                                                                 nono = Lm.get(x.id);
                                                                                                                   int cap;
 private boolean dfs(Node u) {
                                                               for(Node v: x.ch) {
                                                                                                                   int id:
   for(Node v: u.ch) if(distp(v) == Dist[u.id] + 1) {
                                                                if(y.id == nono || Z[y.id]) continue;
                                                                                                                   Edge redge;
```

```
public Edge(Node u, Node v, int w, int id){
                                                                int residual = e.cap - flow.get(e.id);
                                                                                                                 LinkedList<Edge> min_cut(int s, int t) {
   source = u; sink = v;
                                                               if(residual>0 && !e.sink.visited) {
                                                                                                                   HashSet<Node> A = new HashSet<>():
                                                                                                                   LinkedList<Node> bfs = new LinkedList<>():
   cap = w:
                                                                  e.sink.visited = true:
   this.id = id;
                                                                  e.sink.last = e;
                                                                                                                   bfs.add(adi[s]);
 }
                                                                  active.addLast(e.sink);
                                                                                                                   A.add(adi[s]);
                                                                                                                   while(!bfs.isEmpty()) {
class FlowNetwork {
                                                             }
                                                                                                                     Node i = bfs.removeFirst();
 Node[] adi;
                                                                                                                      for(Edge e: i.edges) {
 int edgec = 0:
                                                            if(t.visited) {
                                                                                                                       int c = e.cap - flow.get(e.id):
                                                             LinkedList<Edge> res = new LinkedList<>();
 HashMap<Integer, Integer> flow = new HashMap<>();
                                                                                                                       if(c > 0 \&\& !A.contains(e.sink)) {
 ArrayList<Edge> real = new ArrayList<Edge>();
                                                              Node curr = t;
                                                                                                                         bfs.add(e.sink);
 public FlowNetwork(int size) {
                                                              while(curr != s) {
                                                                                                                         A.add(e.sink);
   adi = new Node[size]:
                                                               res.addFirst(curr.last):
                                                                                                                         if(e.sink.id == t) return null:
   for(int i = 0; i<size; i++) {
                                                               curr = curr.last.sink;
      adj[i] = new Node(i);
                                                                                                                     }
   }
                                                              return res;
                                                           } else return null:
                                                                                                                   LinkedList<Edge> out = new LinkedList<>();
 void add_edge(int u, int v, int w, int id){
                                                                                                                   for(Node n: A) for(Edge e: n.edges)
                                                                                                                       if(!A.contains(e.sink) && e.cap != 0)
   Node Nu = adi[u], Nv = adi[v];
   Edge edge = new Edge(Nu, Nv, w, edgec++);
                                                         int max_flow(int s, int t) {
                                                                                                                           out.add(e);
   Edge redge = new Edge(Nv, Nu, 0, edgec++);
                                                           Node source = adi[s];
                                                                                                                   return out;
   edge.redge = redge;
                                                           Node sink = adi[t];
   redge.redge = edge;
                                                           LinkedList<Edge> path = find_path(source, sink,
   real.add(edge);
                                                                    new LinkedList<Edge>());
   adj[u].append(edge);
                                                            while (path != null) {
                                                                                                                              4. Dynamic Programming
   adj[v].append(redge);
                                                              int min = Integer.MAX_VALUE;
                                                                                                               4.1. Longest Increasing Subsequence. Finds the
   flow.put(edge.id, 0);
                                                              for(Edge e : path) {
                                                                                                               longest increasing subsequence in an array in \mathcal{O}(n \log n)
   flow.put(redge.id, 0);
                                                               min = Math.min(min, e.cap - flow.get(e.id));
                                                                                                               time. Can easility be transformed to longest decreas-
 }
                                                                                                               ing/nondecreasing/nonincreasing subsequence.
                                                              for (Edge e : path) {
                                                               flow.put(e.id, flow.get(e.id) + min);
 void reset() {
                                                                                                               public static int lis(int[] X) {
   for(int i = 0; i<adj.length; i++) {
                                                               Edge r = e.redge;
                                                                                                                 int n = X.lenath:
      adj[i].visited = false; adj[i].last = null;
                                                               flow.put(r.id, flow.get(r.id) - min);
                                                                                                                 int P[] = new int[n];
                                                                                                                 int M[] = new int[n+1];
 }
                                                             path = find_path(source, sink,
                                                                                                                 int L = 0:
                                                                      new LinkedList<Edge>());
                                                                                                                 for(int i = 0: i < n: i + +) {
 LinkedList<Edge> find_path(Node s, Node t,
                                                                                                                   int lo = 1;
                                                           int sum = 0:
         List<Edge> path){
                                                                                                                   int hi = L;
   reset();
                                                           for(Edge e: source.edges) {
                                                                                                                   while(lo<=hi) {</pre>
   LinkedList<Node> active = new LinkedList<>();
                                                             sum += flow.get(e.id);
                                                                                                                      int mid = lo + (hi - lo + 1)/2:
   active.add(s);
                                                                                                                      if(X[M[mid]]<X[i])</pre>
   while(!active.isEmpty() && !t.visited) {
                                                            return sum;
                                                                                                                       lo = mid+1;
     Node now = active.pollFirst();
                                                                                                                      else
     for(Edge e: now.edges) {
                                                                                                                       hi = mid-1:
```

