

Physics IIIA Lab 3

Pre-Lab Questions:

$$1) I_D(V_D) = I_s \left[\exp\left(\frac{eV_D}{nKT}\right) - 1 \right] = I_s \exp\left(\frac{eV_D}{nKT}\right) \left[1 - \exp\left(-\frac{eV_D}{nKT}\right) \right]$$

$$V_D > 0.1 \text{ V}, \quad \frac{kT}{e} \approx 25.7 \text{ mV}, \quad n \approx 2$$

$$I_D(V_D) = I_s \exp\left(\frac{V_D}{2(25.7 \text{ mV})}\right) \left[1 - \exp\left(-\frac{V_D}{2(25.7 \text{ mV})}\right) \right]$$

$$= I_s \exp\left(\frac{V_D}{51.4 \text{ mV}}\right) \left[1 - \exp\left(-\frac{V_D}{51.4 \text{ mV}}\right) \right], \quad \exp\left(-\frac{V_D}{51.4 \text{ mV}}\right) < \exp\left(-\frac{0.1 \text{ V}}{51.4 \text{ mV}}\right) = 0.143$$

$$\text{so for } V_D > 0.1 \text{ V}, \quad \exp\left(-\frac{V_D}{51.4 \text{ mV}}\right) \approx 0$$

$$\text{so then, } I_D(V_D) = I_s \exp\left(\frac{eV_D}{nKT}\right)$$

2) Zener diodes are special diodes that have a low and precise reverse breakdown voltage. Zener diodes are typically used in reverse bias and can act as voltage regulators.

$$3) n=2, \text{ room temp., } \Delta T \approx 9^\circ\text{C}, \quad T_2 - T_1 = \Delta T, \quad T_1 = 20^\circ\text{C}, \quad E_g = 1.14 \text{ eV}, \quad k = 1.38 \times 10^{-23} \text{ J/K}$$

$$I_s \propto T^3 \exp\left(-\frac{E_g}{nKT}\right)$$

$$\frac{I_{s2}}{I_{s1}} = \frac{T_2^3 \exp\left(-\frac{E_g}{nKT_2}\right)}{T_1^3 \exp\left(-\frac{E_g}{nKT_1}\right)} = \frac{T_2^3}{T_1^3} \exp\left(-\frac{E_g}{nKT_2} + \frac{E_g}{nKT_1}\right) = \frac{T_2^3}{T_1^3} \exp\left(\frac{E_g}{nKT_1 T_2} (T_2 - T_1)\right) = \left(\frac{T_2}{T_1}\right)^3 \exp\left(\frac{E_g}{nKT_1 T_2} \Delta T\right)$$

$$= \left(\frac{\Delta T}{T_1} + 1\right)^3 \exp\left(\frac{E_g}{nKT_1 T_2} \Delta T\right) = \left(\frac{9K}{293.15K} + 1\right)^3 \exp\left(\frac{1.14 \text{ eV} \times 1.6 \times 10^{-19} \text{ J}}{2(1.38 \times 10^{-23} \text{ J})(293K)(302K)} (9K)\right)$$

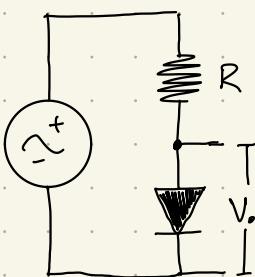
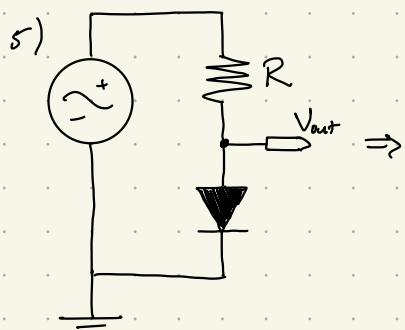
$$= 2.07919 \approx 2$$

$$4) n=2, \Delta V \approx 35 \text{ mV}, \quad e = 1.6 \times 10^{-19} \text{ C}, \quad k = 1.38 \times 10^{-23} \text{ J/K}, \quad T = 293.15 \text{ K}$$

$$I_D(V_D) = I_s \exp\left(\frac{eV_D}{nKT}\right)$$

$$\frac{I_{D2}}{I_{D1}} = \frac{I_s \exp\left(\frac{eV_{D2}}{nKT}\right)}{I_s \exp\left(\frac{eV_{D1}}{nKT}\right)} = \exp\left(\frac{eV_{D2}}{nKT} - \frac{eV_{D1}}{nKT}\right) = \exp\left(\frac{e}{nKT} \Delta V\right) = \exp\left(\frac{1.6 \times 10^{-19} \text{ C}}{2(1.38 \times 10^{-23} \text{ J})(293.15 \text{ K})} (35 \text{ mV})\right)$$

