

Dose and schedule -dependence of Antibody Dependent Cell-mediated Cytotoxicity (ADCC) capacity and efficiency

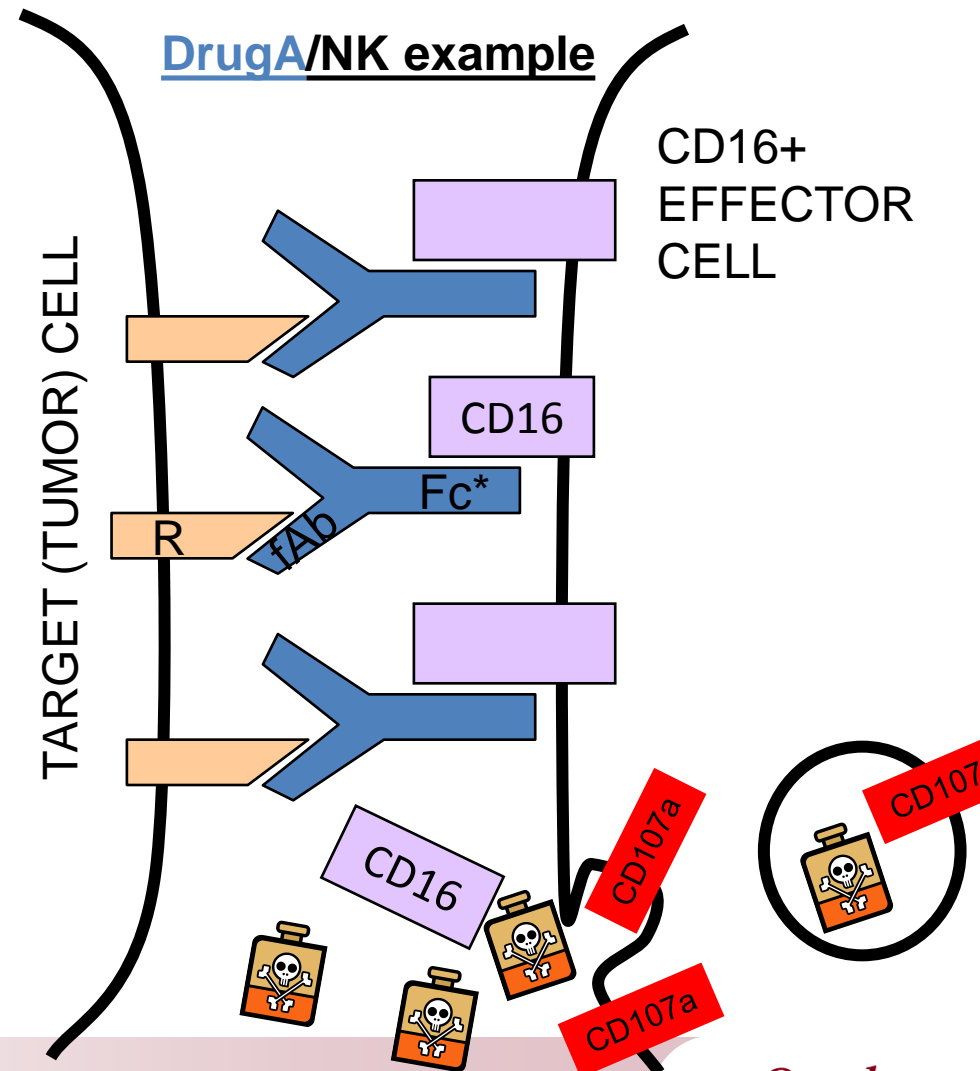
Dean C Bottino
on behalf of the ADCC in GlycoMabs
working group
19 June 2013

Acknowledgements & main collaborators

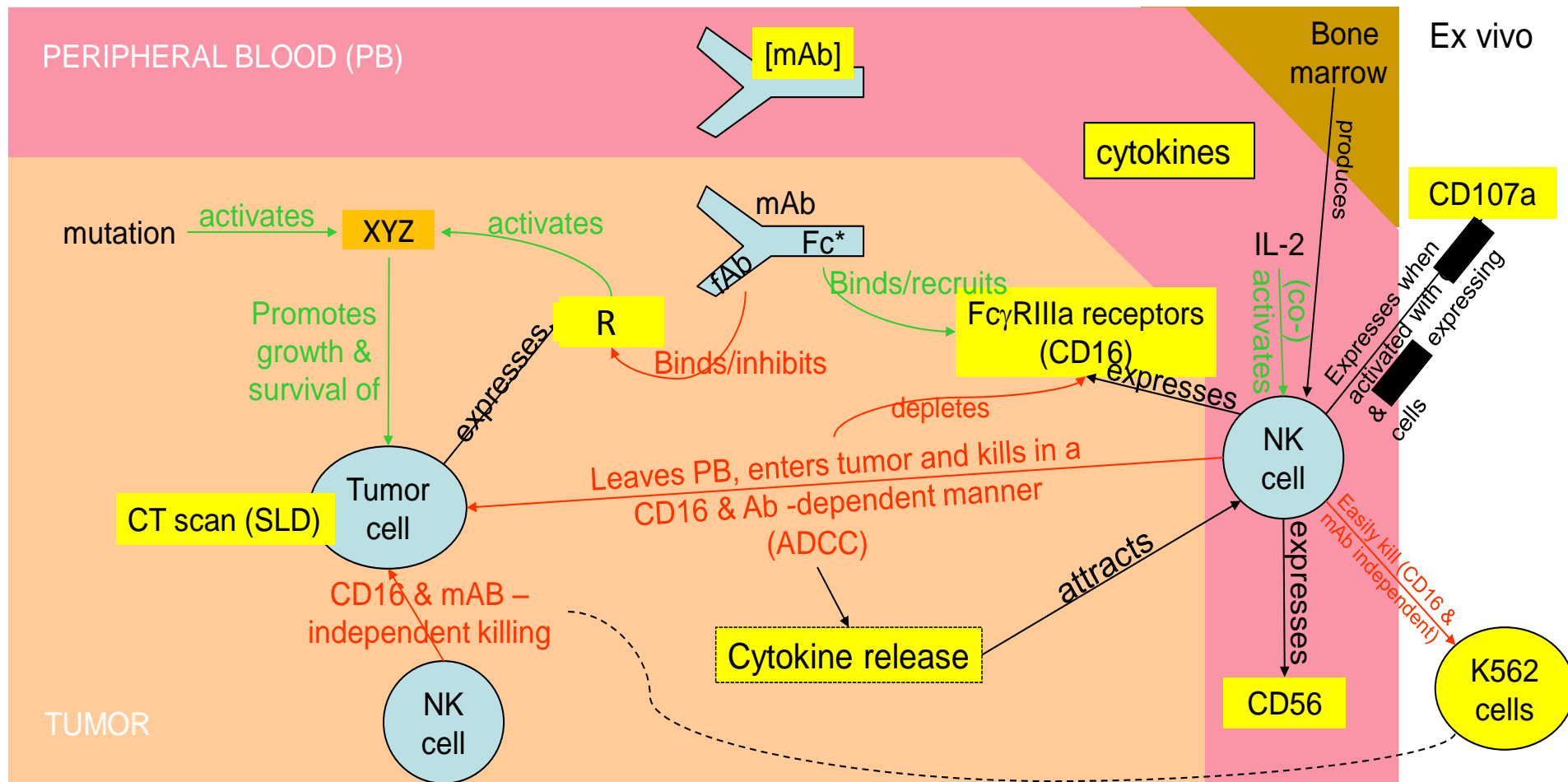
- **Sylvia Herter**, Roche Glycart cell biology
- **Marion Ott**, onc translational medicine
- **Marina Bacac**, Roche Glycart cell biology
- **Cheikh Diack**, clinical pharmacology
- **David Carlile**, clinical pharmacology
- **Eliezer Shochat**, clinical pharmacology
- **Alex Passioukov**, onc translational medicine

ADCC background/definitions

- ADCC = **A**ntibody **D**ependent **C**ell-mediated **C**ytotoxicity
- ADCC in cancer:
 1. mAb's variable region (fAb) binds to Receptor on tumor cell.
 2. A **N**atural **K**iller (NK) cell or **m**acrophage (MΦ) binds to the mAb's Fc
 3. Release of cytotoxins and death of the target cell
- Many anti-signaling mAbs may also elicit ADCC
- Glycoengineering the Fc domain → ↑affinity to Fc receptors (FcγRIIIa = CD16) on NK & MΦ's

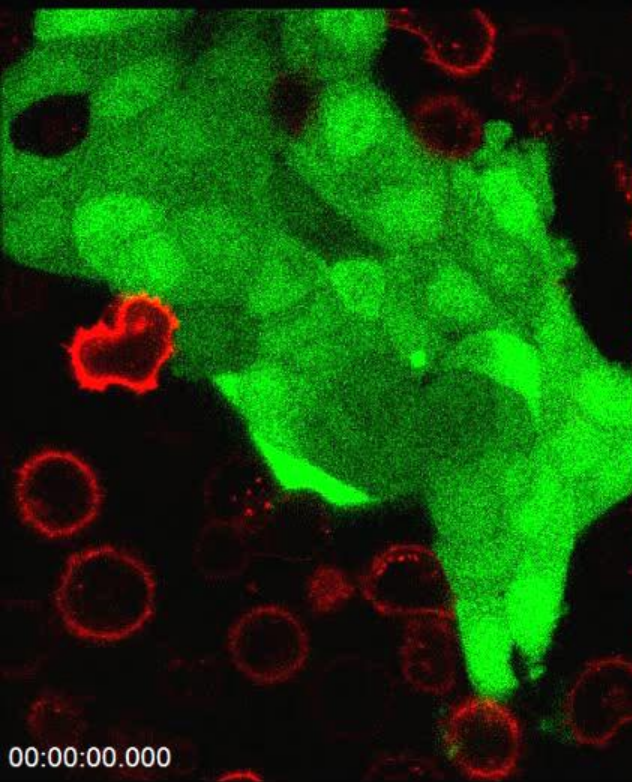


Graphical model of NK-mediated ADCC

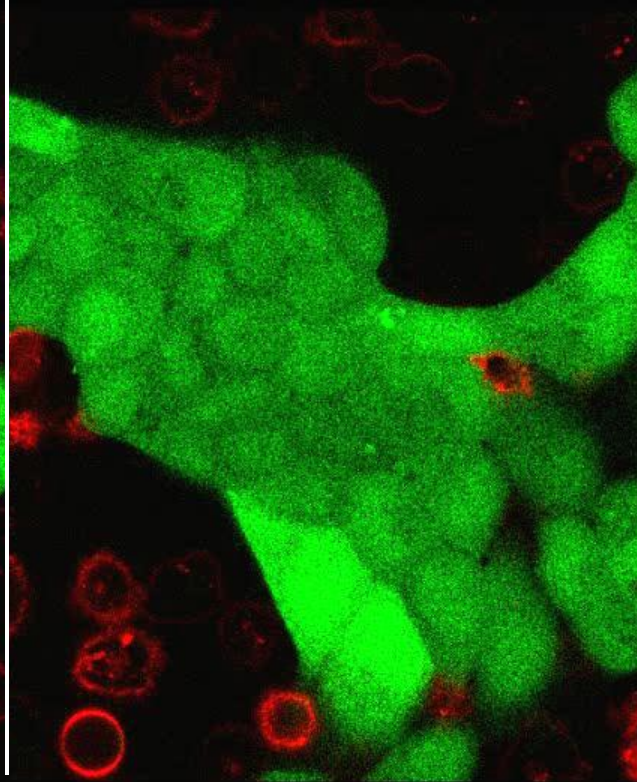


Comparison: ADCC induction by Glycomab vs other mAbs

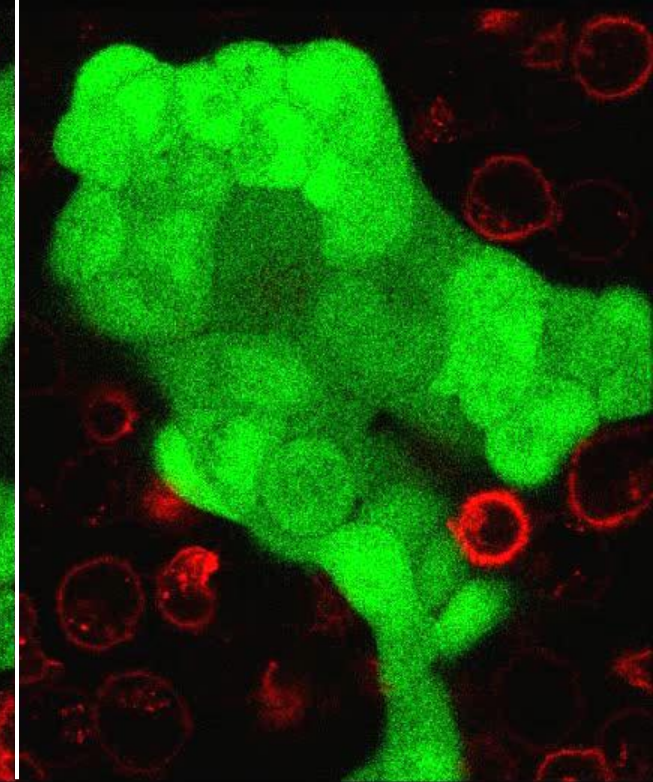
GlycoMab



OlderMab



OtherMab

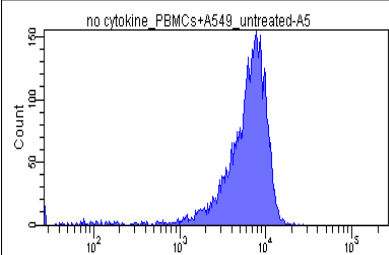


Experimental Conditions:

- T/E ratio = 1:2
- c [mAbs] = 200ng/ml
- YYY tumor cell labeled with green viability marker CMFDA (2 μ M for 30min prior to exp.)
- NK cells labeled with red cell tracker PKH26 (2 μ M for 3 min)
- YYY cells grown on glass bottom culture dishes, then first add NK cells, wait a few min, then add antibody)
- Experiments performed by O. Mundigl, PLBDB

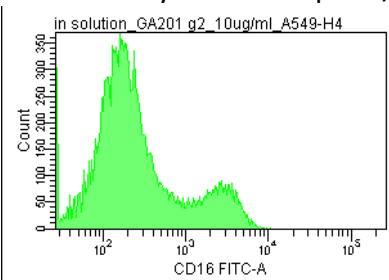
Kinetics of CD16 expression recovery after ADCC (From S. Herter & M. Bacac)

before
ADCC
 $T < 0$

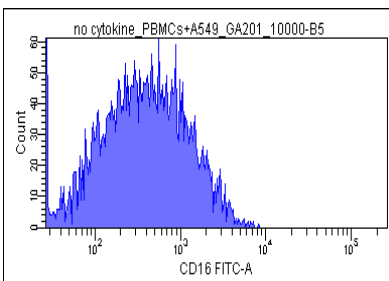


X axis = intensity \sim # of receptors/cell

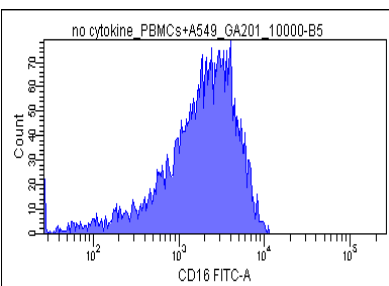
ADCC
3h



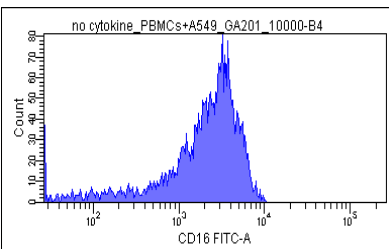
25 h



47 h



73 h



$T < 0$

$T = 0$

$T = 3h$

$T = 25h$

$T = 47h$

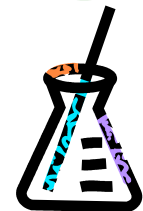
$T = 73h$

Donor provides
2ml blood,
PBMCS isolated

PBMCS put in medium
with XXX (target) cells and
DrugA

PBMCS washed (Drug A
and XXX removed)