```
m = m + i - T[i];
    int newL = lo;
                                                                  i = T[i];
    P[i] = M[newL-1];
                                                                } else {
    M[newL] = i;
                                                                  i = 0;
    if (newL > L)
                                                                  m = m+1;
      L = newL;
                                                                }}}
                                                            return false;
  }
  int[] S = new int[L]:
  int k = M[L];
  for (int i = L-1; i >= 0; i--) {
    S[i] = k; //or X[k]
                                                          4.3. String functions. The z-function computes the longest
    k = P[k];
                                                          common prefix of t and t[i:] for each i in \mathcal{O}(|t|). The boarder
                                                          function computes the longest common proper (smaller than
  return L; // or S
                                                          whole string) prefix and suffix of string t[:i].
}
                                                          def zfun(t):
4.2. Knuuth Morris Pratt substring. Finds if w is a sub-
                                                              z = [0]*len(t)
array to s in linear time.
                                                              n = len(t)
//assumes s.length>=w.length
                                                              l, r = (0,0)
public static boolean kmp(int [] w, int [] s) {
                                                              for i in range(1,n):
                                                                  if i < r:
  int T[] = new int[w.length];
  T[0] = -1; T[1] = 0;
                                                                      z[i] = min(z[i-l], r-i+1)
  int m = 0, i = 2;
                                                                  while z[i] + i < n and t[i+z[i]] == t[z[i]]:
  while(i<w.length) {</pre>
                                                                      z[i]+=1
                                                                  if i + z[i] - 1 > r:
    if(w[i-1] == w[m]) {
      T[i] = ++m;
                                                                      l = i
      i++;
                                                                       r = i + z[i] - 1
    } else if (m>0) {
                                                              return z
      m = T[m];
    } else {
                                                          def matches(t, p):
                                                              s = p + '#' + t
      T[i] = 0:
      i++;
                                                              return filter(lambda x: x[1] == len(p),
                                                                       enumerate(zfun(s)))
    }
  }
```

m = 0; i = 0;

i++;

} else {

while(m+i<s.length){</pre>

 $if(w[i] == s[m+i]) {$

 $if(T[i] > -1) {$

if(i == w.length - 1)

return true; //m

def boarders(s):

return b

b = [0]*len(s)

k = b[i-1]

for i in range(1, len(s)):

k = b[k-1]

b[i] = k+1

if s[k] == s[i]:

while k>0 and s[k] != s[i]:

5.1. **System of Equations.** Solves the system of equations Ax = b by Gaussian elimination. This can for example be used to determine the expected value of each node in a markov

5. Etc

```
int N = b.length;
// Gaussian elimination with partial pivoting
for (int i = 0; i < N; i++) {
 // find pivot row and swap
  int max = i;
  for (int j = i + 1; j < N; j++)
      max = j;
  double[] tmp = A[i];
  A[i] = A[max];
  A[max] = tmp;
  double tmp2 = b[i];
  b[i] = b[max];
  b[max] = tmp2;
  // A doesn't have full rank
  if (Math.abs(A[i][i])<0.00001) return null;</pre>
  // pivot within b
  for (int j = i + 1; j < N; j++)
    b[i] -= b[i] * A[i][i] / A[i][i];
  // pivot within A
  for (int j = i + 1; j < N; j++) {
    double m = A[i][i] / A[i][i];
    for (int k = i+1: k < N: k++)
      A[j][k] -= A[i][k] * m;
    A[j][i] = 0.0;
// back substitution
double[] x = new double[N];
for (int j = N - 1; j >= 0; j - -) {
  double t = 0.0:
  for (int k = j + 1; k < N; k++)
    t += A[i][k] * x[k];
 x[j] = (b[j] - t) / A[j][j];
```

```
chain. Runns in \mathcal{O}(N^3).
//Computes A^{-1} * b
static double[] solve(double[][] A, double[] b) {
      if (Math.abs(A[j][i]) > Math.abs(A[max][i]))
```

}

```
return x;
}
```

5.2. Convex Hull. From a collection of points in the plane the convex hull is often used to compute the largest distance or the area covered, or the length of a rope that encloses the points. It can be found in $\mathcal{O}(N \log N)$ time by sorting the points on angle and the sweeping over all of them.

