

S a i s i s 1 1: Homework 2

Exercise 1

a. If A and B are independent,

$$\mathbf{P}(A|B) = \mathbf{P}(A) \text{ and } \mathbf{P}(A \cap B) = \mathbf{P}(A)\mathbf{P}(B) \text{ and } \mathbf{P}(A|B) = \mathbf{P}(A).$$

If A and B are independent, then A and B are independent. So,

$$\mathbf{P}(A|B) = \mathbf{P}(A) \text{ and } \mathbf{P}(A \cap B) = \mathbf{P}(A)\mathbf{P}(B) \text{ and } \mathbf{P}(A|B) = \mathbf{P}(A).$$

Since $\mathbf{P}(A|B) = \mathbf{P}(A)$ and $\mathbf{P}(A \cap B) = \mathbf{P}(A)\mathbf{P}(B)$, then $\mathbf{P}(A|B) = \mathbf{P}(A)$ and $\mathbf{P}(A \cap B) = \mathbf{P}(A)\mathbf{P}(B)$.

Exercise

a. As usual, a good start is to write out the probability information stated in the problem.

$$\mathbf{P}(\text{failure}) = 0.60 \qquad \mathbf{P}(\text{moderate}) = 0.40 \qquad \mathbf{P}(\text{major}) = 0.10$$

$$\mathbf{P}(\text{poor}|\text{failure}) = 0.50 \qquad \mathbf{P}(\text{fair}|\text{failure}) = 0.40 \qquad \mathbf{P}(\text{good}|\text{failure}) = 0.10 \qquad \mathbf{P}(\text{poor}|\text{moderate}) = 0.20 \qquad \mathbf{P}(\text{fair}|\text{moderate}) = 0.40 \qquad \mathbf{P}(\text{good}|\text{moderate}) = 0.40$$

For the first branc

Since $0. > 0.21$ and 0.255 it is best for to shoot in the air. nd res ectively, \mathbf{P} wins = $0. ; \mathbf{P}$ B wins = 0.175 ; \mathbf{P} C wins = $0. 5$; \mathbf{P} B wins = 0

- b.** We lose only if we get five heads in a row, otherwise we win 1 dollar. The probability distribution of X_2