$$= 1.99797 \approx 2$$



$$V_{out} = \frac{nKT}{e} = nV_T \quad \text{where } V_T = \frac{kT}{e}$$

$$V_{in} = V_{tot} = V_R + V_D = IR + \frac{nKT}{e} = IR + nV_T$$

$$G = \frac{V_{out}}{V_{in}} = \frac{nV_T}{IR + nV_T}$$

$$6) \frac{eV_0 - E_A}{T} \approx \text{constant}$$

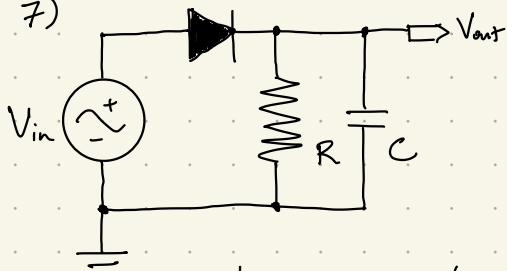
$$\frac{eV_1 - E_A}{T_1} = \frac{eV_2 - E_A}{T_2}$$

$$\frac{eV_1}{T_1} - \frac{eV_2}{T_2} = \frac{E_A}{T_1} - \frac{E_A}{T_2}$$

$$\frac{e(V_1 T_2 - V_2 T_1)}{T_1 T_2} = \frac{E_A(T_2 - T_1)}{T_1 T_2}$$

$$E_A = \frac{e(V_1 T_2 - V_2 T_1)}{T_2 - T_1}$$

7)



$$V = V_0 e^{-t/\tau}$$

$$\Delta V = V_0 \left(1 - e^{-\frac{1}{f\tau}}\right)$$

$$\frac{\Delta V}{V_0} = \frac{V_0 \left(1 - e^{-\frac{1}{f\tau}}\right)}{V_0} = 1 - e^{-\frac{1}{f\tau}}$$

$$1 - e^{-\frac{1}{f\tau}} = \frac{1}{f\tau} - \frac{1}{2(f\tau)^2} + \frac{1}{6(f\tau)^3} + \dots$$

$$\text{since } f \gg \frac{1}{RC} = \frac{1}{\tau} \Rightarrow f\tau \gg 1$$

$$\text{so then } 1 - e^{-\frac{1}{f\tau}} \approx \frac{1}{f\tau}$$

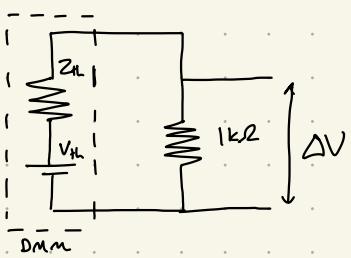
$$\frac{\Delta V}{V_0} \approx \frac{1}{f\tau}$$

Lab Exercises:

Problem R3.1

a) $V_{th} = 2.994 \text{ V}$

$\Delta V = 882 \text{ mV}$



$$\Delta V = \frac{R}{R + Z_{th}} V_{th} \Rightarrow \frac{\Delta V}{V_{th}} (R + Z_{th}) = R \Rightarrow Z_{th} = \frac{V_{th}}{\Delta V} \left(1 - \frac{\Delta V}{V_{th}}\right) R = \frac{2.994}{0.882} \left(1 - \frac{0.882}{2.994}\right) (1000) = 2394.6 \Omega \approx 2.4 \text{ k}\Omega$$

$$\Delta V = \frac{(2 \text{ k}\Omega)}{(2 \text{ k}\Omega) + (2.4 \text{ k}\Omega)} (2.994 \text{ V}) = 1.36 \text{ V}$$

actual ΔV for $R = 2 \text{k}\Omega$ was recorded to be $\approx 1.368 \text{ V}$