```
import java.util.*;
public class ConvexHull {
 static class Point implements Comparable<Point> {
    static Point xmin;
    int x, y;
    public Point(int x, int y) {
      this.x = x; this.y = y;
    public int compareTo(Point p) {
      int c = cross(this, xmin, p);
      if(c!=0) return c;
      double d = dist(this,xmin) - dist(p,xmin);
      return (int) Math.signum(d);
 static double dist(Point p1, Point p2) {
    return Math.hypot(p1.x - p2.x, p1.y - p2.y);
  static int cross(Point a, Point b, Point c) {
    int dx1 = b.x - a.x;
    int dy1 = b.y - a.y;
    int dx2 = c.x - b.x;
    int dy2 = c.y - b.y;
    return dx1*dv2 - dx2*dv1:
 Point[] convexHull(Point[] S) {
    int N = S.length;
    // find a point on the convex hull.
    Point xmin = S[0];
    int id = 0;
    for(int i = 0; i < N; i++) {
      Point p = S[i];
      if(xmin.x > p.x | |
         xmin.x == p.x \&\& xmin.y > p.y) {
       xmin = p;
```

id = i;

```
}
S[id] = S[N-1];
S[N-1] = xmin;
Point.xmin = xmin;
// Sort on angle to xmin.
Arrays.sort(S, 0, N-1);
Point[] H = new Point[N+1];
H[0] = S[N-2]:
H[1] = xmin;
for(int i = 0; i < N-1; i++)
 H[i+2] = S[i];
int M = 1:
// swipe over the points
for(int i = 2; i \le N; i++) {
  while(cross(H[M-1],H[M],H[i]) <= 0) {
    if(M>1)
      M--;
    else if (i == N)
      break:
    else
      i += 1:
  M+=1;
  Point tmp = H[M];
  H[M] = H[i];
 H[i] = tmp;
Point[] Hull = new Point[M];
for(int i = 0; i < M; i++)
 Hull[i] = H[i];
return Hull;
```

6. NP Tricks

6.1. MaxClique. The max clique problem is one of Karp's 21 NP-complete problems. The problem is to find the lagest subset of an undirected graph that forms a clique - a complete graph. There is an obvious algorithm that just inspects every subset of the graph and determines if this subset is a clique. This algorithm runns in $\mathcal{O}(n^22^n)$. However one can use the

meet in the middle trick (one step divide and conqurer) and reduce the complexity to $\mathcal{O}(n^2 2^{\frac{n}{2}})$.

```
static int max_clique(int n, int[][] adj) {
 int fst = n/2:
  int snd = n - fst;
 int[] maxc = new int[1<<fst];</pre>
 int max = 1:
  for(int i = 0; i < (1 << fst); i++) {
   for(int a = 0; a<fst; a++) {</pre>
      if((i&1<<a) != 0)
        maxc[i] = Math.max(maxc[i], maxc[i^(1<<a)]);
    boolean ok = true;
    for(int a = 0; a<fst; a++) if((i&1<<a) != 0) {
      for(int b = a+1; b<fst; b++) {</pre>
          if((i\&1 << b) != 0 \&\& adi[a][b] == 0)
              ok = false;
     }
   }
   if(ok) {
      maxc[i] = Integer.bitCount(i);
      max = Math.max(max, maxc[i]);
  for(int i = 0; i < (1 << snd); i++) {
   boolean ok = true;
    for(int a = 0; a<snd; a++) if((i&1<<a) != 0) {
      for(int b = a+1; b < snd; b++) {
        if((i&1<<b) != 0)
          if(adi[a+fst][b+fst] == 0)
            ok = false:
     }
   if(!ok) continue;
    int mask = 0:
    for(int a = 0; a<fst; a++) {</pre>
      ok = true;
      for(int b = 0; b < snd; b++) {
        if((i&1<<b) != 0) {
          if(adi[a][b+fst] == 0) ok = false;
       }
      if(ok) mask |= (1<<a);
```

7. Coordinate Geometry

7.1. **Area of a nonintersecting polygon.** The signed area of a polygon with n verticies is given by

$$A = \frac{1}{2} \sum_{i=0}^{n-1} (x_i y_{i+1} - x_{i+1} y_i)$$

7.2. **Intersection of two lines.** Two lines defined by

$$a_1x + b_1y + c_1 = 0$$
$$a_2x + b_2y + c_2 = 0$$

Intersects in the point

$$P = (\frac{b_1c_2 - b_2c_1}{w}, \frac{a_2c_1 - a_1c_2}{w}),$$

where $w = a_1b_2 - a_2b_1$. If w = 0 the lines are parallell.

7.3. Distance between line segment and point. Given a linesegment between point P, Q, the distance D to point R is given by:

$$\begin{split} a &= Q_y - P_y \\ b &= Q_x - P_x \\ c &= P_x Q_y - P_y Q_x \\ R_P &= \big(\frac{b(bR_x - aR_y) - ac}{a^2 + b^2}, \frac{a(aR_y - bR_x) - bc}{a^2 + b^2}\big) \\ D &= \begin{cases} \frac{|aR_x + bR_y + c|}{\sqrt{a^2 + b^2}} & \text{if } (R_{P_x} - P_x)(R_{P_x} - Q_x) < 0, \\ \min |P - R|, |Q - R| & \text{otherwise} \end{cases} \end{split}$$

7.4. **Picks theorem.** Find the amount of internal integer coordinates i inside a polygon with picks theorem $A = \frac{b}{2} + i - 1$, where A is the area of the polygon and b is the amount of coordinates on the boundary.

the Segment AB, the Ray AB and the line AB.

(distSeg, distHalfinf, distLine)

def distSegP(P, Q, R):

a, b, c = pts2line(P, Q)