PBMCS "recover" from
ADCC



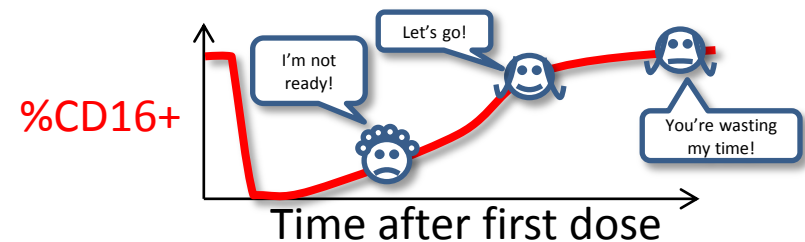
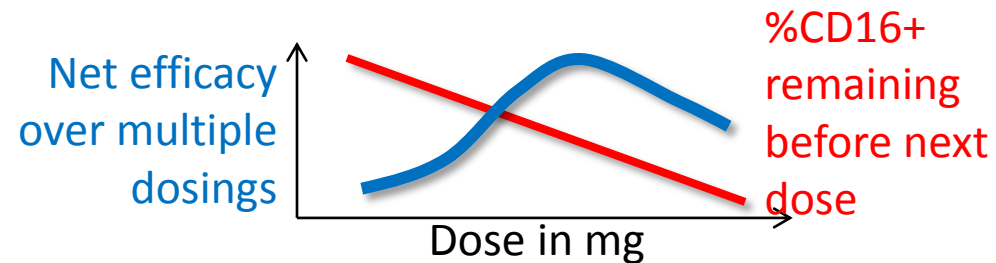
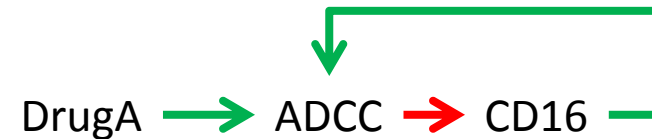
Gating color code

GREEN = "P2" = $CD3^-/CD56^{dim}$ ('worker' NKs)

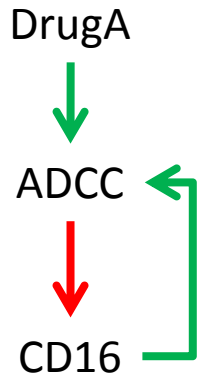
BLUE = "P3" = $CD3^-/CD56^{dim}/PI^-$ (still alive)

Motivating clinical questions

- Given that:
 - DrugA stimulates ADCC
 - ADCC transiently depletes CD16 on effector cells
 - CD16 is required for ADCC
- Can a lower DrugA dose actually give us better anti-tumor efficacy than a higher dose?
- Can a longer gap between DrugA doses give us better anti-tumor efficacy?
- Can we lower the dose from the recommended dose without losing efficacy?



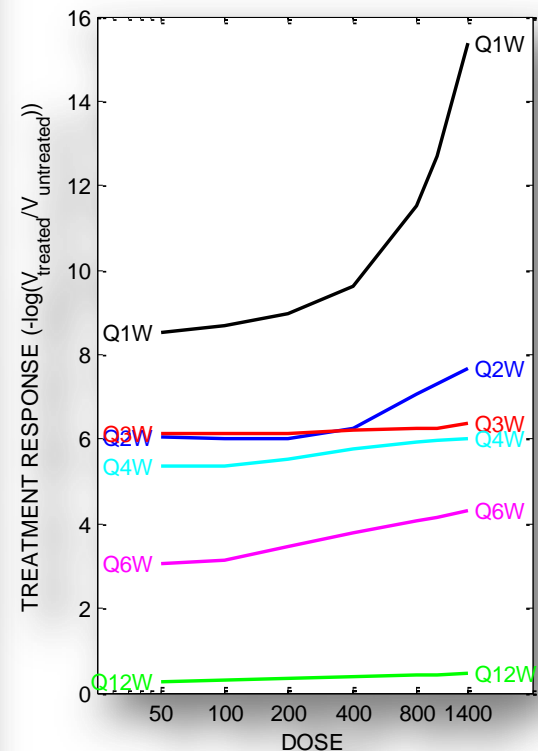
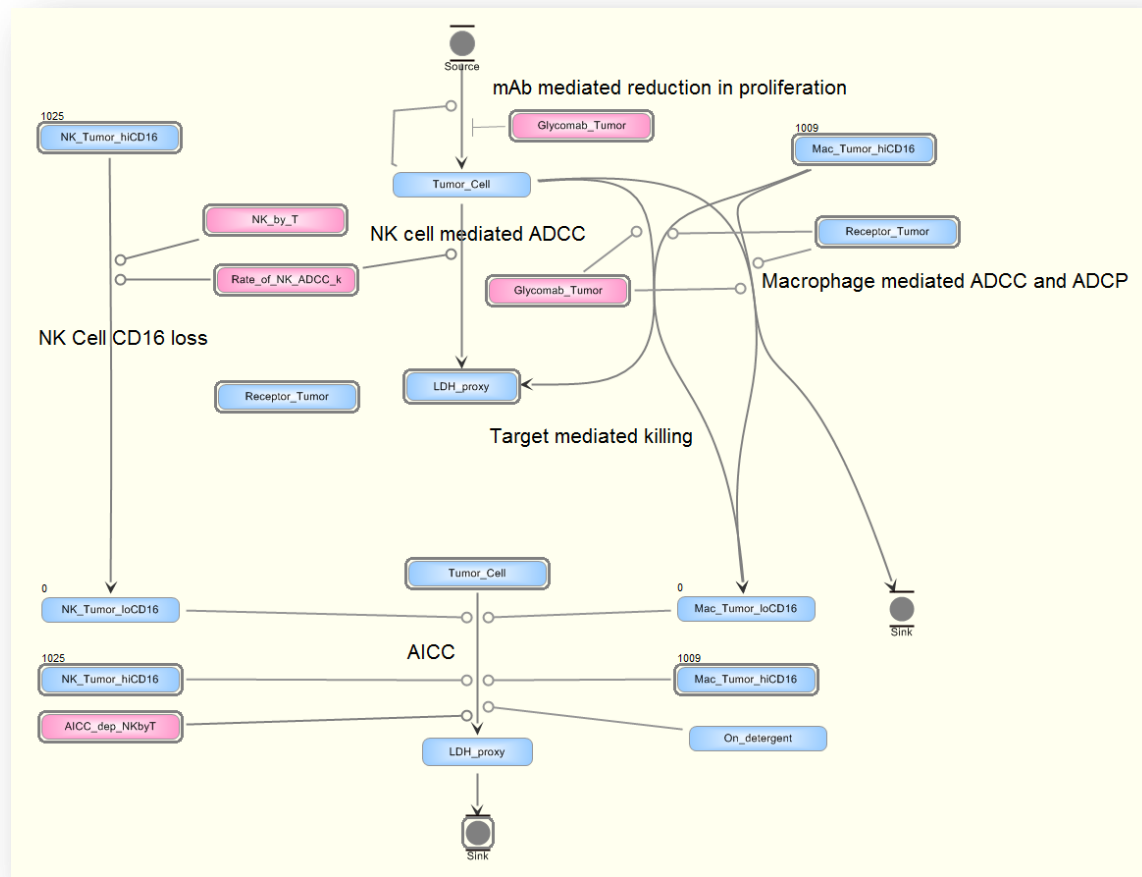
Related modeling questions

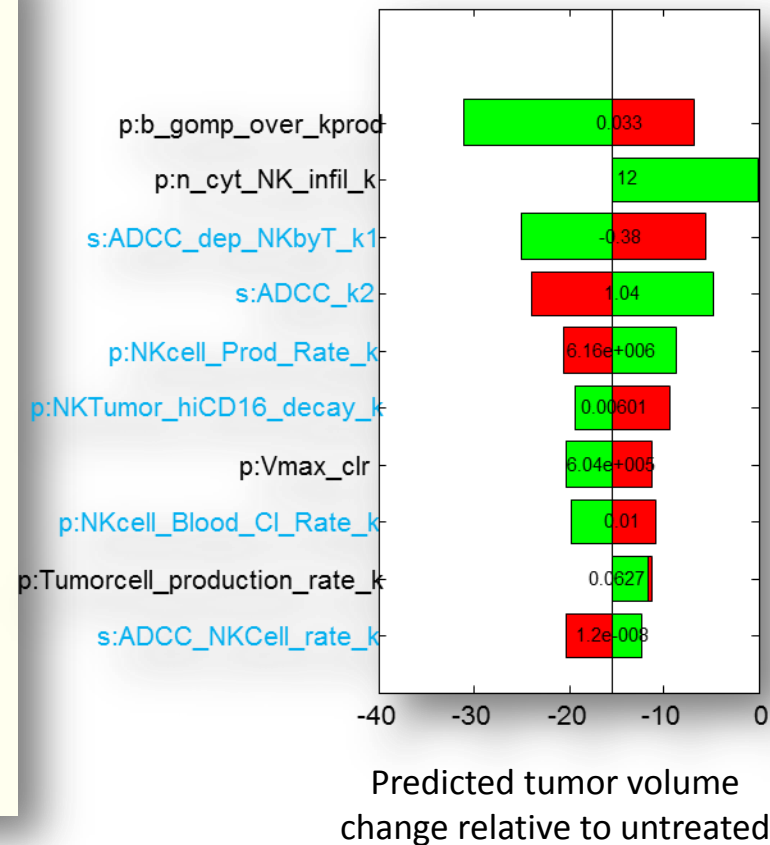


- Given a mathematical model based on:
 - In vitro concentration-dependent % ADCC killing data
 - In vitro %CD16+ depletion & recovery kinetic observations
 - In vitro “second ADCC” cell killing observations
 - Clinical DrugA population PK modeling
- Are there any physiologically reasonable parameter ranges for which the model predicts:
 - A bell-shaped dose-efficacy relationship?
 - Better efficacy from a longer dosing interval?
- If the model can be qualified for this purpose, is the predicted dose-response relationship flat in the dose range of interest?
- What are the major drivers of efficacy? Is dose one of them?

Let's ask the mechanistic model...

...developed in collaboration with Rosa Drug Development Partners





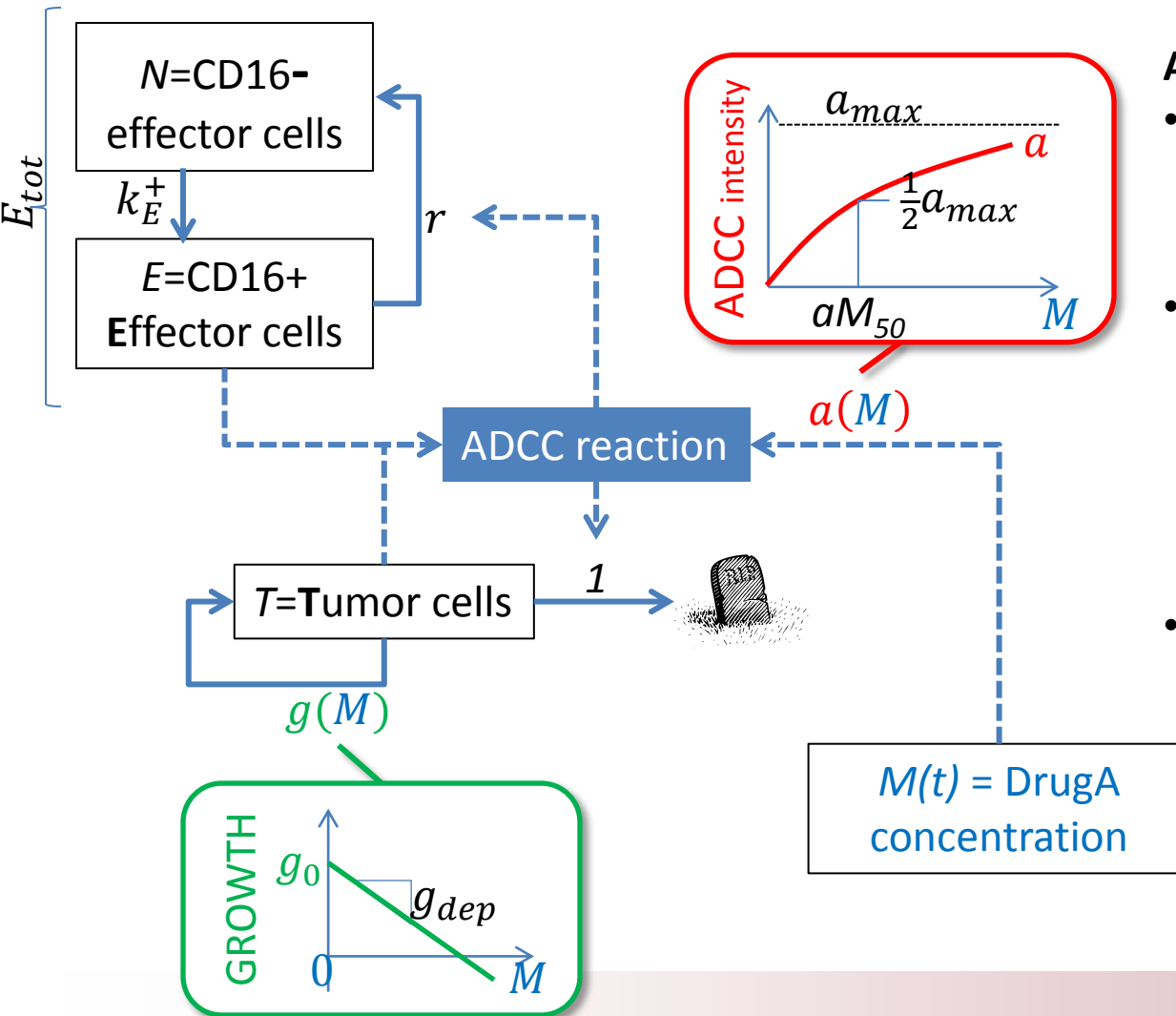
WorkFlow

1. Specify structural model & assumptions
2. Using data from in vitro assays with HV blood:
 1. Fit to ADCC & CD16 [DrugA]-response data
 2. Fit to ADCC & CD16 kinetic/recovery data (not yet done)
 3. Predict 2nd ADCC experiments, compare to data
3. Extrapolate to clinical scenario:
 1. Use popPK model & additional assumptions to predict $M(t)=[DrugA]_{tumor}$ over a range of doses & schedules
 2. Use $M(t)$ to 'drive' in vitro ADCC model & predict %CD16+ and tumor kill kinetics over several cycles
4. Assess whether bell-shaped dose-efficacy is predicted or whether waiting longer between doses is predicted to increase efficacy

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Simple cellular ADCC model: schematic



ASSUMPTIONS

- CD16+ effector cells (E) are produced/recover at a constant rate k_E^+ . $N+E = E_{tot}$ assumed constant.
- Absent ADCC, tumor cells (T) proliferate exponentially at a net rate g , which can be attenuated by Receptor inhibition as a function of $[mAb]=M$. ADCC effects are implicit in g_0 .
- In the presence of E and mAb, ADCC can occur at an $[mAb]=M$ dependent rate $a(M(t))ET$. Each ADCC reaction results in loss of one tumor cell and r CD16+ effector cells.