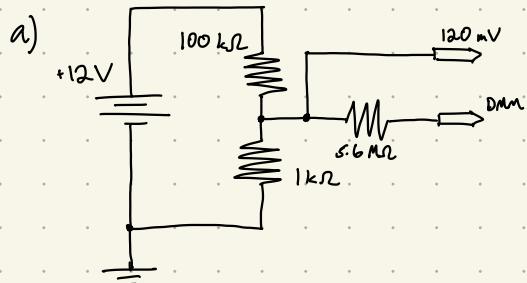
b) DMM Readings:

forward-bias: $V = 0.610 \text{ V}$

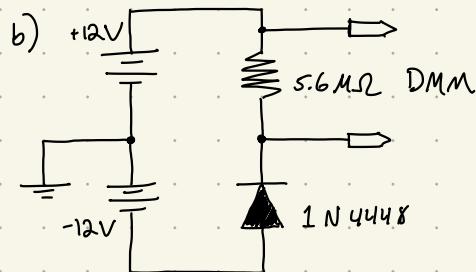
reverse-bias: $V = 1$ (registered as an overload)

In reverse-bias the diode doesn't let current through so it can be said to have a very high impedance and therefore high voltage drop reading causing the DMM to read it as an overload.

Problem R 3.2



without $5.6\text{ M}\Omega$ resistor: $V = 119.9\text{ mV}$
with $5.6\text{ M}\Omega$ resistor: $V = 77.0\text{ mV}$



$$V = 32.1\text{ mV}$$

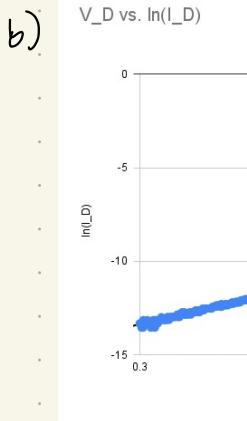
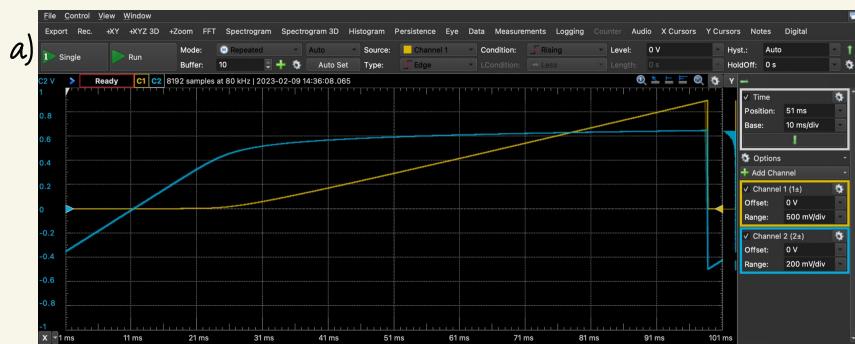
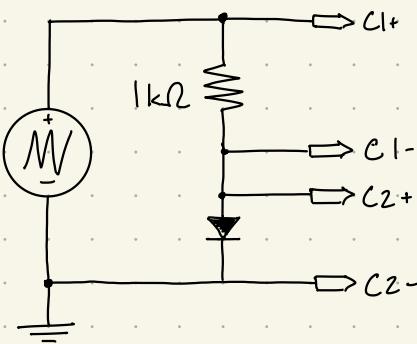
The voltage across the resistor was higher after warming up the diode for a short-time.

$$V = -149\text{ mV} \text{ with the } -3.3 \text{ and } -12\text{ V reverse voltages}$$

Increasing the diodes temperature makes it less effective at stopping current in reverse bias, causing the total current in the circuit to increase, and in turn increasing the voltage drop across the resistor.

The leakage current is not dependent on reverse voltage.

Problem R3.3



$$\text{slope} : 21.1 = \frac{1}{nV_T}, V_T = \frac{kT}{e} \Rightarrow 21.1 = \frac{e}{n k T} \Rightarrow n = \frac{e}{21.1 k T} = \frac{1.6 \times 10^{-19}}{21.1 (1.38 \times 10^{-23})(293)} = 1.88$$

$$\text{intercept} : -19.7 = \ln(I_s) \Rightarrow I_s = e^{-19.7} = 2.78 \text{ nA}$$

$$c) I_0(V_0) = I_s \exp\left(\frac{eV_0}{n k T}\right), n=1.88, I_s=2.78 \text{ nA}$$