```
Rpx, Rpy = project((a,b,c), R)
7.5. Implementations.
                                                          dp = min(dist(P, R), dist(Q, R))
                                                          dl = distl((a,b,c), R)
import math
                                                          if (inside(Rpx, P[0], Q[0]) and
                                                                  inside(Rpy, P[1], Q[1])):
# Distance between two points
def dist(p, q):
                                                            return (dl, dl, dl)
  return math.hypot(p[0]-q[0], p[1] - q[1])
                                                          if insideH((Rpx, Rpy), P, Q):
                                                            return (dp, dl, dl)
# Converts two points to a line (a, b, c),
                                                          return (dp. dp. dl)
# ax + by + c = 0
                                                        # Finds if A \ll i \ll B.
# if p == q, a = b = c = 0
                                                        def inside(i, A, B):
def pts2line(p, q):
                                                          return (i-A)*(i-B) <= 0
  return (-q[1] + p[1],
      q[0] - p[0],
      p[0]*q[1] - p[1]*q[0])
                                                        # Finds if a point i on the line AB
                                                        # is on the seament AB.
                                                        def insideS(i, A, B):
# Distance from a point to a line,
# given that a != 0 or b != 0
                                                          return (inside(i[0], A[0], B[0])
                                                            and inside(i[1], A[1], B[1]))
def distl(l, p):
  return (abs(l[0]*p[0] + l[1]*p[1] + l[2])
                                                        # Finds if a point i on the line AB
       /math.hypot(l[0], l[1]))
                                                        # is on the ray AB.
# intersects two lines.
                                                        def insideH(i, A, B):
                                                          return ((i[0] - A[0])*(A[0] - B[0]) \le 0
# if parallell, returnes False.
def inters(l1, l2):
                                                            and (i[1] - A[1])*(A[1] - B[1]) <= 0)
   a1,b1,c1 = l1
                                                        # Finds if segment AB and CD overlabs.
  a2,b2,c2 = 12
                                                        def overlap(A, B, C, D):
   cp = a1*b2 - a2*b1
                                                            if A[0] == B[0]:
  if cp != 0:
                                                                return __overlap(A[1], B[1], C[1], D[1])
     return ((b1*c2 - b2*c1)/cp, (a2*c1 - a1*c2)/cp)
                                                            else:
   else:
                                                                return __overlap(A[0], B[0], C[0], D[0])
     return False
                                                        # Helper functions
                                                        def \_overlap(x1, x2, x3, x4):
# projects a point on a line
def project(l, p):
                                                            x1, x2 = (min(x1,x2), max(x1, x2))
                                                            x3, x4 = (min(x3,x4), max(x3, x4))
  a. b. c = l
                                                            return x2 >= x3 and x1 <= x4
  return ((b*(b*p[0] - a*p[1]) - a*c)/(a*a + b*b),
      (a*(a*p[1] - b*p[0]) - b*c)/(a*a + b*b))
                                                        # prints a point
                                                        def p(P):
# Finds the distance between a point, and
                                                            print(str(P[0]) + ' ' + str(P[1]))
                                                        # prints common points between
  a, b, c = pts2line(P, Q)
                                                        # two segments AB and CD.
```