Simple cellular ADCC model: equations

pre-treatment

$$N = E_{tot} - E$$

First order
conversion of
CD16- to
CD16+ cells

Rate of change
of CD16+
Effector cells

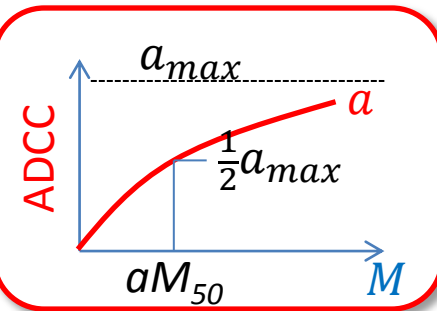
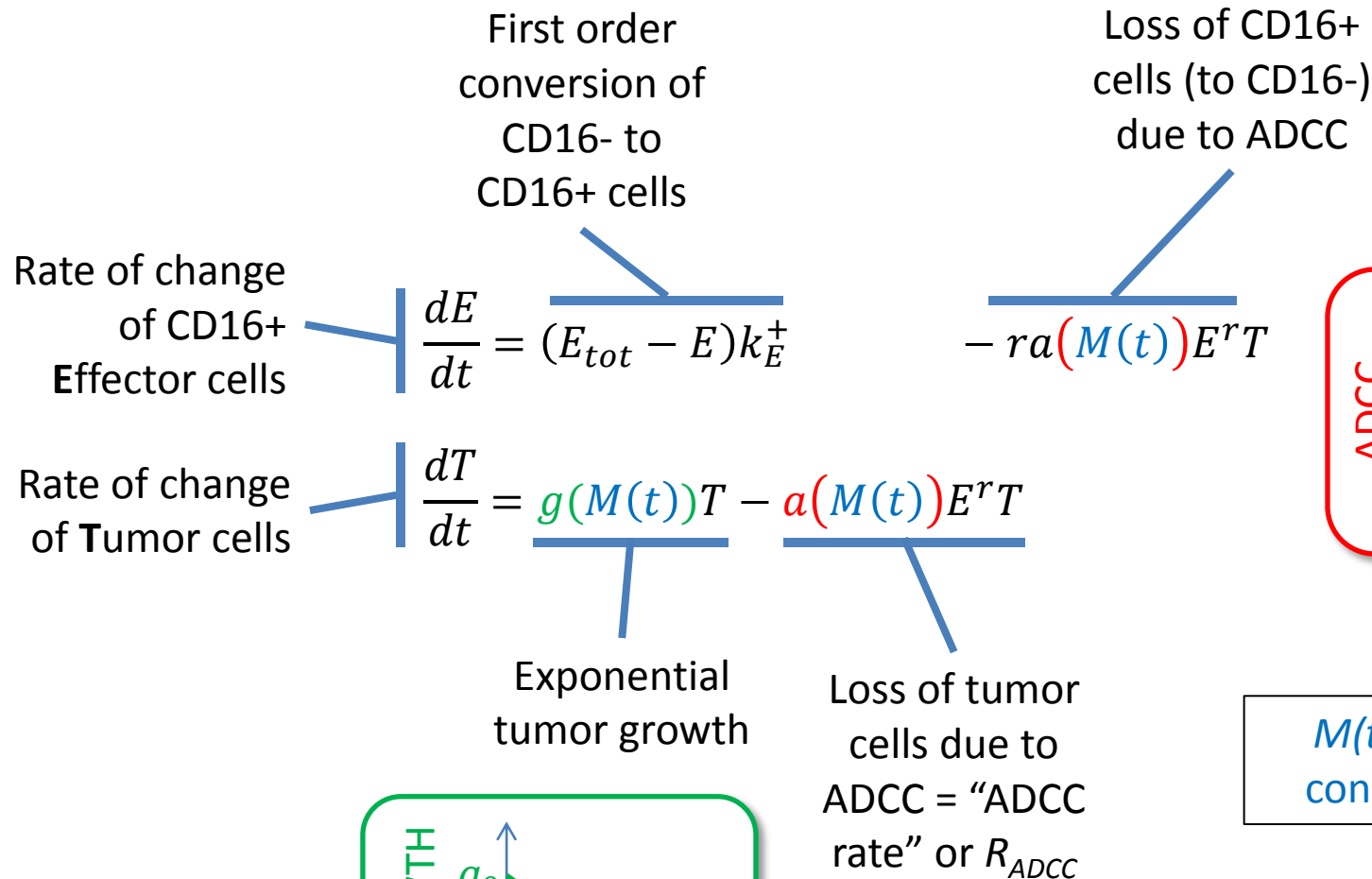
$$\frac{dE}{dt} = (E_{tot} - E)k_E^+$$

Rate of change
of Tumor cells

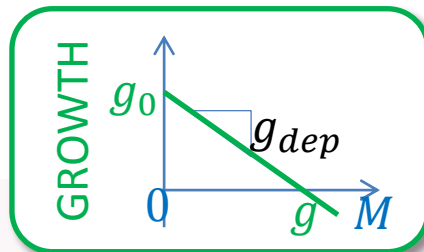
$$\frac{dT}{dt} = g_0 T$$

Exponential
tumor growth

Simple cellular ADCC model: equations on DrugA treatment



$M(t)$ = DrugA concentration



Simple cellular ADCC model: equations on DrugA treatment in XYZ^{mut}

First order
conversion of
CD16- to
CD16+ cells

Loss of CD16+
cells (to CD16-)
due to ADCC

Rate of change
of CD16+
Effector cells

$$\frac{dE}{dt} = (E_{tot} - E)k_E^+$$

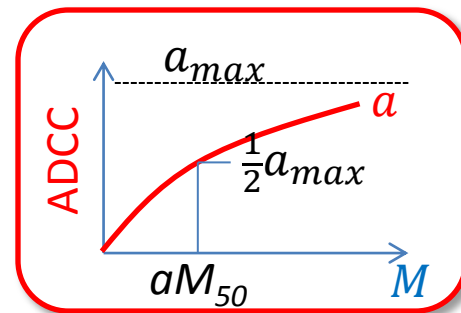
$$-ra(M(t))E^rT$$

Rate of change
of Tumor cells

$$\frac{dT}{dt} = g_0T - a(M(t))E^rT$$

Exponential
tumor growth
unaffected by
[mAb] in XYZ
mutant setting

Loss of tumor
cells due to
ADCC = "ADCC
rate" or R_{ADCC}



$M(t)$ = DrugA
concentration

Variables & parameters

$$\frac{dE}{dt} = (E_{tot} - E)k_E^+ - ra(M(t))E^rT$$

$$\frac{dT}{dt} = g(M(t))T - a(M(t))E^rT$$

	alias	Description	Units
E	E	#/vol of CD16+ Effector cells (state variable)	Cells (/vol)
T	T	#/vol of viable Tumor (target) cells (state variable)	Cells (/vol)
$M(t)$	mab	mAb concentration in tumor as function of time	ng/ml
E_{tot}	Etot	Total number of (CD16+ and CD16-) effector cells	Cells (/vol)
k_E^+	kEprod	Production/recovery rate of CD16+ Effector cells	1/day
r	r	Ratio: # of CD16+ cells depleted per tumor cell killed	1
a_{max}	amax	Maximum ADCC intensity as $M \rightarrow \infty$	1/(cells x day)
am_{50}	am50	mAb concentration giving 50% of max ADCC intensity	ng/ml
g_0	g0	Intrinsic tumor growth rate (including AICC offset)	1/day

Summary of model assumptions

- **Closed system:** Effector cells are neither destroyed nor replaced
- **ADCC interaction:** ADCC occurs when r ($r \sim 1$) CD16+ cells encounter a tumor cell in the presence of mAb and cytokines. A single ADCC reaction kills one tumor cell and converts r CD16+ cells to CD16-.
- **CD16 Recovery:**
 - CD16- cells can return to CD16+ (1st order).
 - CD16-/ + gating equivalent to ADCC incompetence/competence

This system of ODE's exhibits bi-stable behavior depending on the ratio ϕ of tumor growth rate g_0 to ADCC intensity a and total effector cell number E_{tot}

Nondimensionalized ODEs (r=1):

$$\frac{de}{d\tau} = 1 - e - \gamma_1 eu$$

$$\frac{du}{d\tau} = \gamma_2 u - \gamma_3 eu$$

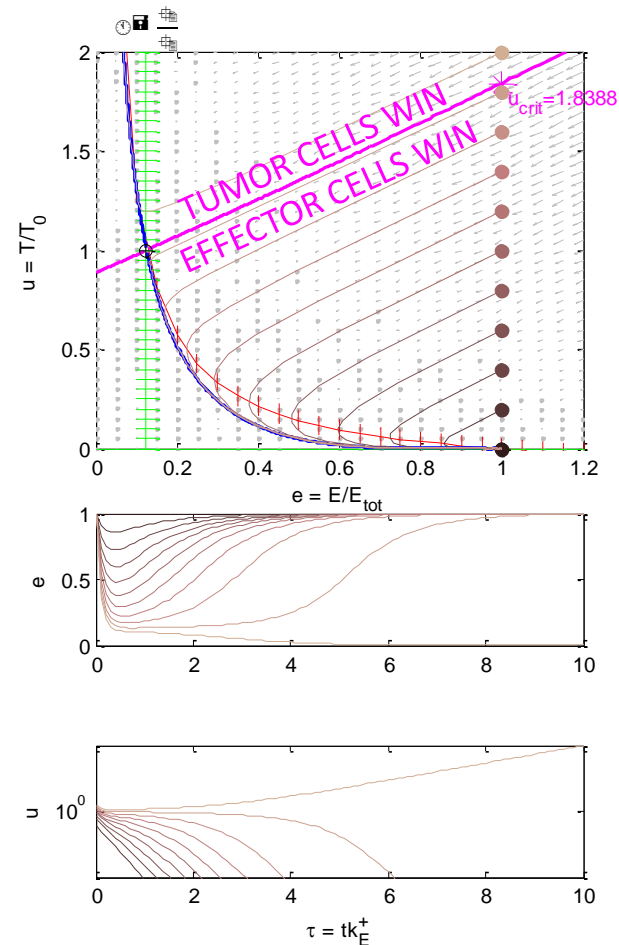
Where:

$$e = \frac{E}{E_{tot}}, u = \frac{T}{T_0}, \tau = k_E^+ t,$$

$$\gamma_1 = \frac{aT_0}{k_E^+}, \gamma_2 = \frac{g_0}{k_E^+}, \gamma_3 = \frac{aE_{tot}}{k_E^+}$$

System behavior is highly

sensitive to $\phi \equiv \frac{\gamma_2}{\gamma_3} = \frac{g_0}{aE_{tot}}$



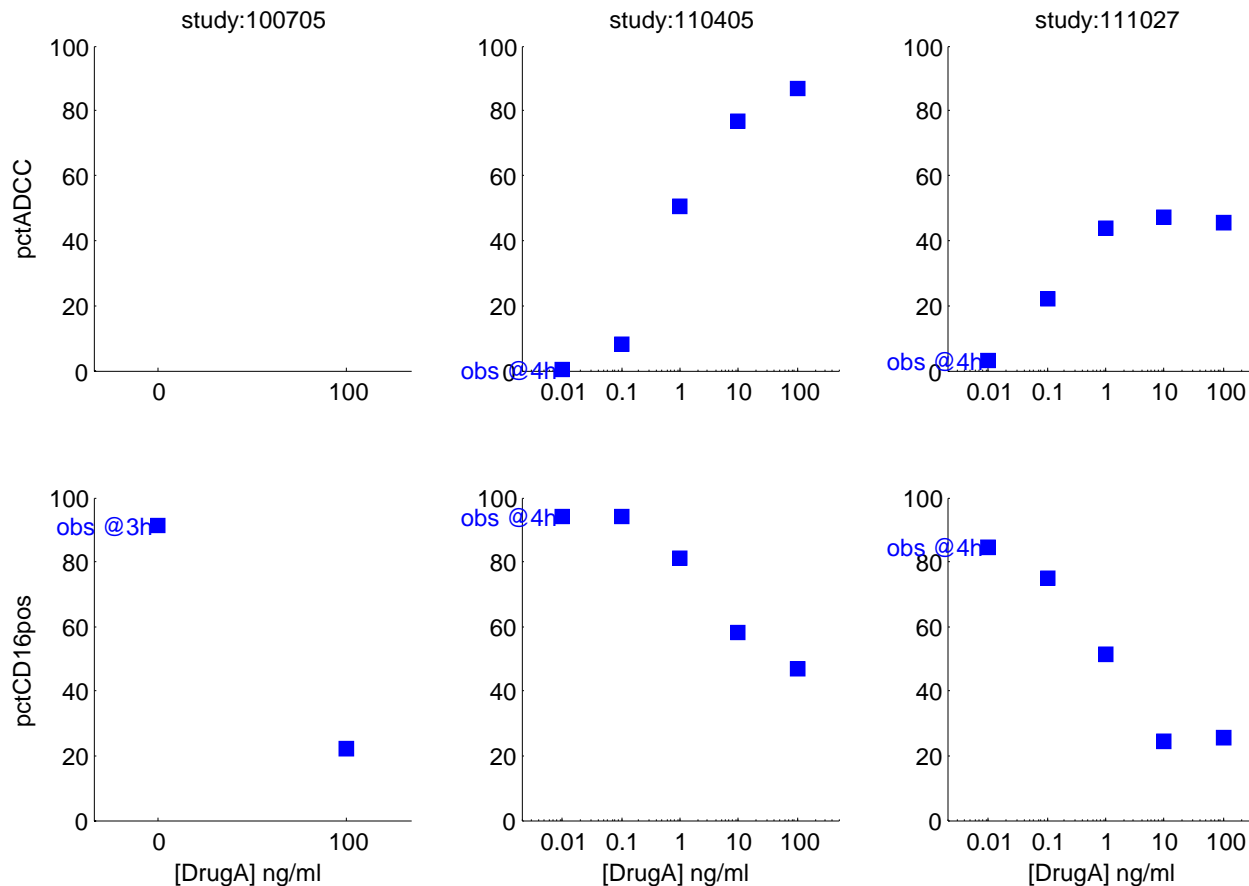
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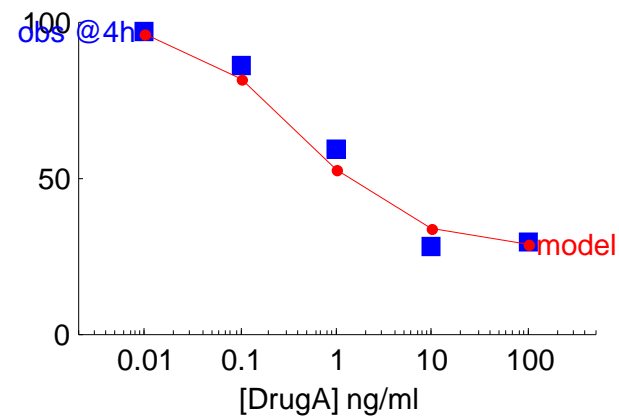
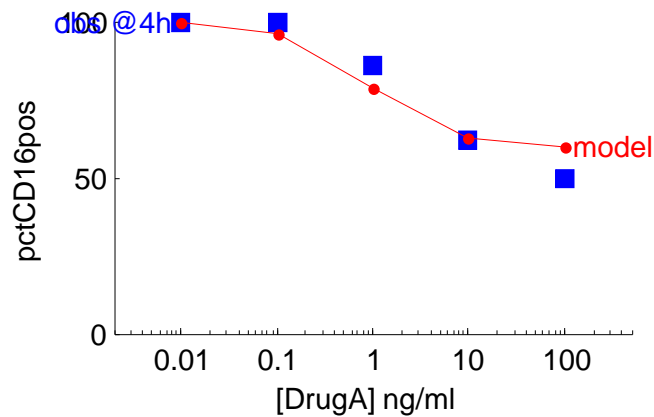
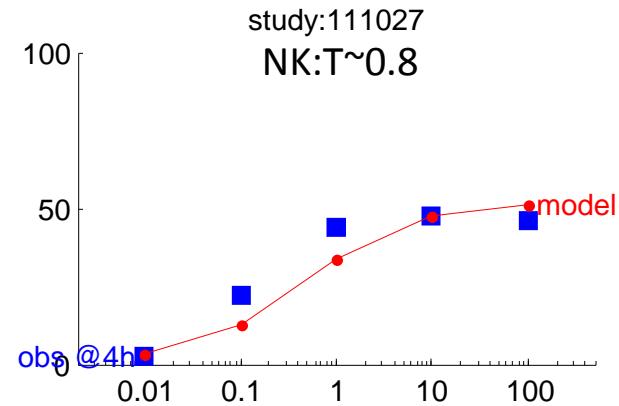
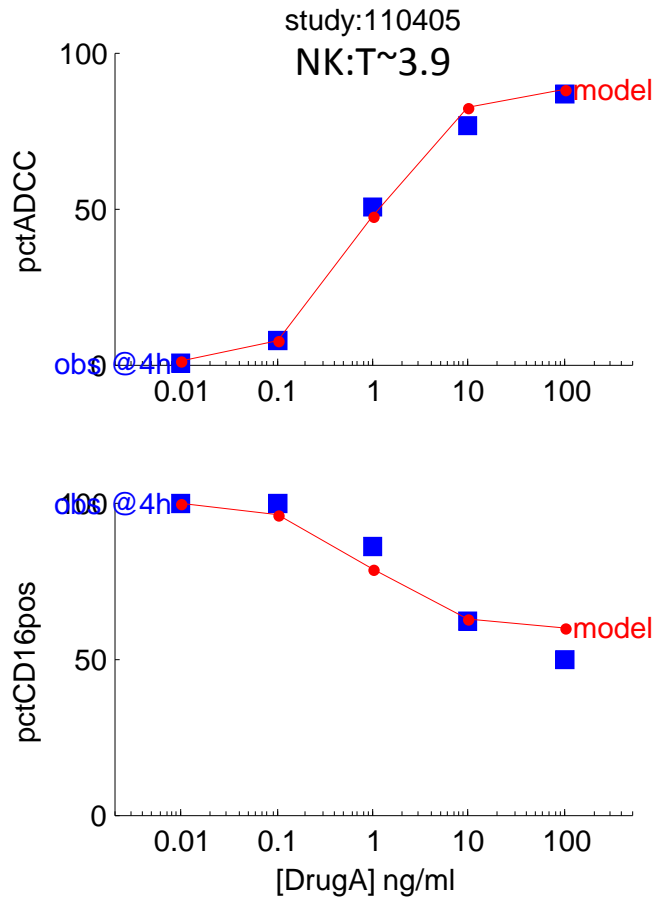
In vitro %ADCC %CD16+ assay probes [DrugA]-dependence of cell killing & CD16 depletion