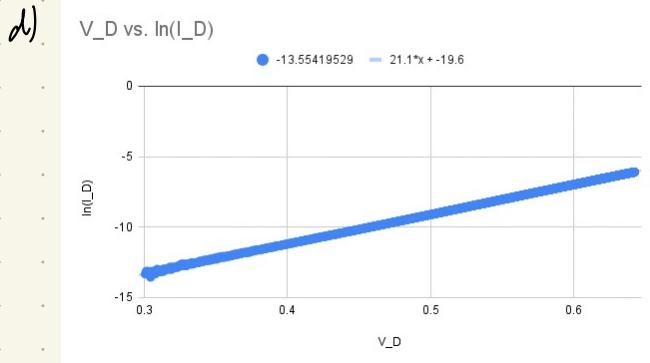
$$I_0(V_0) = (2.78 \text{ nA}) \exp\left(\frac{eV_0}{1.88 k T}\right)$$

$$V_0 = 0.4 \text{ V}, I_0 = 12.6 \mu\text{A} \quad \text{measured } I_0 = 12.68 \mu\text{A} \quad \% \text{ diff} = 0.63\%$$

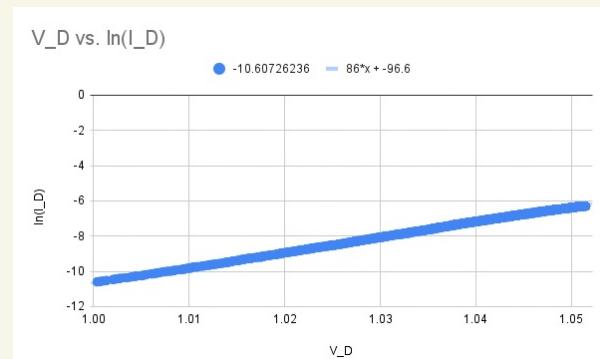
$$V_0 = 0.5 \text{ V}, I_0 = 103.4 \mu\text{A} \quad \text{measured } I_0 = 104.4 \mu\text{A} \quad \% \text{ diff} = 0.97\%$$

$$V_0 = 0.6 \text{ V}, I_0 = 848.6 \mu\text{A} \quad \text{measured } I_0 = 869.1 \mu\text{A} \quad \% \text{ diff} = 2.4\%$$

The predicted values are all very close the measured ones.



warm diode

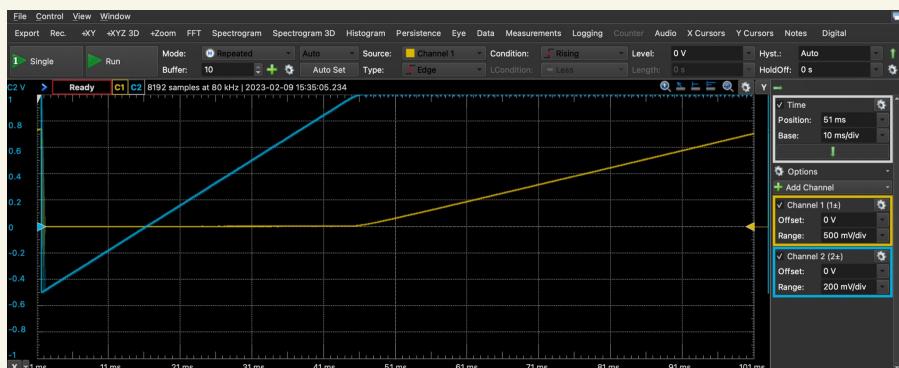


cold diode

$$\text{slope: } 21.1 = \frac{1}{nV_T}, \quad V_T = \frac{kT}{e} \Rightarrow 21.1 = \frac{e}{nkT} \Rightarrow n = \frac{e}{21.1 kT} = \frac{1.6 \times 10^{-19}}{21.1 (1.38 \times 10^{-23})(293)} = 1.88$$

$$\text{intercept: } -19.6 = \ln(I_s) \Rightarrow I_s = e^{-19.6} = 3.07 \text{ nA}$$

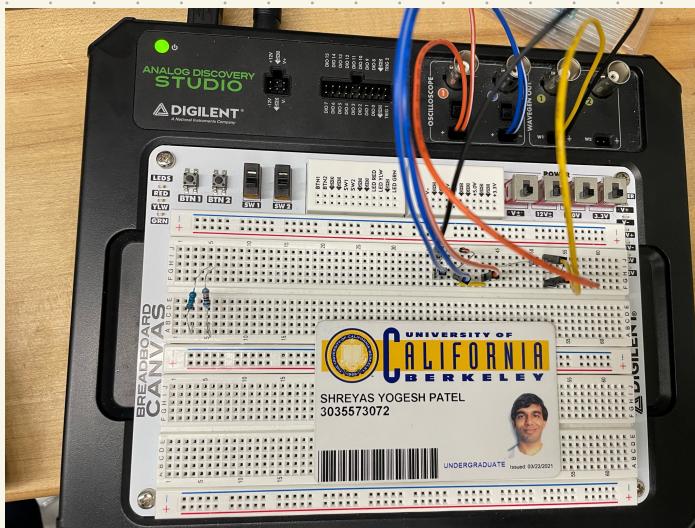
Cold Diode ($T = 77 \text{ K}$)



