

**Q1. 21 January Shift 1**

If the domain of the function  $f(x) = \cos^{-1}\left(\frac{2x-5}{11-3x}\right) + \sin^{-1}(2x^2 - 3x + 1)$  is the interval  $[\alpha, \beta]$ , then  $\alpha + 2\beta$  is equal to :

- (1) 3      (2) 5      (3) 1      (4) 2

**Q2. 21 January Shift 2**

Let the maximum value of  $(\sin^{-1} x)^2 + (\cos^{-1} x)^2$  for  $x \in \left[-\frac{\sqrt{3}}{2}, \frac{1}{\sqrt{2}}\right]$  be  $\frac{m}{n}\pi^2$ , where  $\text{gcd}(m, n) = 1$ . Then

$m + n$  is equal to \_\_\_\_.

**Q3. 22 January Shift 1**

The number of solutions of  $\tan^{-1} 4x + \tan^{-1} 6x = \frac{\pi}{6}$ , where  $-\frac{1}{2\sqrt{6}} < x < \frac{1}{2\sqrt{6}}$ , is equal to

- (1) 3      (2) 0      (3) 2      (4) 1

**Q4. 24 January Shift 2**

If the domain of the function  $f(x) = \sin^{-1}\left(\frac{1}{x^2-2x-2}\right)$ , is  $(-\infty, \alpha] \cup [\beta, \gamma] \cup [\delta, \infty)$ , then  $\alpha + \beta + \gamma + \delta$  is equal to

- (1) 2      (2) 3      (3) 4      (4) 5

**Q5. 28 January Shift 1**

If  $k = \tan\left(\frac{\pi}{4} + \frac{1}{2}\cos^{-1}\left(\frac{2}{3}\right)\right) + \tan\left(\frac{1}{2}\sin^{-1}\left(\frac{2}{3}\right)\right)$ , then the number of solutions of the equation  $\sin^{-1}(kx - 1) = \sin^{-1} x - \cos^{-1} x$  is \_\_\_\_.

**Q6. 28 January Shift 2**

Considering the principal values of inverse trigonometric functions, the value of the expression

$\tan\left(2\sin^{-1}\left(\frac{2}{\sqrt{13}}\right) - 2\cos^{-1}\left(\frac{3}{\sqrt{10}}\right)\right)$  is equal to :

- (1)  $\frac{16}{63}$       (2)  $-\frac{33}{56}$       (3)  $-\frac{16}{63}$       (4)  $\frac{33}{56}$

**ANSWER KEYS**

1. (1)      2. 65      3. (4)      4. (3)      5. 1      6. (4)