- PBMCs from healthy volunteers incubated with (XYZ^{mut}) cells in presence of DrugA with NK:T ~ (2.5 & 1) for 4h.
- $\%ADCC \equiv 100 \frac{LDH_{exper} - LDH_{spont}}{LDH_{max} - LDH_{spont}}$
 - “experimental” is with given [DrugA] in presence of effector cells
 - “Spontaneous” is in presence of effector cells but no DrugA (~AICC)
 - “Maximal” is detergent treated
- $\%CD16^+ \equiv \frac{E(4h)}{E_{tot}}$ gives fraction of (NK) cells that are CD16 positive (rel to gate).

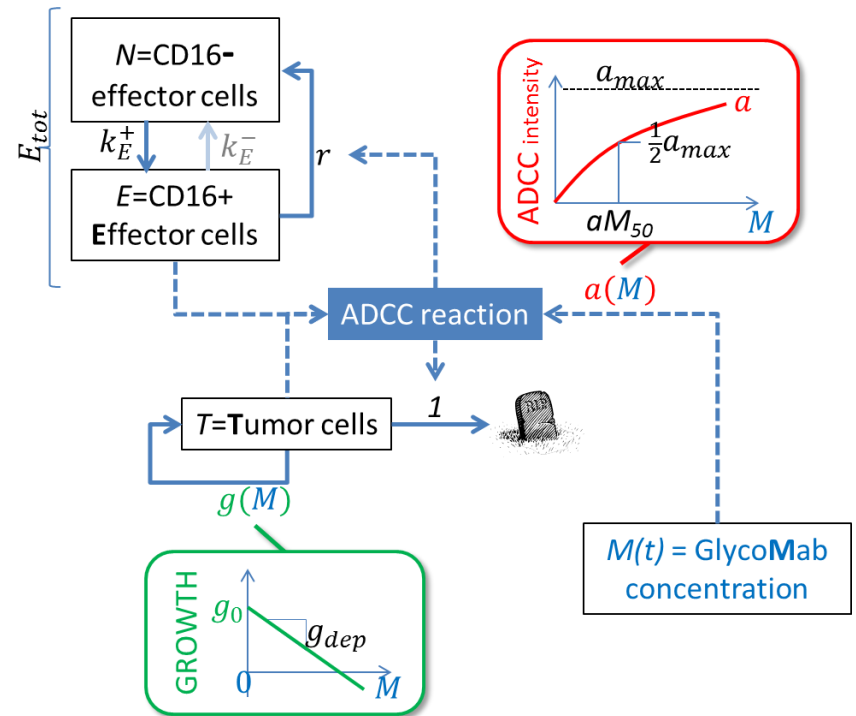
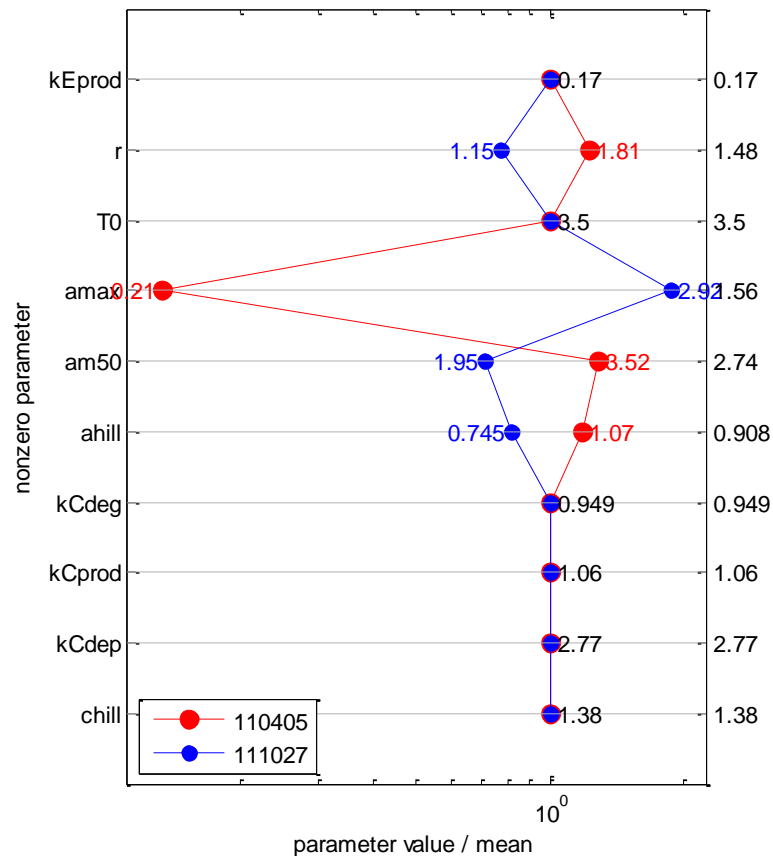
After 3-4h of incubation, %ADCC increases while %CD16+ decreases with increasing [DrugA]



The model parameters can be adjusted to simultaneously reproduce the observed in vitro concentration-response of %ADCC and %CD16+

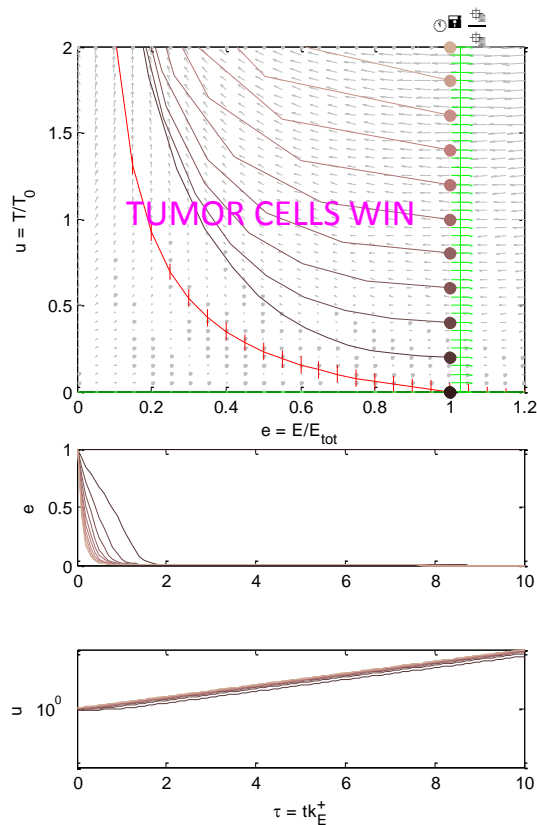


Parameter estimates (least squares followed by shrinking step)



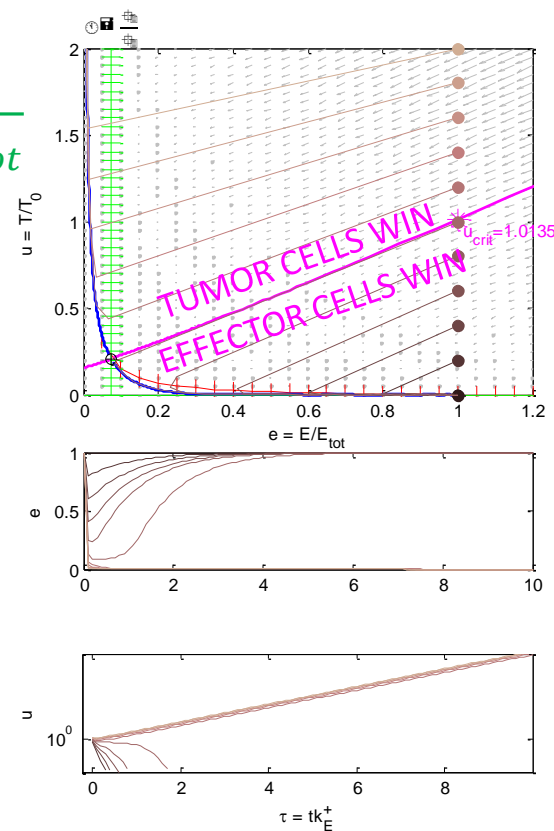
Stability analysis using parameter estimates from in vitro assays (at $a=a_{\max}$, $NK:T \sim 1$)

110405 ($\phi=1.03$)

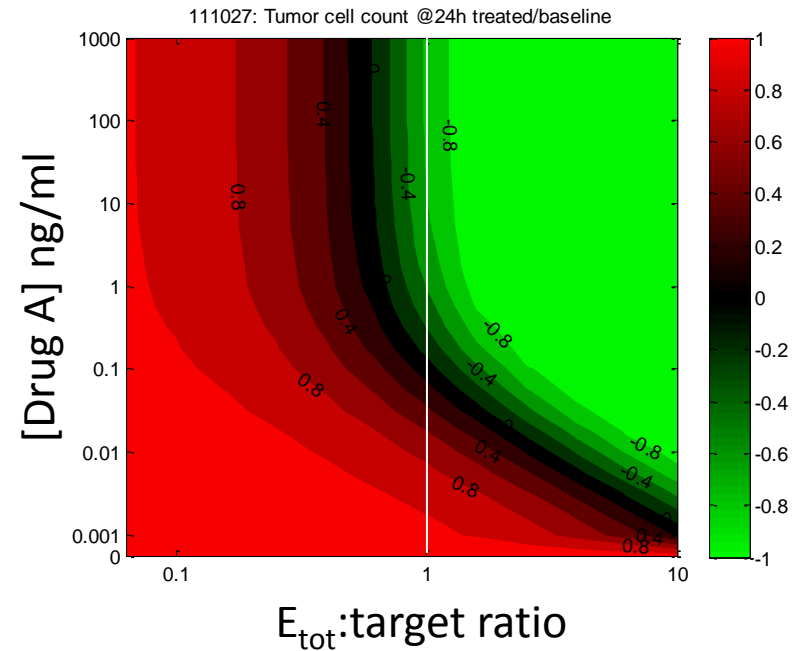
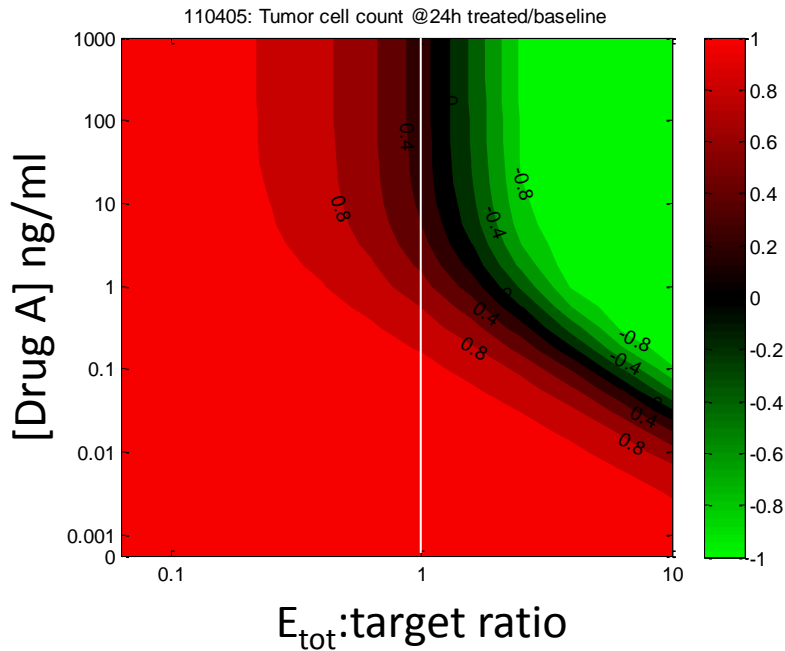


$$\phi \equiv \frac{\gamma_2}{\gamma_3} = \frac{g_0}{aE_{\text{tot}}}$$

111027 ($\phi=0.07$)