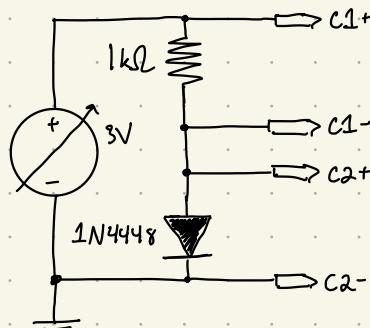
$$\text{slope: } 86 = \frac{1}{nV_T}, \quad V_T = \frac{kT}{e} \Rightarrow 86 = \frac{e}{nkT} \Rightarrow n = \frac{e}{86 kT} = \frac{1.6 \times 10^{-19}}{86 (1.38 \times 10^{-23})(77)} = 1.75$$

$$\text{intercept: } -96.6 = \ln(I_s) \Rightarrow I_s = e^{-96.6} = 1.11 \times 10^{-42} \text{ A}$$

The data shifts by having a greater slope and much lower intercept.



Problem R3.4



$$a) V_D = 586 \text{ mV}$$

$$V_R = 390 \text{ mV}$$

$$V_D + V_R = 976 \text{ mV} = 0.976 \text{ V}$$

$$I_D = \frac{V_R}{R} = \frac{390 \text{ mV}}{1 \text{ k}\Omega} = 390 \mu\text{A}$$

| Wavegen V (V) | V_D (V) | V_R (V) | $V_D + V_R$ (V) | I_D (mA) |
|---------------|-----------|-----------|-----------------|------------|
| 0.6 | 0.512 | 0.078 | 0.580 | 0.078 |
| 1 | 0.586 | 0.39 | 0.976 | 0.39 |
| 3 | 0.658 | 2.228 | 2.886 | 2.228 |
| 5 | 0.688 | 4.108 | 4.796 | 4.796 |

| Wavegen V (V) | V_D (V) | V_R (V) | $V_D + V_R$ (V) | I_D (mA) |
|---------------|-----------|-----------|-----------------|------------|
| 1 | 0.478 | 0.514 | 0.992 | 51.4 |
| 3 | 0.552 | 2.486 | 2.988 | 243.6 |
| 5 | 0.582 | 4.4 | 4.982 | 440 |

$$c) n = 1.88, I_s = 2.78 \text{ nA}, T = 293.15 \text{ K}, V_D = 2.886 \text{ V}, k = 1.38 \times 10^{-23} \text{ J K}^{-1}$$

$$i) \frac{V_o - V}{R} = I_D \Rightarrow \frac{V_o - V}{R} = I_s \exp\left(\frac{eV_D}{nKT}\right) \Rightarrow \exp\left(\frac{eV_D}{nKT}\right) = \frac{V_o - V}{I_s R} \Rightarrow V_D = \frac{nKT}{e} \ln\left(\frac{V_o - V}{I_s R}\right)$$

$$V_D = \frac{(1.88)(1.38 \times 10^{-23})(293.15)}{1.6 \times 10^{-19}} \ln\left(\frac{0.114 \text{ V}}{(2.78 \times 10^{-9})(10000)}\right) = 1.49 \text{ V}$$

$$ii) I_D = \frac{3 \text{ V}}{1 \text{ k}\Omega} = 3 \text{ mA}$$

$$V_D = \left(\frac{nKT}{e}\right) \ln\left(1 + \frac{I_D}{I_s}\right) \Rightarrow \frac{1.88(1.38 \times 10^{-23})(293.15)}{1.6 \times 10^{-19}} \ln\left(1 + \frac{3 \text{ mA}}{2.78 \text{ nA}}\right) = 0.66 \text{ V}$$

$$I_D = \frac{V_o - V}{R} = \frac{3 - 0.66 \text{ V}}{1 \text{ k}\Omega} = 2.351 \text{ mA}$$

$$V_D = 0.649 \text{ V}$$

$$I_D = \frac{3 - 0.649 \text{ V}}{1 \text{ k}\Omega} = 2.351 \text{ mA}$$

$$V_D = 0.649 \text{ V}$$

$$iii) V_o - V_D - R I_s \left[\exp\left(\frac{eV_D}{nKT}\right) - 1 \right] = 0$$

