

Theory and Practice of Finite Element Methods

Shared memory parallelisation Tasks, WorkStream

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Aims for this module

- Identify parts / blocks of code that are (easily) parallelizable
- Learn how to parallelize using
 - Threads (Posix threads)
 - Tasks (Intel TBB)
 - WorkStream (Threaded building blocks)







Reference material

- Tutorials
 - https://dealii.org/current/doxygen/deal.ll/step_9.html
 - https://dealii.org/current/doxygen/deal.ll/step_13.html
 - http://www.math.colostate.edu/~bangerth/videos.676.39.html
 - http://www.math.colostate.edu/~bangerth/videos.676.40.html
- Documentation:
 - https://dealii.org/current/doxygen/deal.ll/group_threads.html
 - https://www.dealii.org/current/doxygen/deal.II/namespaceWorkStream.html
 - https://dealii.org/current/doxygen/deal.ll/namespaceparallel.html







Identifying parallelizable code

Consider this example:

```
template <int dim>
void MyProblem<dim>::setup_system (){
  dof handler.distribute dofs();
  DoFTools::make_hanging_node_constraints (...);
  DoFTools::make_sparsity_pattern (...);
VectorTools::interpolate_boundary_values (...);
```

- Operations (1,2,3) are independent of one another
 - Could be reordered without consequence







Identifying parallelizable code

"Embarrassingly parallelizable tasks"

```
template <int dim>
void MyProblem<dim>::assemble system () {
for (auto cell : dof_handler.active_cells()) {
  fe values.reinit (cell);
  ... assemble local contribution...
  ...copy local contribution into global matrix/rhs vector...
```

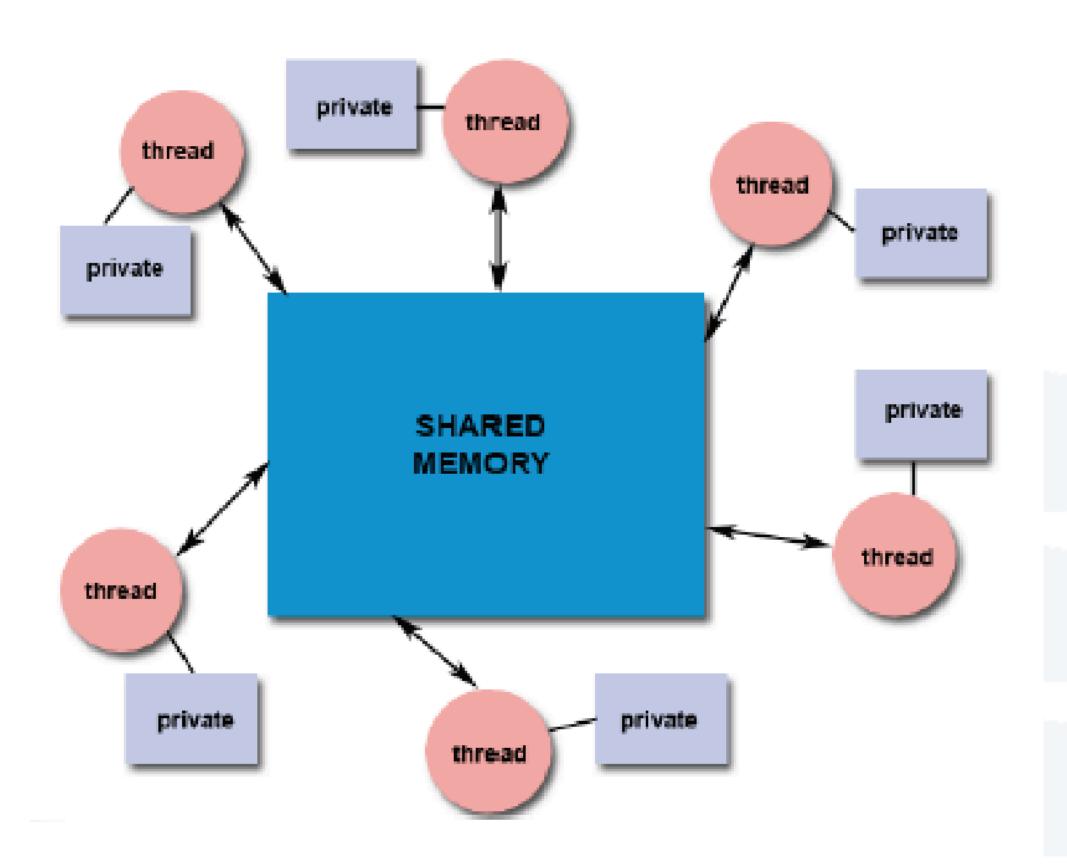
- Many more cells than machine cores
- Computations of local matrices/vectors are mutually independent
- Accumulation into global system matrix/vector is not!