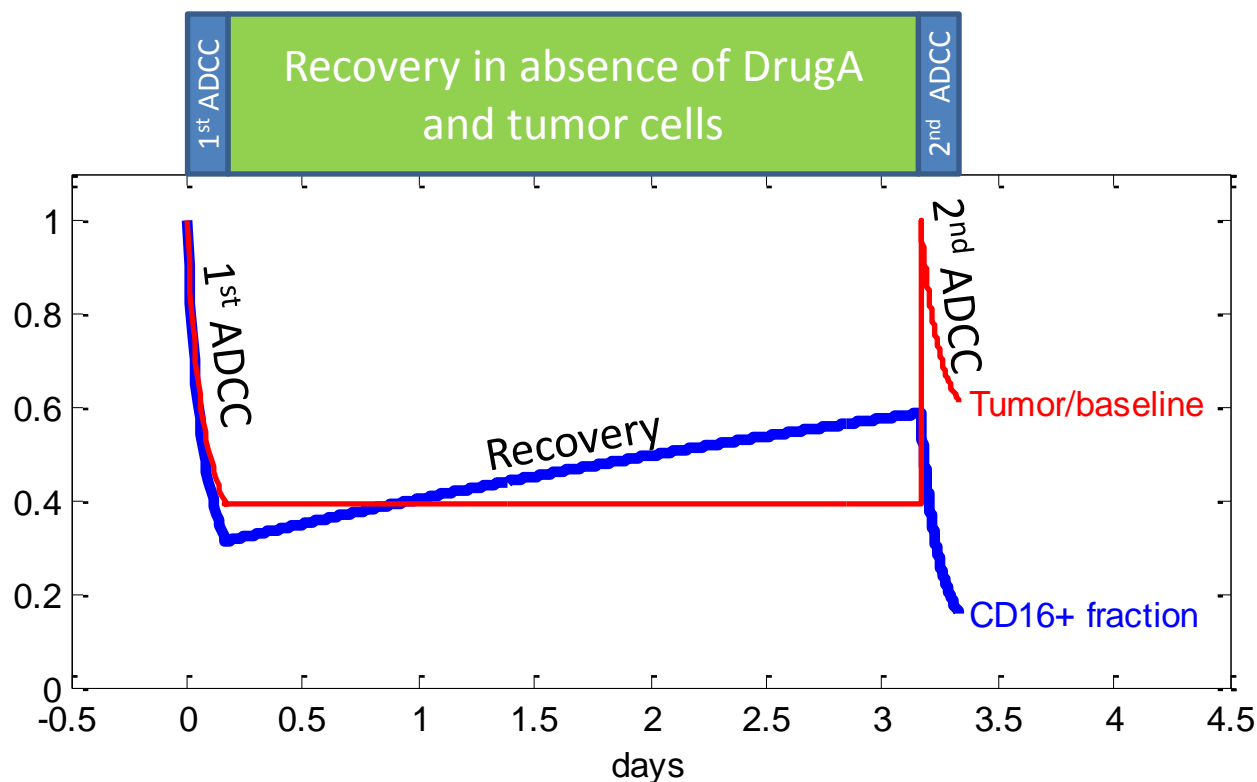


Simulated E:T & exposure dependence (24h incubation)



24h simulated incubation
22h doubling time assumed
No effect on growth, ADCC only

2nd ADCC experiments & simulations



Second ADCC simulations

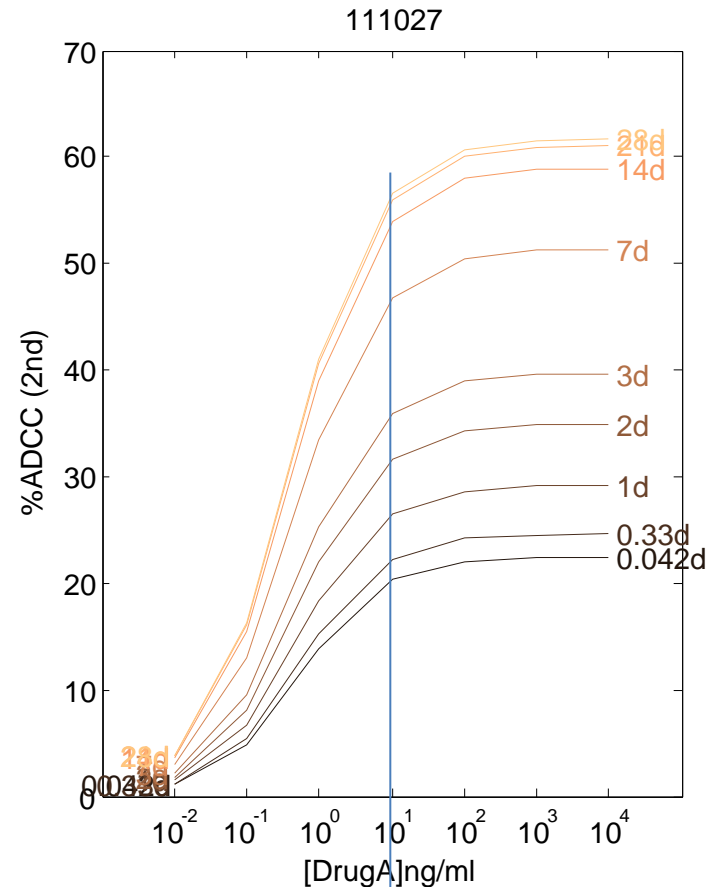
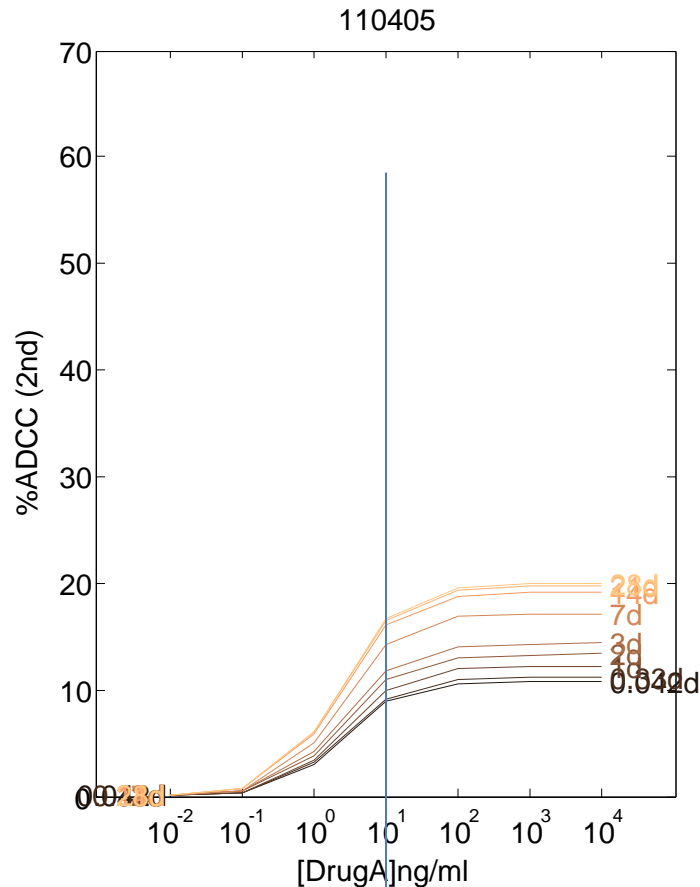
IN VITRO

- PBMCs isolated from subject 110711
- 1st ADCC conditions
 - NK:T ratio ~ 1
 - [DrugA] = 100ng/ml
 - 4 hours incubation
- Washout DrugA & tumor cells & allow PBMC recovery for 3 days
- PBMC's may become 'unhappy' in culture after 3 days
- 2nd ADCC conditions
 - NK:T ratio 1:1
 - [DrugA] = .1,1,10,100 ng/ml
 - 4 hours incubation

IN SILICO

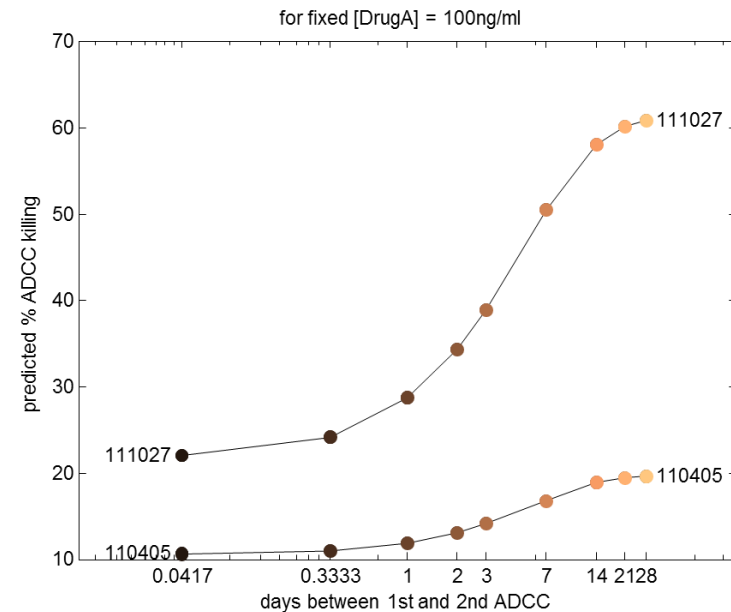
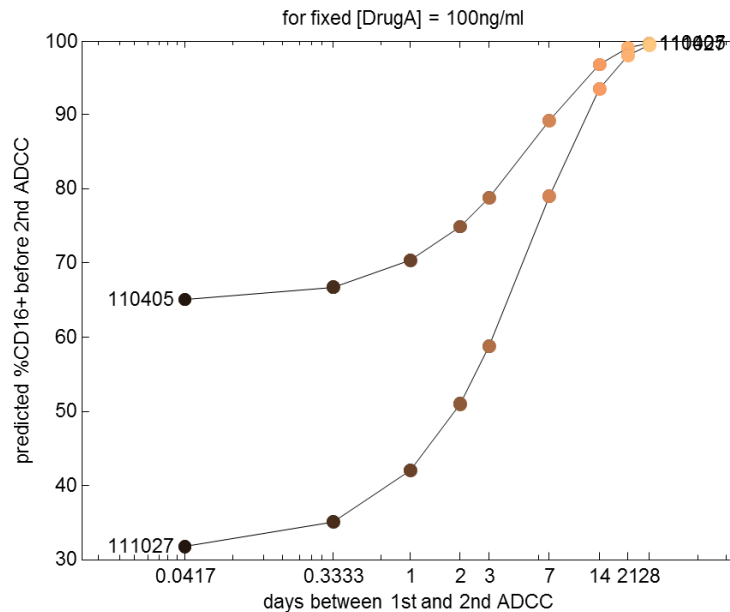
- Parameters as calibrated to subjects 110405 & 111027
- 1st ADCC conditions
 - NK:T ratio ~ 1
 - [DrugA] = 100ng/ml
 - 4 hours simulated time
- Set [DrugA]=0 after 4h and allow CD16 recovery for 1h, 8h, 1, 2, 4, 7, 14, 21, 28days
- Virtual cells are always happy...
- 2nd ADCC conditions
 - Etot held constant, tumor cells set back to original T0 value.
 - [DrugA] = .01,0.1,1,10,100,10³,10⁴
 - 4 hours simulated time

2nd ADCC simulations predict dependence on both concentration and recovery time.



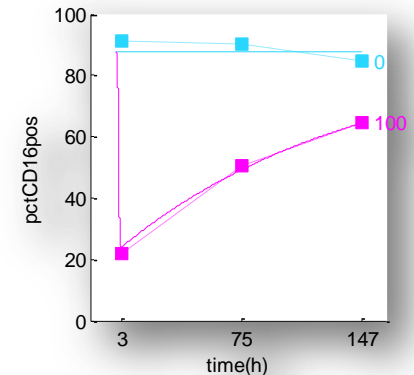
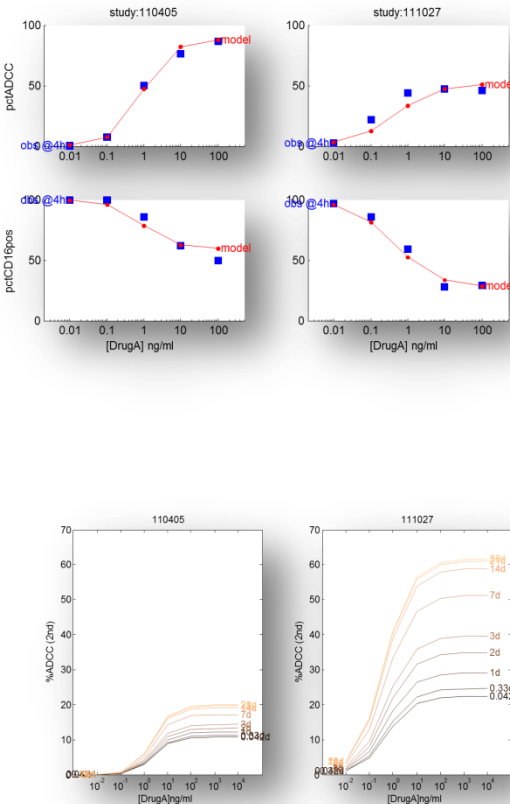
Next slide: look at 100ng/ml “slice” through the above graphs

Model predicts that in vitro, ADCC is sensitive to recovery time up to ~14 days (but inter-individual variability is even more important)



Conclusions of this section

- In vitro model can capture:
 - Mab-dependence of tumor cell killing and CD16+ depletion.
 - CD16+ recovery kinetics after ADCC
 - Qualitative 2nd ADCC dependence on recovery time and DrugA concentration

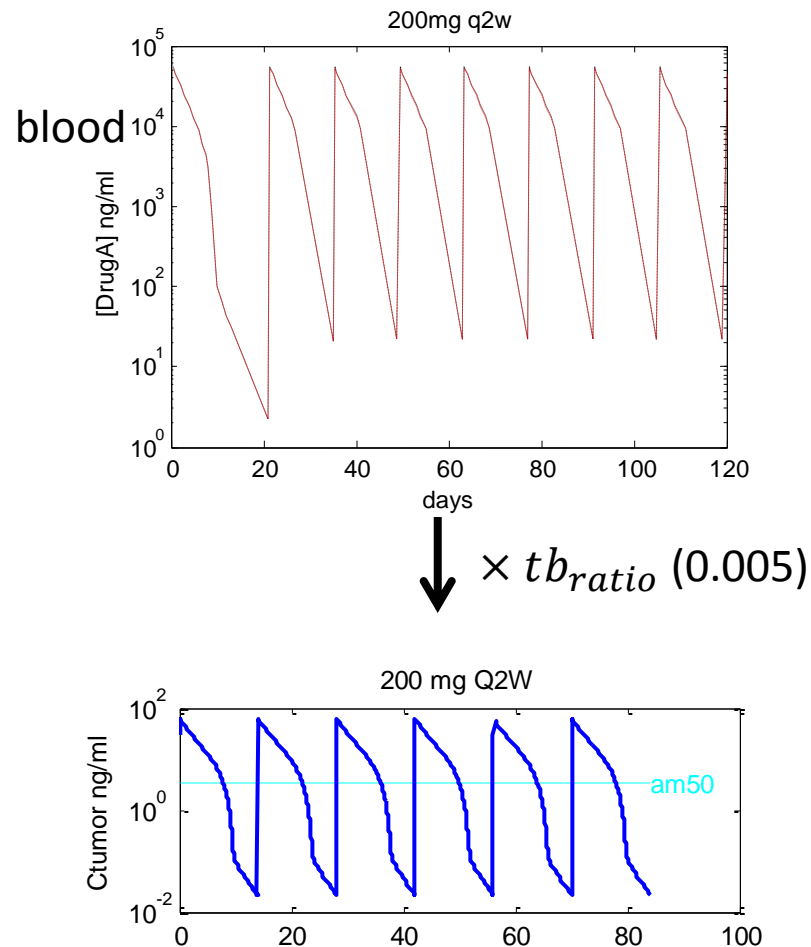


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4. Assess whether U-shaped dose-efficacy is predicted or whether waiting longer between doses is predicted to increase efficacy