$$V_D = 0.649 \text{ V}$$

Problem R3.5

a) $R = 1 \text{ k}\Omega$

$$V_{D_0} = 0.663 \text{ V}$$

$$V_d = 14.9 \text{ mV}$$

$$V_{R_0} = 3.17 \text{ V} \Rightarrow I_{D_0} = 3.17 \text{ mA}$$

$$V_R = 0.93 \text{ V} \Rightarrow i_d = 930 \mu\text{A}$$

$$r_d = \frac{V_d}{i_d} = \frac{14.9 \text{ mV}}{0.251 \text{ mA}} = 16.02 \Omega$$

b) $R = 10 \text{ k}\Omega$

$$V_{D_0} = 0.557 \text{ V}$$

$$V_d = 13.4 \text{ mV}$$

$$V_{R_0} = 3.42 \text{ V} \Rightarrow I_{D_0} = 0.342 \text{ mA}$$

$$V_R = 0.97 \text{ V} \Rightarrow i_d = 97 \mu\text{A}$$

$$r_d = \frac{V_d}{i_d} = \frac{13.4 \text{ mV}}{0.097 \text{ mA}} = 138.14 \Omega$$

c) $R = 1 \text{ k}\Omega$, $\frac{V_d}{V_{in}} = \frac{14.9 \text{ mV}}{1 \text{ V}} = 14.9 \times 10^{-3}$

$$\frac{V_d}{V_{in}} = \frac{r_d}{R + r_d} = \frac{16.02 \Omega}{1000 \Omega + 16.02 \Omega} = 15.77 \times 10^{-3}$$

$$R = 10 \text{ k}\Omega, \quad \frac{V_d}{V_{in}} = \frac{13.4 \text{ mV}}{1 \text{ V}} = 13.4 \times 10^{-3}$$

$$\frac{V_d}{V_{in}} = \frac{r_d}{R + r_d} = \frac{138.14 \Omega}{10000 \Omega + 138.14 \Omega} = 13.6 \times 10^{-3}$$

The expected ratios are consistent with the measured ones.

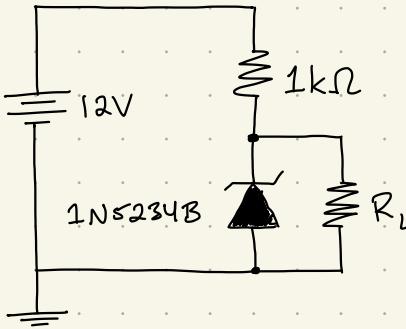
d) $r_d = \frac{nV_T}{eI_{D_0}} = \frac{nkT}{eI_{D_0}}$

$$R = 1 \text{ k}\Omega, \quad r_d = \frac{(1.88)(1.38 \times 10^{-23})(293)}{(1.6 \times 10^{-19})(3.17 \times 10^{-3})} = 14.99 \Omega$$

$$R = 10 \text{ k}\Omega, \quad r_d = \frac{(1.88)(1.38 \times 10^{-23})(293)}{(1.6 \times 10^{-19})(0.342 \times 10^{-3})} = 138.92 \Omega$$

The measured diode dynamic impedances are very close and consistent with the expected values.

Problem R3.6



a) V_{B0} for 1N4448 = 6.2V

$$V_R = 5.8V \Rightarrow I_R = \frac{V_R}{R} = 5.8mA$$

For the minimum load, I_D is negligible in comparison to I_R , so
 $I_R = I_{R_L} \Rightarrow R_L = \frac{V_{R_L}}{I_{R_L}} = \frac{6.2V}{5.8mA} = 1.069k\Omega$

b) before R_L : $V_i = 6.252V$, $V_R = 5.766V \Rightarrow I_2 = \frac{V_R}{R} = 5.766mA$

after R_L : $V_i = 6.248V$, $V_R = 5.77V \Rightarrow I_2 = \frac{V_R}{R} = 5.77mA$, $I_{R_L} = \frac{V_R}{R_L} = \frac{6.248}{1000} = 0.62mA$