Shared memory model



- All threads have access to the same global shared memory.
- Threads also have their own private memory.
- Shared data is accessible by all threads.
- Private data can be only accessed by the thread that owns it.
- Programmers are responsible for synchronizing access (protecting) globally shared data.

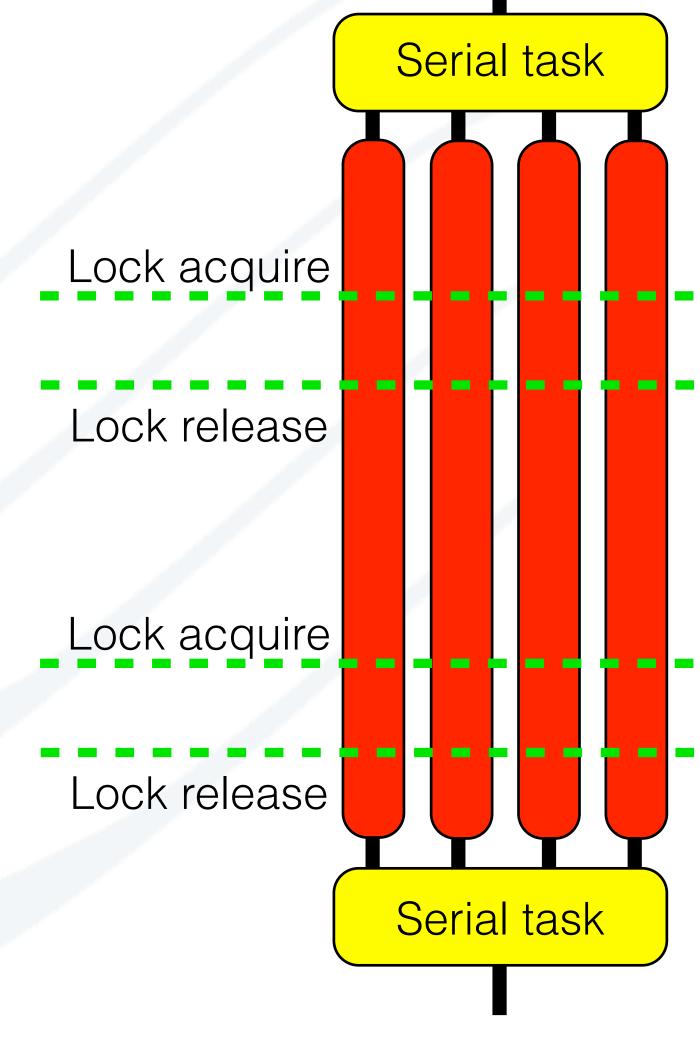






Independent threaded tasks: Option 1

- Code divergence with / without barriers (global / in-thread locks)
- Best used for small number of completely independent tasks
- Inside each thread: Shared data
 - Reading is a safe operation!
 - Use locks to allow data writing
 - Convergence point for threads (bottleneck)
 - Potential for deadlocks









Information about the system

```
MultithreadInfo::n_cores()
MultithreadInfo::n_threads()
MultithreadInfo::set_threads_limit()
```

- Query number of cores, and number of enabled threads
- Set maximum number of threads you want to "spawn"







Creating independent threaded tasks: the Threads class

- The call to join() is a blocking call
- Waits for the thread to finish before continuing







Creating independent threaded tasks: the ThreadGroup class

- Why is this inefficient?
- How do we prevent data races?