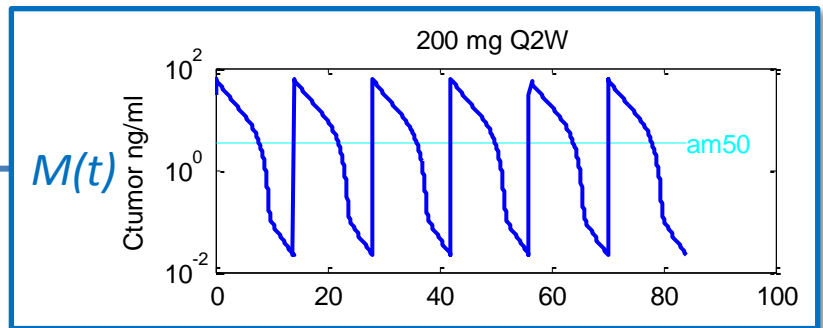
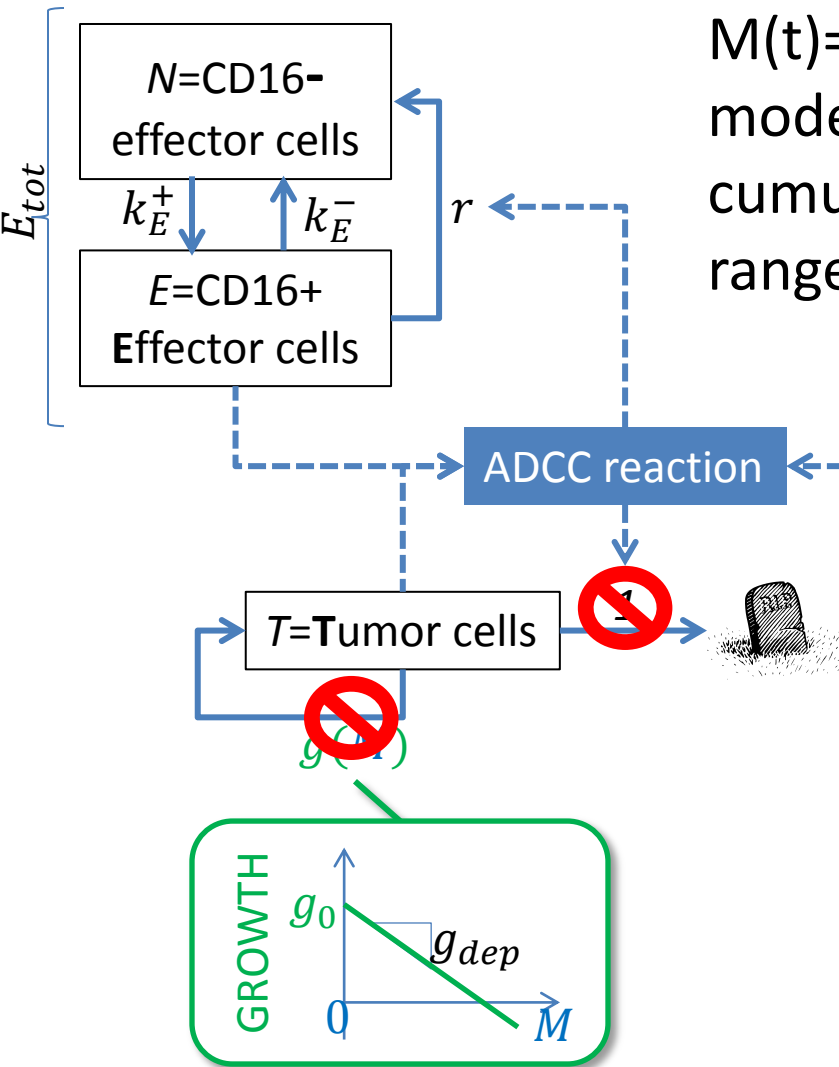
Use popPK model & additional assumptions to predict $M(t)=[DrugA]_{tumor}$ over a range of doses & schedules

- For simplicity, we approximate $M(t) = [DrugA]_{tumor}$ by assuming $M(t) \approx tb_{ratio} [DrugA]_{blood}^*$
- Literature (Wittrup) suggests generic IgG1 tb_{ratio} (at vessel wall) to be ~ 0.006 , so we use a range of 0.001 to 0.01



*[DrugA] time profile at a given location in the tumor interstitium is a complex function of blood concentration, vascular permeability, diffusivity, distance from nearest vessel, Receptor density & internalization, CD16 density, and other factors.

Next, **clamp tumor size** & use $M(t)=[\text{DrugA}]_{\text{tumor}}$ to 'drive' the in vitro model and predict %CD16, ADCC rate, and cumulative ADCC time profiles over a range of doses & schedules



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First some more definitions...

$$\frac{dE}{dt} = (E_{tot} - E)k_E^+ - rR_{ADCC}$$

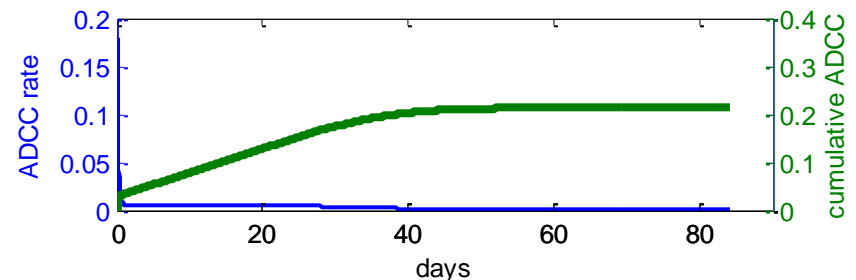
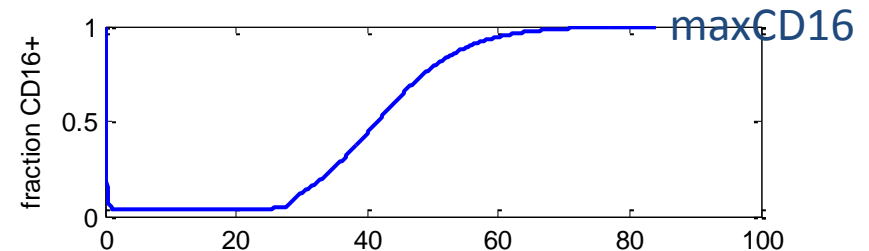
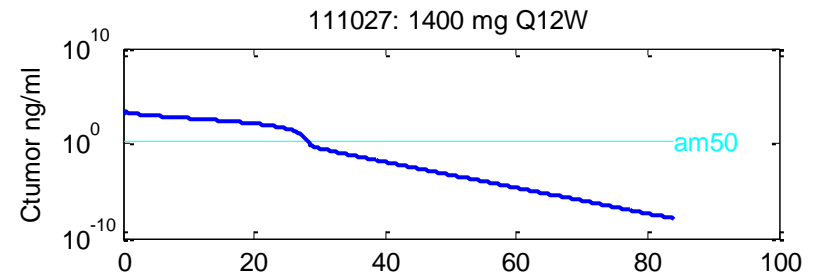
$$\frac{dT}{dt} = g_0T - R_{ADCC}$$

$$R_{ADCC} \equiv E^r T \left(\frac{a_{max} M^{h_m}}{am_{50}^{h_m} + M^{h_m}} \right)$$

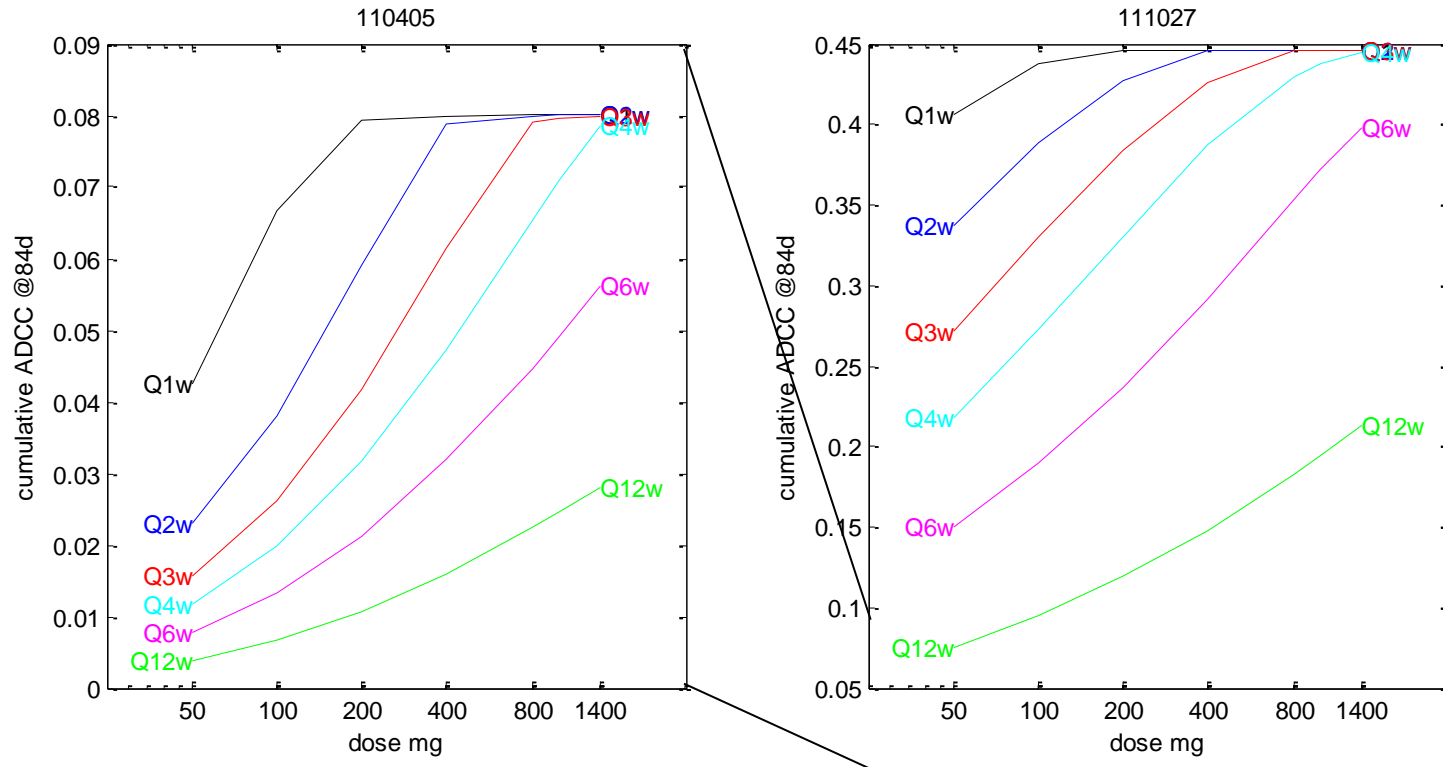
$$"%CD16^{+}"(t) \equiv \frac{E(t)}{E_{tot}}$$

$$ADCC_{cum}(t) \equiv \int_0^t R_{ADCC}(\tau) d\tau$$

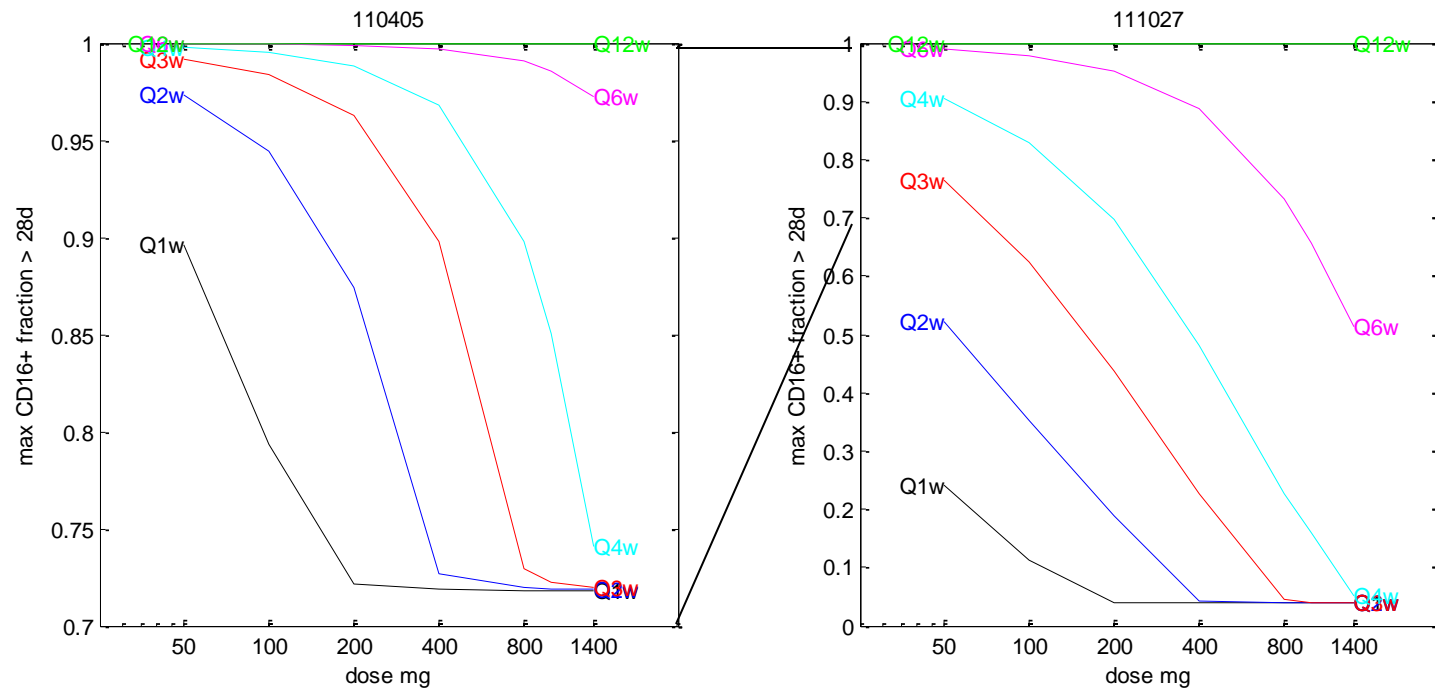
$$maxCD16 \equiv \max_{t>28d} E(t)/E_{tot}$$



Simulations predict cumulative ADCC is neither bell-shaped in dose nor “reverse schedule-dependent”

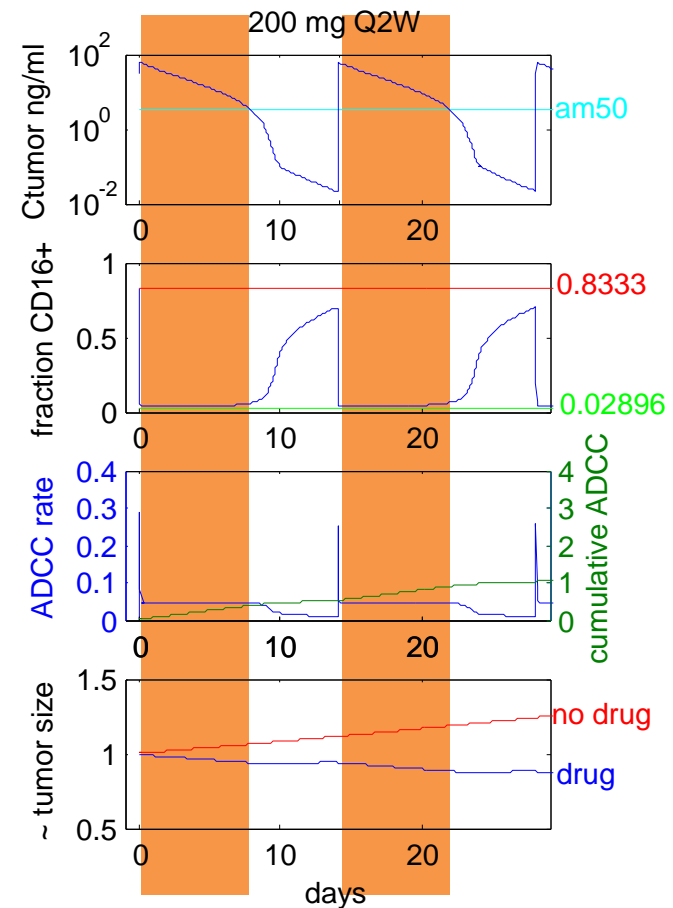
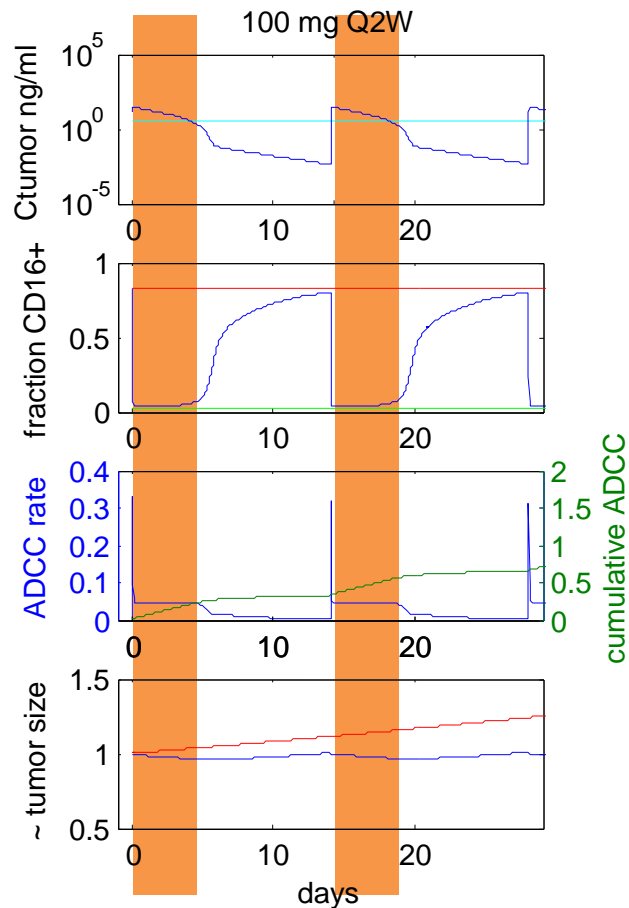


... even though %CD16+ acts the way we think it would...