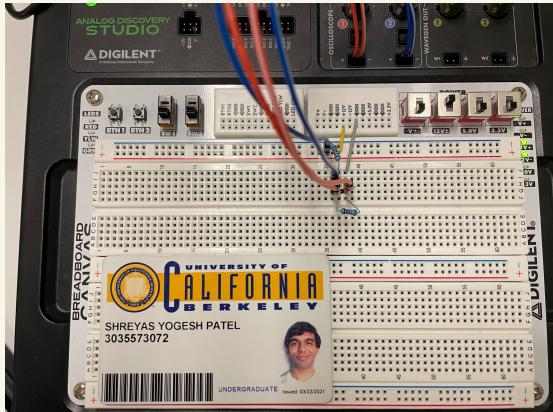
$$\Delta V_i = -0.004V, \Delta I_2 = (5.77 - 5.766 - 0.62) mA = -0.616mA$$

$$r_2 = \frac{\partial V_i}{\partial I_2} = \frac{0.004V}{0.616mA} = 0.00649k\Omega = 6.49\Omega$$

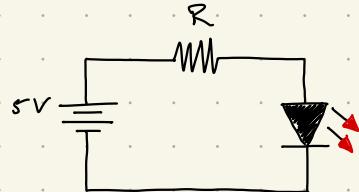
c) $V_{out} \approx 6.25V$, $r_2 = 6.49\Omega \Rightarrow I = 0.963A$

$$P = IV = (6.25)(0.963) = 6.01875W$$

The circuit wouldn't work because the power dissipated by the resistor would exceed its rating.



Problem R 3.7



a) $V_D = 1.5 \text{ V}$
 $V_R = 3.5 \text{ V}$, $I_o = 10 \text{ mA}$
 $R = \frac{V_R}{I_o} = \frac{3.5 \text{ V}}{10 \text{ mA}} = 0.35 \text{ k}\Omega = 350 \Omega$

actual: $V_D = 1.618 \text{ V} \Rightarrow V_R = 3.382 \text{ V} \Rightarrow R = \frac{3.382 \text{ V}}{10 \text{ mA}} = 338.2 \Omega$

$V_R = 3.41 \text{ V}$, $R = 337.5 \Omega \Rightarrow I_o = \frac{V_R}{R} = \frac{3.41 \text{ V}}{337.5 \Omega} = 10.1 \text{ mA}$

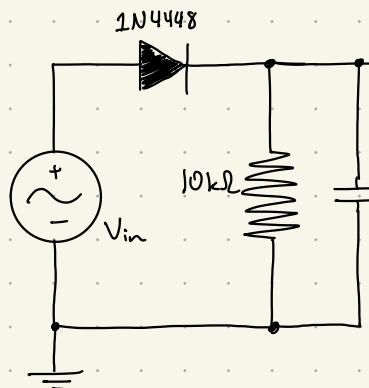
b) $V_D = 1.5 \text{ V} \Rightarrow V_R = 22.5 \text{ V} \Rightarrow I_o = \frac{V_R}{R} = \frac{22.5 \text{ V}}{100 \text{ k}\Omega} = 0.225 \text{ mA}$

actual $V_D = 1.751 \text{ V}$, $h = \frac{E_a \lambda}{C}$, $E_a = \frac{e(V_T - V_a T_1)}{T_2 - T_1} = \frac{e(V_T - V_a T_1) \lambda}{T_2 - T_1} C$

Red: $T_1 = 22^\circ\text{C} = 293.15 \text{ K}$, $V_1 = 1.754 \text{ V}$, $E_a = \frac{(1.6 \times 10^{-9})(1.754(260.15) - 1.766(293.15))}{260.15 - 293.15} = 2.98 \times 10^{-9}$
 $T_2 = -13^\circ\text{C} = 260.15 \text{ K}$, $V_2 = 1.766 \text{ V}$; $h = E_a \frac{\lambda}{C} \cdot (2.98 \times 10^{-9}) \left(\frac{650 \times 10^{-9}}{3 \times 10^8} \right) = 6.45 \times 10^{-34} \text{ J.s}$

Green: $T_1 = 22^\circ\text{C} = 293.15 \text{ K}$, $V_1 = 1.792 \text{ V}$, $E_a = \frac{(1.6 \times 10^{-9})(1.792(260.15) - 1.827(293.15))}{260.15 - 293.15} = 3.36 \times 10^{-9}$
 $T_2 = -13^\circ\text{C} = 260.15 \text{ K}$, $V_2 = 1.827 \text{ V}$; $h = E_a \frac{\lambda}{C} \cdot (3.36 \times 10^{-9}) \left(\frac{650 \times 10^{-9}}{3 \times 10^8} \right) = 6.34 \times 10^{-34} \text{ J.s}$