```
def SegSeg(A, B, C, D):
                                                           inside(iy, C[1], D[1])):
 eqa = A == B
                                                           p((ix, iy))
 eac = C == D
                                                            return True
 if ega and egc:
                                                          return False
   if A == C:
      p(A)
                                                       # Intersections between circles
      return True
                                                       def intersections(c1, c2):
    return False
                                                         x1, y1, r1 = c1
 if eac:
                                                         x2. v2. r2 = c2
                                                         if x1 == x2 and y1 == y2 and r1 == r2:
    eqa, A, B, C, D = (eqc, C, D, A, B)
 if ega:
                                                            return False
   l = pts2line(C, D)
                                                         if r1 > r2:
                                                           x1, y1, r1, x2, y2, r2 = (x2, y2, r2, x1, y1, r1) 8.2. TLE.
   if (l[0]*A[0] + l[1]*A[1] + l[2] == 0 and
                                                         dist2 = (x1 - x2)*(x1-x2) + (y1 - y2)*(y1 - y2)
      inside(A[0], C[0], D[0]) and
                                                          rsq = (r1 + r2)*(r1 + r2)
      inside(A[1], C[1], D[1])):
                                                         if dist2 > rsq or dist2 < (r1-r2)*(r1-r2):
      (A)q
      return True
                                                            return []
    return False
                                                          elif dist2 == rsa:
                                                           cx = x1 + (x2-x1)*r1/(r1+r2)
 A, B = tuple(sorted([A,B]))
                                                           cy = y1 + (y2-y1)*r1/(r1+r2)
 C, D = tuple(sorted([C,D]))
                                                            return [(cx, cy)]
 l1 = pts2line(A, B)
                                                          elif dist2 == (r1-r2)*(r1-r2):
 l2 = pts2line(C, D)
                                                            cx = x1 - (x2-x1)*r1/(r2-r1)
 if l1[0]*l2[1] == l1[1]*l2[0]:
                                                           cy = y1 - (y2-y1)*r1/(r2-r1)
    if \l1[0]*\l2[2] == \l1[2]*\l2[0]:
                                                            return [(cx, cy)]
      if overlap(A, B, C, D):
       if B == C:
                                                         d = math.sqrt(dist2)
          p(B)
                                                         f = (r1*r1 - r2*r2 + dist2)/(2*dist2)
          return True
                                                         xf = x1 + f*(x2-x1)
                                                         vf = v1 + f*(y2-y1)
        if D == A:
          p(A)
                                                         dx = xf - x1
          return True
                                                         dy = yf-y1
                                                         h = math.sqrt(r1*r1 - dx*dx - dy*dy)
        s = sorted([A,B,C,D])
        p(s[1])
                                                         norm = abs(math.hypot(dx, dy))
       p(s[2])
                                                         p1 = (xf + h*(-dy)/norm, yf + h*(dx)/norm)
        return True
                                                         p2 = (xf + h*(dy)/norm, yf + h*(-dx)/norm)
      else:
                                                         return sorted([p1, p2])
        return False
    else:
                                                       # Finds the bisector through origo
      return False
                                                       # between two points by normalizing.
 ix, iy = inters(l1, l2)
                                                       def bisector(p1, p2):
 if (inside(ix, A[0], B[0]) and
                                                         d1 = math.hypot(p1[0], p2[1])
                                                         d2 = math.hypot(p2[0], p2[1])
    inside(iy, A[1], B[1]) and
    inside(ix, C[0], D[0]) and
```

```
return ((p1[0]/d1 + p2[0]/d2),
        (p1[1]/d1 + p2[1]/d2))
```

8. Acieving AC on a solved problem

8.1. **WA**.

- Check that minimal input passes.
- Can an int overflow?
- Reread the problem statement.
- Start creating small testcases with python.
- Does cout print with high enough precision?
- Abstract the implementation.

- Is the solution sanity checked?
- Use pypy instead of python.
- Rewrite in C++ or Java.
- Can we apply DP anywhere?
- To minimize penalty time you should create a worst case input (if easy) to test on.

8.3. **RTE.**

- Recursion limit in python?
- Arrayindex out of bounds?
- Division by 0?
- Modifying iterator while iterating over it?
- Not using a well definied operator for Collections.sort?
- If nothing makes sense and the end of the contest is approaching you can binary search over where the error is with try-except.

8.4. MLE.

- Create objects outside recursive function.
- Rewrite recursive solution to itterative with an own stack.