

Q1. 21 January Shift 1

If $x^2 + x + 1 = 0$, then the value of $(x + \frac{1}{x})^4 + (x^2 + \frac{1}{x^2})^4 + (x^3 + \frac{1}{x^3})^4 + \dots + (x^{25} + \frac{1}{x^{25}})^4$ is:

- (1) 162 (2) 175 (3) 145 (4) 128

Q2. 21 January Shift 2

Let z be the complex number satisfying $|z - 5| \leq 3$ and having maximum positive principal argument. Then

$34 \left| \frac{5z-12}{5z+16} \right|^2$ is equal to :

- (1) 26 (2) 12 (3) 20 (4) 16

Q3. 22 January Shift 1

Let $\alpha = \frac{-1+i\sqrt{3}}{2}$ and $\beta = \frac{-1-i\sqrt{3}}{2}$, $i = \sqrt{-1}$. If

$(7 - 7\alpha + 9\beta)^{20} + (9 + 7\alpha - 7\beta)^{20} + (-7 + 9\alpha + 7\beta)^{20} + (14 + 7\alpha + 7\beta)^{20} = m^{10}$, then m is _____

Q4. 22 January Shift 2

Let $S = \{z \in \mathbb{C} : 4z^2 + \bar{z} = 0\}$. Then $\sum_{z \in S} |z|^2$ is equal to:

- (1) $\frac{5}{64}$ (2) $\frac{1}{16}$ (3) $\frac{3}{16}$ (4) $\frac{7}{64}$

Q5. 23 January Shift 1

Let $S = \{z : 3 \leq |2z - 3(1+i)| \leq 7\}$ be a set of complex numbers. Then $\min_{z \in S} \left| \left(z + \frac{1}{2}(5+3i) \right) \right|$ is equal to :

- (1) 2 (2) $\frac{5}{2}$ (3) $\frac{3}{2}$ (4) $\frac{1}{2}$

Q6. 23 January Shift 2

If $z = \frac{\sqrt{3}}{2} + \frac{i}{2}$, $i = \sqrt{-1}$, then $(z^{201} - i)^8$ is equal to

- (1) 1 (2) 256 (3) -1 (4) 0

Q7. 24 January Shift 2

Let $z = (1+i)(1+2i)(1+3i) \dots (1+ni)$, where $i = \sqrt{-1}$. If $|z|^2 = 44200$, then n is equal to _____

Q8. 28 January Shift 1

Let z be a complex number such that $|z - 6| = 5$ and $|z + 2 - 6i| = 5$. Then the value of $z^3 + 3z^2 - 15z + 141$ is equal to

- (1) 50 (2) 61 (3) 37 (4) 42

Q9. 28 January Shift 2

Let $A = \{z \in \mathbb{C} : |z - 2| \leq 4\}$ and $B = \{z \in \mathbb{C} : |z - 2| + |z + 2| = 5\}$. Then the max $\{|z_1 - z_2| : z_1 \in A \text{ and } z_2 \in B\}$ is

(1) $\frac{17}{2}$

(2) 8

(3) 9

(4) $\frac{15}{2}$

ANSWER KEYS

1. (3)

2. (3)

3. 49

4. (3)

5. (1)

6. (2)

7. 5

8. (1)

9. (1)