

**Q1. 21 January Shift 1**

If  $x^2 + x + 1 = 0$ , then the value of  $(x + \frac{1}{x})^4 + (x^2 + \frac{1}{x^2})^4 + (x^3 + \frac{1}{x^3})^4 + \dots + (x^{25} + \frac{1}{x^{25}})^4$  is:

(1) 162      (2) 175      (3) 145      (4) 128

**Q2. 21 January Shift 2**

Let  $z$  be the complex number satisfying  $|z - 5| \leq 3$  and having maximum positive principal argument. Then  $34\left|\frac{5z-12}{5iz+16}\right|^2$  is equal to :

- (1) 26      (2) 12      (3) 20      (4) 16

**Q3. 22 January Shift 1**

Let  $\alpha = \frac{-1+i\sqrt{3}}{2}$  and  $\beta = \frac{-1-i\sqrt{3}}{2}$ ,  $i = \sqrt{-1}$ . If

$(7 - 7\alpha + 9\beta)^{20} + (9 + 7\alpha - 7\beta)^{20} + (-7 + 9\alpha + 7\beta)^{20} + (14 + 7\alpha + 7\beta)^{20} = m^{10}$ , then  $m$  is \_\_\_\_\_

**Q4. 22 January Shift 2**

Let  $S = \{z \in \mathbb{C} : 4z^2 + \bar{z} = 0\}$ . Then  $\sum_{z \in S} |z|^2$  is equal to:

- (1)  $\frac{5}{64}$       (2)  $\frac{1}{16}$       (3)  $\frac{3}{16}$       (4)  $\frac{7}{64}$

**Q5. 23 January Shift 1**

Let  $S = \{z : 3 \leqslant |2z - 3(1+i)| \leqslant 7\}$  be a set of complex numbers. Then  $\min_{z \in S} |(z + \frac{1}{2}(5+3i))|$  is equal to :

- (1) 2      (2)  $\frac{5}{2}$       (3)  $\frac{3}{2}$       (4)  $\frac{1}{2}$

**Q6. 23 January Shift 2**

If  $z = \frac{\sqrt{3}}{2} + \frac{i}{2}$ ,  $i = \sqrt{-1}$ , then  $(z^{201} - i)^8$  is equal to

- (1) 1      (2) 256      (3) -1      (4) 0

**Q7. 24 January Shift 2**

Let  $z = (1+i)(1+2i)(1+3i)\dots(1+ni)$ , where  $i = \sqrt{-1}$ . If  $|z|^2 = 44200$ , then  $n$  is equal to \_\_\_\_\_

**Q8. 28 January Shift 1**

Let  $z$  be a complex number such that  $|z - 6| = 5$  and  $|z + 2 - 6i| = 5$ . Then the value of  $z^3 + 3z^2 - 15z + 141$  is equal to

- (1) 50      (2) 61      (3) 37      (4) 42

**Q9. 28 January Shift 2**

Let  $A = \{z \in \mathbb{C} : |z - 2| \leq 4\}$  and  $B = \{z \in \mathbb{C} : |z - 2| + |z + 2| = 5\}$ . Then the max  $\{|z_1 - z_2| : z_1 \in A \text{ and } z_2 \in B\}$  is :

(1)  $\frac{17}{2}$       (2) 8      (3) 9      (4)  $\frac{15}{2}$

**ANSWER KEYS**

1. (3)    2. (3)    3. 49    4. (3)    5. (1)    6. (2)    7. 5    8. (1)

9. (1)

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