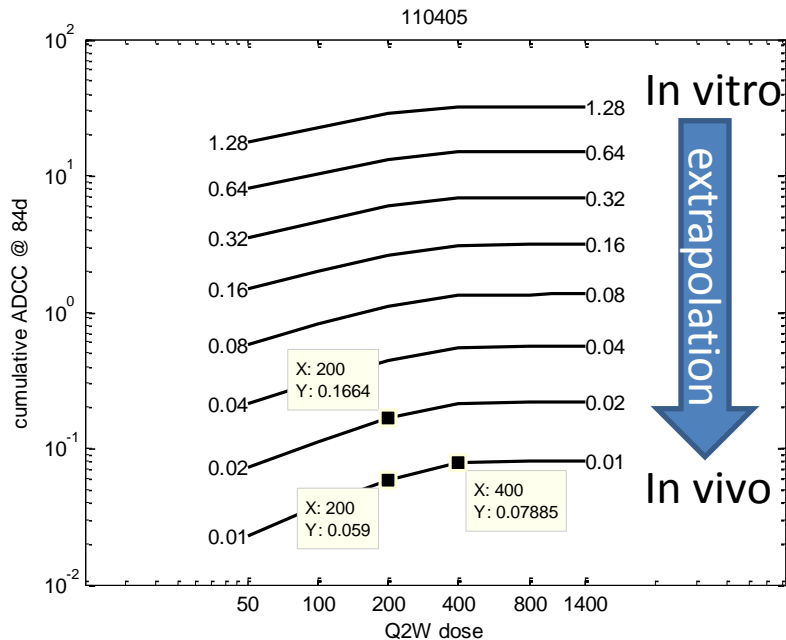


What's going on?

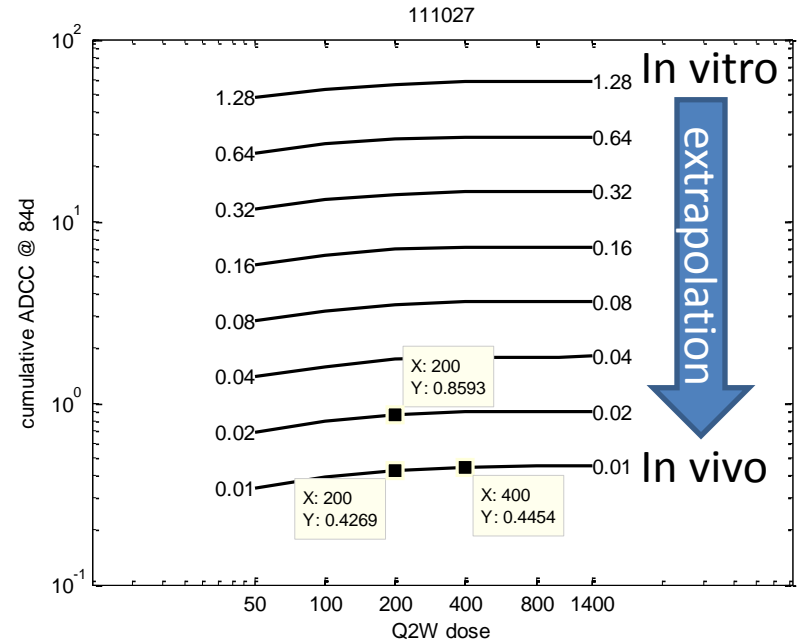
Model predicts that most ADCC occurs **when**
[mAb]>am₅₀ & %CD16+ is low



Additional prediction/insight: cumulative ADCC is much more sensitive to $E_{\text{tot}}:T$ ratio than to dose



Doubling dose 200→400: ADCC 0.06→0.08 (+33%)
Doubling $E:T$ 0.01→0.02: ADCC 0.06→0.17 (+200%)



Doubling dose 200→400: ADCC 0.43→0.45 (+4%)
Doubling $E:T$ 0.01→0.02: ADCC 0.43→0.86 (+100%)

Conclusions

- In spite of interesting ADCC/CD16 dynamics, both the complex and simple multi-scale models predict
 - Strictly monotonic dose-efficacy relationship
 - No inverse schedule dependence at relevant doses
 - Higher sensitivity to Effector:Target ratio than to Drug A dose
- Complex models are useful for
 - Encompassing many potential mechanisms and their interactions
 - Sensitivity analysis pointing to sub-models of interest
- Simpler models are useful for
 - Deconstructing counterintuitive behavior (of bigger model) via phase plane & bifurcation analysis
 - Faster analyses and better defined parameter estimation
 - Explaining quickly to wide audiences

Technical appendix

And archive of paths not taken or to
be taken

Nondimensionalize

- Scale time by CD16 turnover rate:
 $\tau = k_E^- t$
- Scale E by E_{tot} so that e is the CD16+ ratio: $e = \frac{E}{E_{tot}}$.
- Scale T by initial tumor size: $u = \frac{T}{T_0}$.
- Let:
- $\gamma_1 = \frac{k_E^+}{k_E^-}$
- $\gamma_2 = \frac{T_0 r E_{tot}^{r-1} a'}{k_E^-}$
- $\gamma_3 = \frac{g'}{k_E^-}$
- $\gamma_4 = \frac{a' E_{tot}^r}{k_E^-}$

$$\frac{dE}{dt} = E_{tot} k_E^+ - (k_E^+ + k_E^-) E - r a' E^r T$$

$$\frac{dT}{dt} = g' T - a' E^r T$$

$$\begin{aligned} \frac{de}{d\tau} &= \frac{k_E^+}{k_E^-} - \left(\frac{k_E^+}{k_E^-} + 1 \right) e - \frac{T_0 r E_{tot}^{r-1} a'}{k_E^-} e^r u \\ \frac{du}{d\tau} &= \frac{g'}{k_E^-} u - \frac{a' E_{tot}^r}{k_E^-} e^r u \end{aligned}$$

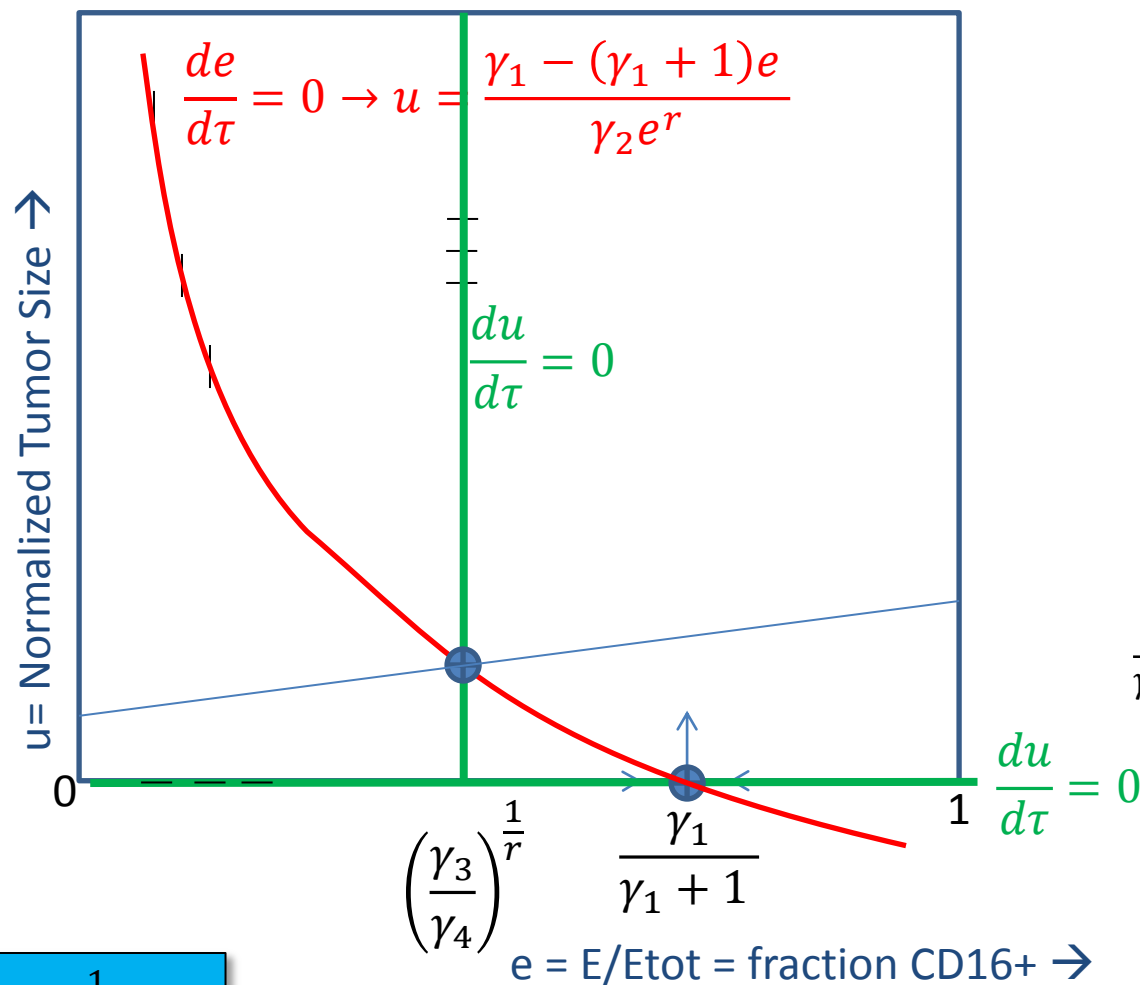
$$\begin{aligned} \frac{de}{d\tau} &= \gamma_1 - (\gamma_1 + 1)e - \gamma_2 e^r u \\ \frac{du}{d\tau} &= \gamma_3 u - \gamma_4 e^r u \end{aligned}$$

Stability analysis

drug: $g=g'>0$, $a'>0$

$$\frac{de}{d\tau} = \gamma_1 - (\gamma_1 + 1)e - \gamma_2 e^r u$$

$$\frac{du}{d\tau} = \gamma_3 u - \gamma_4 e^r u$$



$$\gamma_1 = \frac{k_E^+}{k_E^-}$$

$$\gamma_2 = \frac{T_0 r E_{tot}^{r-1} a'}{k_E^-}$$

$$\gamma_3 = \frac{g'}{k_E^-}$$

$$\gamma_4 = \frac{a' E_{tot}^r}{k_E^-}$$

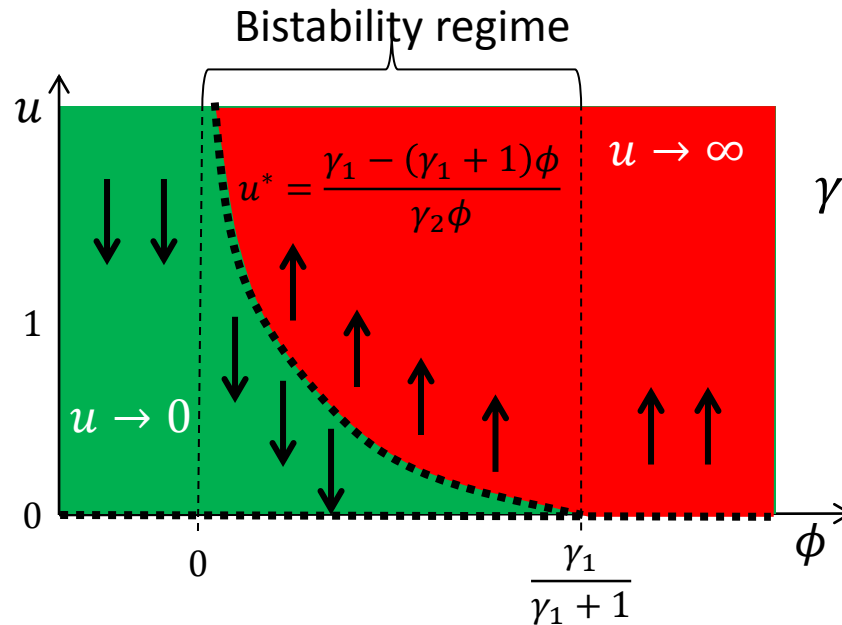
$$\frac{\gamma_1}{\gamma_1 + 1} = \frac{k_E^+}{k_E^+ + k_E^-}$$

$$\phi \equiv \left(\frac{\gamma_3}{\gamma_4}\right)^{\frac{1}{r}} = \left(\frac{g'}{a'}\right)^{\frac{1}{r}} \frac{1}{E_{tot}}$$

Bifurcation stuff

$$\begin{aligned}\frac{de}{d\tau} &= \gamma_1 - (\gamma_1 + 1)e - \gamma_2 e^r u \\ \frac{du}{d\tau} &= \gamma_3 u - \gamma_4 e^r u\end{aligned}$$

- Key parameter $\phi \equiv \frac{\gamma_3}{\gamma_4} = \frac{g'}{a'E_{tot}}$
- Absent drug, $\phi > \frac{\gamma_1}{\gamma_1 + 1}$, otherwise tumor wouldn't grow.
- As we add more drug, ϕ gets smaller because g' gets smaller and a' gets bigger. When $\phi < \frac{\gamma_1}{\gamma_1 + 1}$, we get a saddle at (ϕ, u^*) and two regions. If u is small enough the tumor shrinks to zero, otherwise it grows without bound.
- If Receptor inhibition is strong enough to actually shrink the tumor, ie, $g' < 0$, then we get down to $\phi < 0$, in which case the tumor shrinks no matter what.



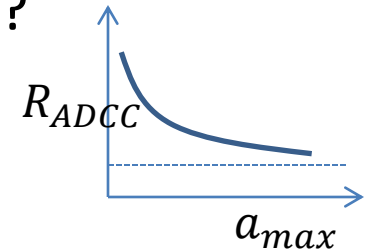
$$\begin{aligned}\gamma_1 &= \frac{k_E^+}{k_E^-} \\ \gamma_2 &= \frac{T_0 r E_{tot}^{r-1} a'}{k_E^-} \\ \gamma_3 &= \frac{g'}{k_E^-} \\ \gamma_4 &= \frac{a' E_{tot}^r}{k_E^-}\end{aligned}$$

$$\phi \equiv \left(\frac{\gamma_3}{\gamma_4} \right)^{\frac{1}{r}} = \left(\frac{g'}{a'} \right)^{\frac{1}{r}} \frac{1}{E_{tot}}$$

$$\frac{\gamma_1}{\gamma_1 + 1} = \frac{k_E^+}{k_E^+ + k_E^-}$$

This model predicts that significant ADCC can occur even when %CD16+ is tiny!