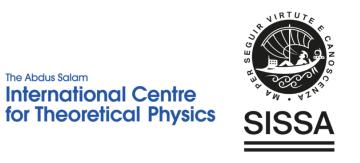


Creating independent threaded tasks: Ranged based assembly

• Less threads created = more efficient

```
void MyProblem<dim>::assemble on cell range (
  cell_iterator &range_begin,
  cell_iterator &range_end) {...};
void MyProblem<dim>::assemble_system () {
  Threads::ThreadGroup<void> threads;
  std::vector<std::pair<cell iterator, cell iterator> >
    sub_ranges = Threads::split_range
      dof_handler.begin_active(),
      dof handler.end(),
      n_virtual_cores);
  for (t=0; t<n_virtual_cores; ++t)</pre>
    threads += Threads::new_thread
      &MyProblem<dim>::assemble on cell range,
      this,
      sub_ranges[t].first,
      sub_ranges[t].second);
  threads.join_all ();}
```







Independent threaded tasks

```
void MyProblem<dim>::assemble_on_one_cell (cell_iterator &cell) {
  static Threads::Mutex mutex;
  mutex.acquire ();
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)</pre>
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)</pre>
      system_matrix.add (dof_indices[i], dof_indices[j],
                          cell_matrix(i,j));
  ... same for rhs...
  mutex.release ();
```

How do we prevent data races?



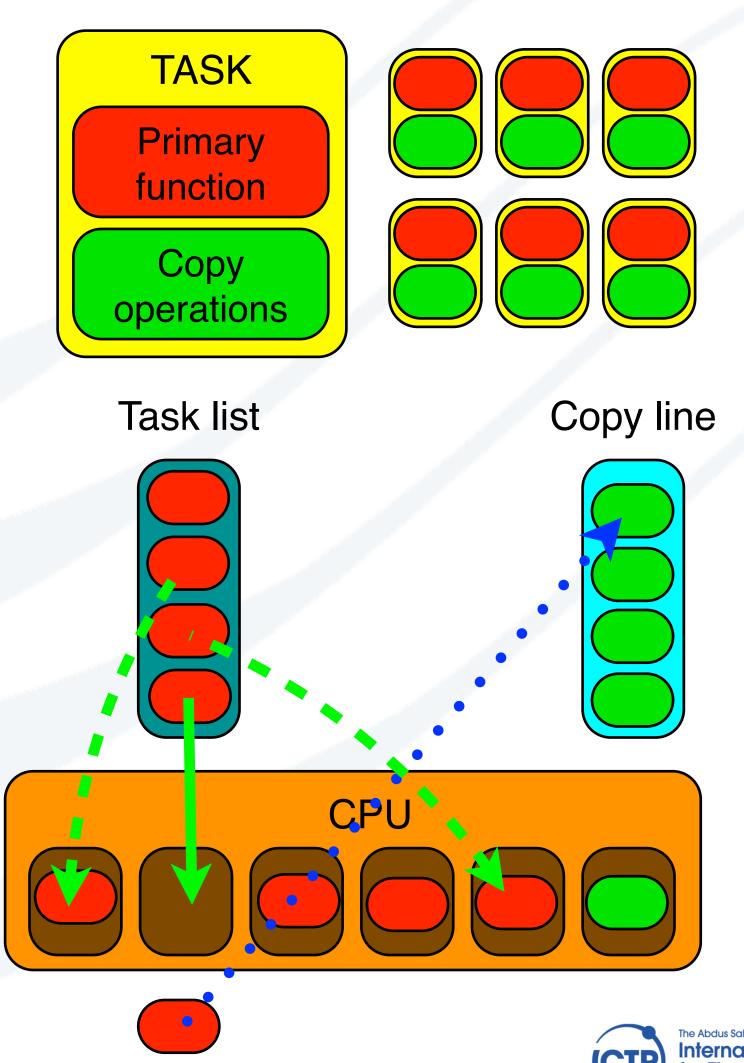




Creating independent threaded tasks: the WorkStream class

- Task-based threading
 - Continuous use of free CPU cores
 - Create a list of tasks
 - When core free, use it to perform next task
 - Expensive operations continually executed
 - Perform blocking tasks independently
 - Data copied to shared objects serially
 - Optimizations:
 - "Automatic" load balancing
 - Overhead reduction: Works on data chunks