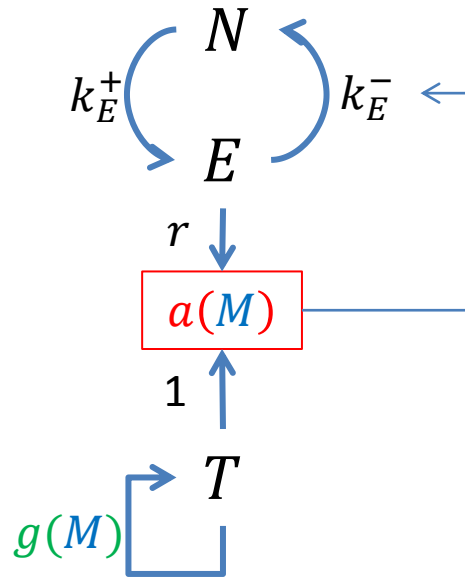
- ‘Thought experiment’: If we assume constant tumor T_0 and $r = 1$, what happens to the ADCC rate R_{ADCC} if we have sustained high concentrations of DrugA and a high a_{max} (max ADCC efficiency)?
 - No ADCC because %CD16+ gets knocked way down?
 - Some ADCC because we have DrugA on board?
 - Lots of ADCC because $a \sim a_{max}$, which is big?
- The answer, according to the model, is:



$\%CD16^+ \rightarrow 0$, but $R_{ADCC} \rightarrow E_{tot}k_E^+ > 0$ as $a_{max} \rightarrow \infty$

- In other words, *even if a_{max} is big enough to make $CD16^+ \sim 0$, the ADCC rate can still be nonzero!*

New model



ASSUMPTIONS

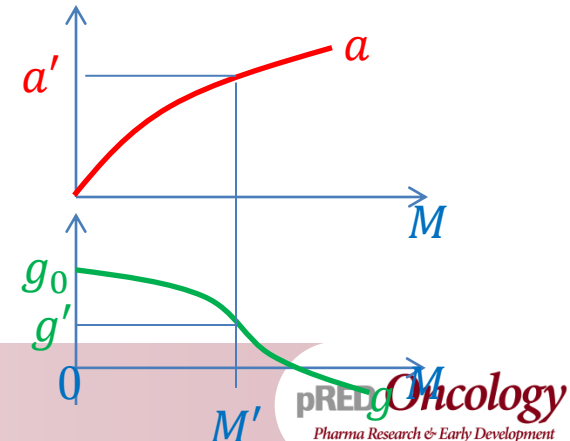
- CD16+ effector cells (E) are produced/recover at a constant rate k_E^+ and 'decay' absent ADCC activity at a rate k_E^- . N is the number of CD16 Negative cells. $N + E = E_{tot}$ assumed constant for now (in vitro).
- Absent ADCC/AICC, tumor cells (T) proliferate exponentially at a net rate g , which can be attenuated by Receptor inhibition as a function of $[mAb] = M$, ie $g(M)$. AICC effects are implicit in g .
- In the presence of E and mAb, ADCC can occur at an $[mAb] = M$ dependent rate $a(M(t))ET$. Each ADCC reaction results in loss of one tumor cell and r CD16+ effector cells.

Effector cells:

$$\frac{dE}{dt} = (E_{tot} - E)k_E^+ - k_E^- E - r a(M(t)) E^r T$$

Tumor cells:

$$\frac{dT}{dt} = g(M(t)) T - a(M(t)) E^r T$$



The model

$$\frac{dE}{dt} = (E_{tot} - E)k_E^+ - k_E^- E - ra(M(t))E^r T$$

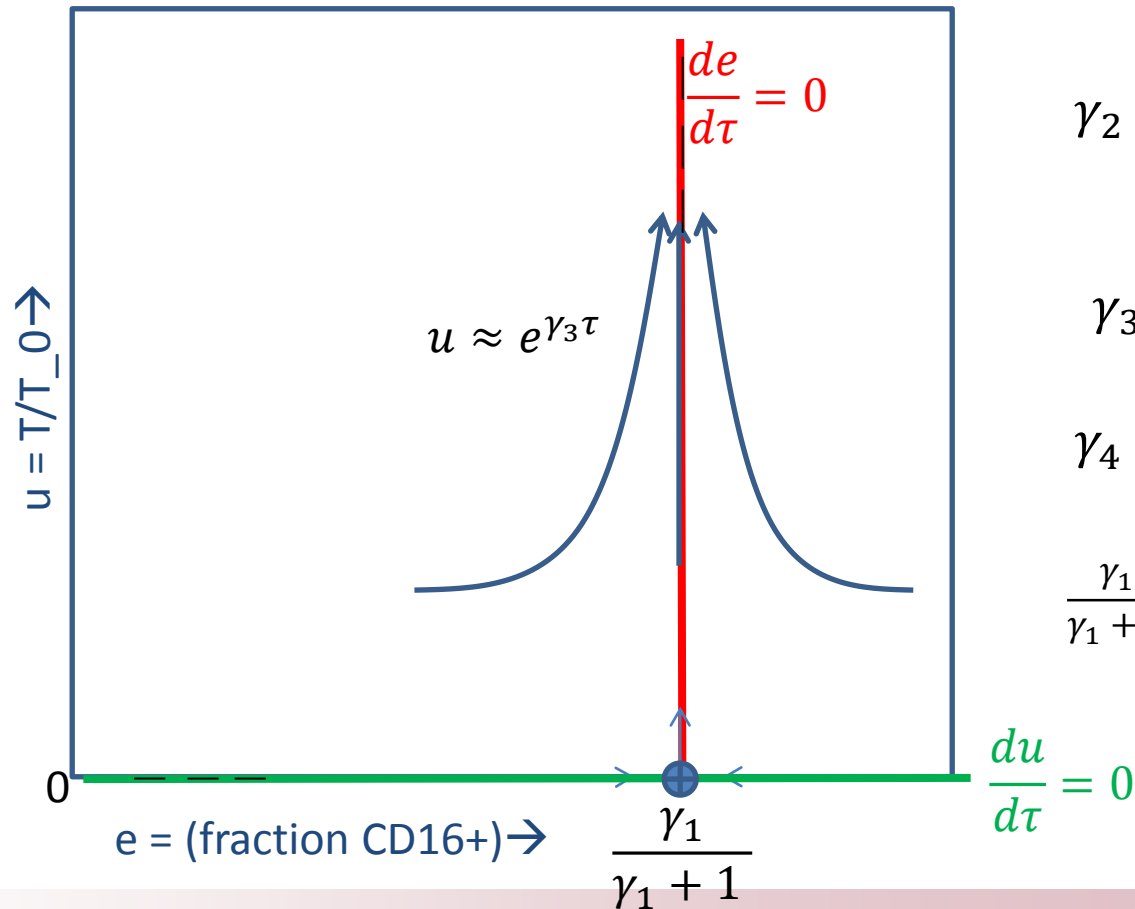
$$\frac{dT}{dt} = g(M(t))T - a(M(t))E^r T$$

	Description	Value
E	#/vol of CD16+ Effector cells (state variable)	>0
T	#/vol of viable Tumor (target) cells (state variable)	>0
E_{tot}	Total number of (CD16+ and CD16-) effector cells	>0
k_E^+	Production/recovery rate of CD16+ Effector cells	>0
k_E^-	Baseline 1 st order degradation rate of CD16+ Effector cells	>0
r	Ratio of how many CD16+ cells depleted per tumor cell killed	>0
$a(M)$	ADCC efficiency as function of mAb concentration	>0
$M(t)$	mAb concentration as function of time	>=0
$g(M)$	Tumor growth rate as function of mAb concentration Baseline growth rate g_0 includes AICC effects	$-\infty < g < +\infty$ $g(0) = g_0 > 0$

Stability analysis

No drug: $g=g_0$, $a'=0$

$$\begin{aligned}\frac{de}{d\tau} &= \gamma_1 - (\gamma_1 + 1)e - \gamma_2 e^r u \\ \frac{du}{d\tau} &= \gamma_3 u - \gamma_4 e^r u\end{aligned}$$



$$\begin{aligned}\gamma_1 &= \frac{k_E^+}{k_E^-} \\ \gamma_2 &= \frac{T_0 r E_{tot}^{r-1} a'}{k_E^-} \\ &= 0\end{aligned}$$

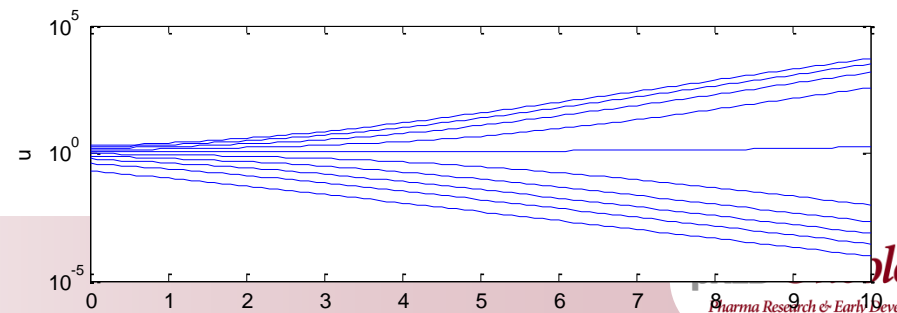
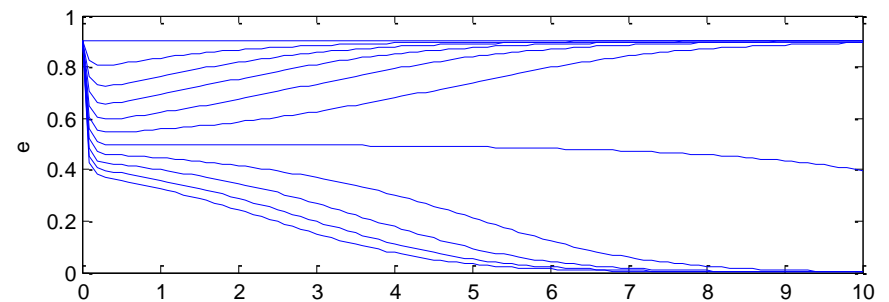
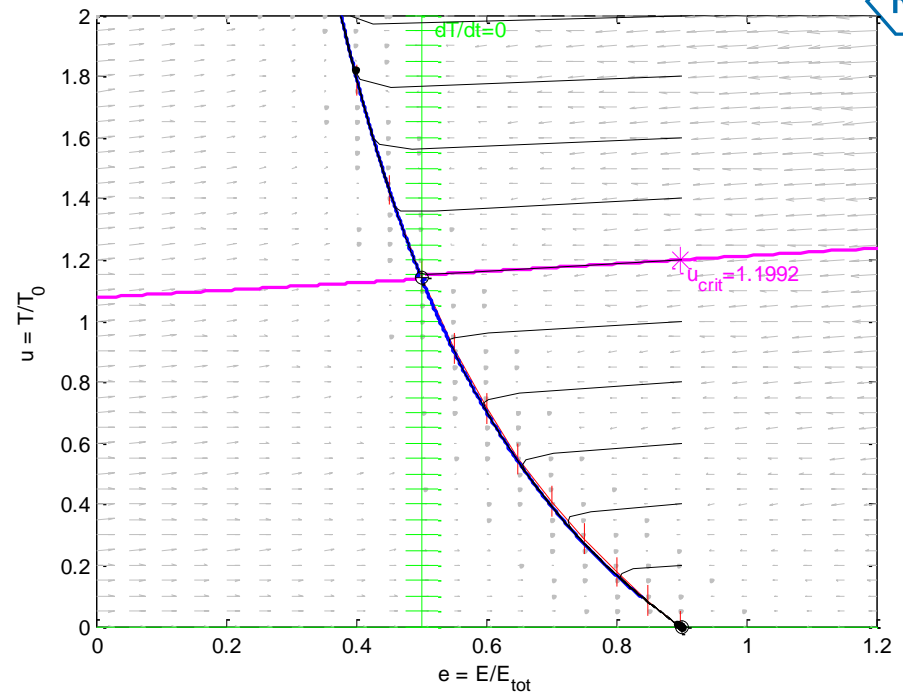
$$\gamma_3 = \frac{g'}{k_E^-} = \frac{g_0}{k_E^-}$$

$$\gamma_4 = \frac{a' E_{tot}^r}{k_E^-} = 0$$

$$\frac{\gamma_1}{\gamma_1 + 1} = \frac{k_E^+}{k_E^+ + k_E^-}$$

Simple_cell_mode

l.m



LDH data

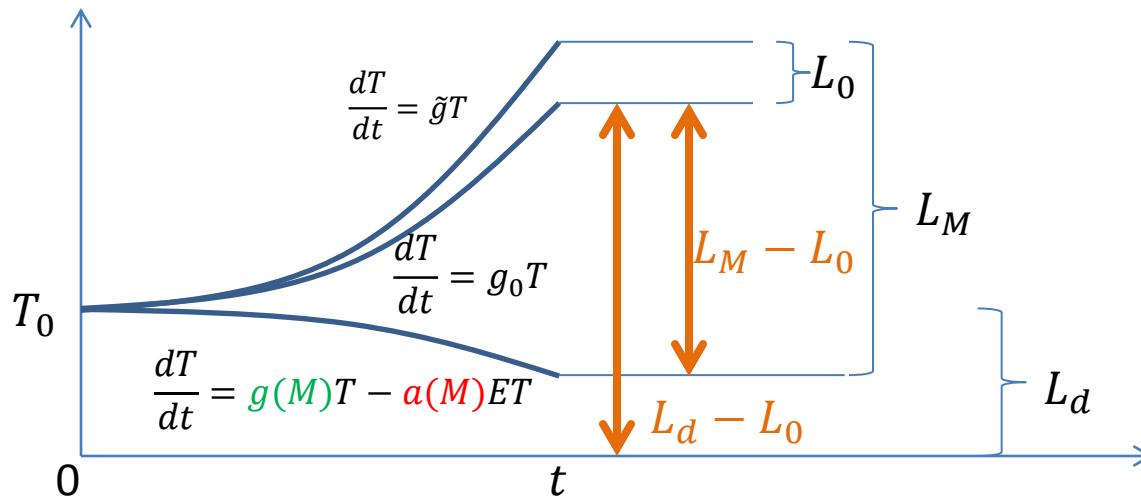
$$\frac{dE}{dt} = E_{tot}k_E^+ - (k_E^+ + k_E^-)E - ra(M)E^rT$$

$$\frac{dT}{dt} = g(M)T - a(M)E^rT$$

- The %ADCC is calculated as: (experimental LDH release - spontaneous LDH release)/(maximal LDH release – spontaneous LDH release)x100. = 100 α (see equation \rightarrow)
 - “experimental” is with given conc of DrugA in presence of effector cells
 - Spontaneous is in presence of effector cells but no DrugA
 - Maximal is detergent treated

$$\alpha(M) \equiv \frac{L_M - L_0}{L_d - L_0}$$

$$g_0 = \tilde{g} - \underbrace{k_i E_{tot}}_{AICC} = \tilde{g} - \tilde{k}_i$$



$$\alpha(t; m) = \frac{T_0 e^{g_0 t} - T(t; M)}{T_0 e^{g_0 t}} = 1 - \frac{T(t; M)}{T_0 e^{g_0 t}} = 1 - u(t; M) e^{-g_0 t}$$