Creating independent threaded tasks: parallelization of (per-cell) assembly

```
template <int dim>
void MyClass<dim>::assemble on one cell (
   const typename DoFHandler<dim>::active_cell_iterator &cell)
                                                                          Expensive constructor call
 FEValues<dim> fe_values (...);
 FullMatrix<double> cell_matrix (...);
                                                                         Repeated memory allocation
  Vector<double>
                     cell rhs (...);
  std::vector<double> rhs values (...);
 rhs_function.value_list (...)
  // assemble local contributions
 fe values.reinit (cell);
                                                                          Independent tasks
 for (unsigned int i=0; i<fe.dofs_per_cell; ++i)</pre>
    for (unsigned int j=0; j<fe.dofs per cell; ++j)
      for (unsigned int q=0; q<n points; ++q)
        cell_matrix(i,j) += ...;
  ... same for cell rhs...
  // now copy results into global system
  std::vector<unsigned int> dof_indices (...);
  cell->get_dof_indices (dof indices);
  for (unsigned int i=0; i<fe.dofs per cell; ++i)
    for (unsigned int j=0; j<fe.dofs per cell; ++j)
                                                                          Serial operation
      system matrix.add (...);
  ...same for rhs...
  // or constraints.distribute local to global (...);
                                                                                                       for Theoretical Physics
```





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Threading using WorkStream: the ScratchData class

- Assistant struct / class
- Contains reused data structures
 - FEValues objects
 - Helper vectors and storage containers
 - Precomputed data
- Needs a constructor and a copy constructor
 - Some objects must be manually reconstructed
 - We create one initial instance of the class
 - TBB duplicates as required (queue_length)

```
struct ScratchData {
  std::vector<double>
                            rhs_values;
                            fe_values;
  FEValues<dim>
  ScratchData (
    const FiniteElement<dim> &fe,
    const Quadrature<dim>
                             &quadrature,
    const UpdateFlags
                              update flags)
    : rhs_values (quadrature.size()),
      fe values (fe, quadrature, update flags)
    {}
   ScratchData (const ScratchData &rhs)
   : rhs_values (rhs.rhs_values),
     fe_values (rhs.fe_values.get_fe(),
                rhs.fe_values.get_quadrature(),
                rhs.fe values.get update flags())
    {}
```







Threading using WorkStream: the PerTaskData class

- Contains data structures required for serial operations
 - Multiple copies made (queue_length*chunk_size)
 - Must be "self-contained"
- Used in two places
 - Threaded function
 - Bound to an instance of the threaded function
 - Used as a "data-in" object
 - Serial function
 - A used instance is passed to this function
 - Used as a "data-out" object







Threading using WorkStream: Revised assembly

```
template <int dim>
void MyClass<dim>::assemble on one cell (
   const typename DoFHandler<dim>::active_cell_iterator &cell,
   ScratchData &scratch,
   PerTaskData &data)
  // reinitialise data
  scratch.fe values.reinit (cell);
  rhs function.value list (scratch.fe values.get quadrature points,
                            scratch.rhs_values);
  data.cell_matrix = 0;
  data.cell_rhs
                   = 0;
  // assemble local contributions
  for (unsigned int i=0; i<fe.dofs_per_cell; ++i)</pre>
    for (unsigned int j=0; j<fe.dofs_per_cell; ++j)</pre>
      for (unsigned int q=0; q<fe_values.n_quadrature_points; ++q)</pre>
        data.cell_matrix(i,j) += ...;
```

Now use objects contained within ScratchData and PerTaskData structs







Threading using WorkStream: Serial copy operation

- Uses writes "fixed" data in PerTaskData to single class object system_matrix (and whatever else)
- Has to be a serially performed operation







Threading (not) using WorkStream: Manual assembly using these data structures

- This performs the same serial assembly as we had before
 - More efficient though (use of ScratchData)







Threading using WorkStream

```
ScratchData scratch data (...);
PerTaskData per_task_data (...);
WorkStream::run ( dof_handler.begin_active(),
                  dof handler.end(),
                  *this,
                  &MyClass::assemble_system_one_cell,
                  &MyClass::copy local to global,
                  scratch_data,
                  per task data );
```

- Execute function in threaded manner
- Only operates on functions with a specific prototype
 - Theadable function: void function_name(cell, scratch, per_task_data)
 - Serial function: void function_name(per_task_data)







Workstream

https://www.dealii.org/current/doxygen/deal.II/namespaceWorkStream.html

NOTE: If your data objects are large, or their constructors are expensive, it is helpful to keep in mind that queue_length copies of the ScratchData object and queue_length*chunk_size copies of the CopyData object are generated.