Problem R3.8



$$a) \Delta V = V_{in} - V_{out} = 2.4895V - 1.9495V = 0.54V$$

$$I_D = I_S \exp\left(\frac{eV_0}{n k T}\right) \Rightarrow \frac{eV_0}{n k T} = \ln\left(\frac{I_D}{I_S}\right) \Rightarrow V_0 = \frac{n k T}{e} \ln\left(\frac{I_D}{I_S}\right)$$

$$I_D = \frac{V_0}{R} = \frac{1.9495V}{10k\Omega} = 0.195mA, V_0 = \frac{(0.88)(1.38 \times 10^{-23})(293)}{(1.6 \times 10^{-19})} \ln\left(\frac{0.195 \times 10^{-3}}{2.78 \times 10^{-9}}\right) = 0.53$$

$$b) V_D = 0.39V$$

The diode voltage is a little less than the voltage difference from part a.

$$c) V_{pp} = 218.60mV$$

$$\frac{\Delta V}{V_0} = \frac{1}{fRC}, R = 10k\Omega, C = 10\mu F, f = 100Hz$$

$$\exp V_{pp} = \frac{V_0}{fRC} = \frac{2.5}{(100)(10k\Omega)(10\mu F)} = 0.25V = 250mV$$

$$\% \text{ diff} = 12.56\%$$

$$i) f = 200Hz$$

$$V_{pp} = 118.5mV$$

$$\exp V_{pp} = \frac{2.5}{(200)(10k\Omega)(10\mu F)} = 0.125V = 125mV$$

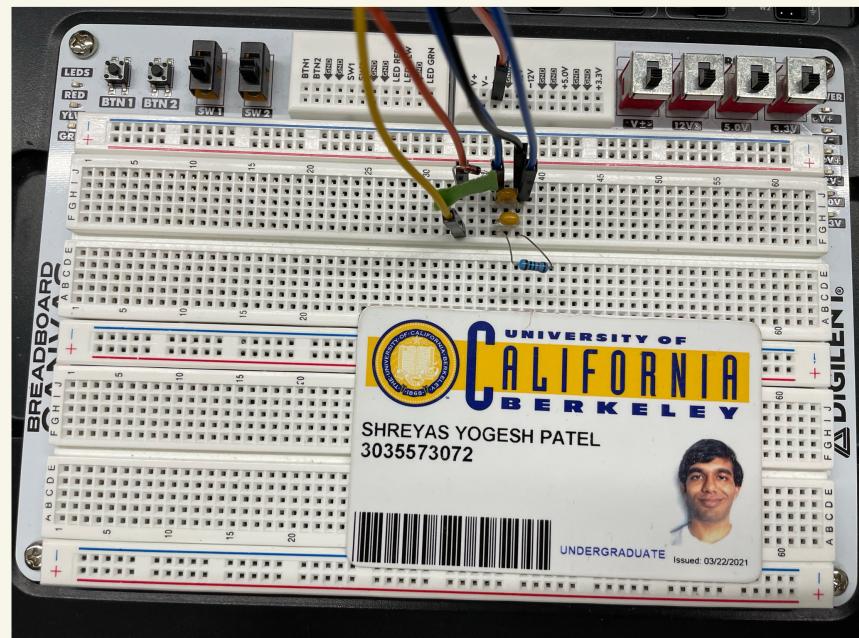
$$\% \text{ diff} = 5.2\%$$

$$ii) C = 20\mu F$$

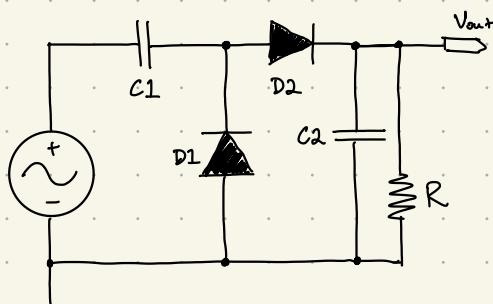
$$V_{pp} = 118.5mV$$

$$\exp V_{pp} = \frac{2.5}{(100)(10k\Omega)(20\mu F)} = 125mV$$

$$\% \text{ diff} = 5.2\%$$



Problem R3.9



$$C_1 = C_2 = 10 \mu F$$

$$D_1 = D_2 = 1N4448$$

$$R = 3 k\Omega$$

$$c) V_{rms} = 4.76 \text{ mV}$$

The ripple is reduced by a factor of 16

$$a) \text{expected } V_{out} \approx 2V_0 - 1.2V = 10V - 1.2V = 8.8V$$

$$\text{measured } V_{out} \approx 8.87V$$

$$b) I_{peak} = \frac{V}{R} = \frac{6.6V}{3k\Omega} = 2.2 \text{ mA}$$

$$V_{KMS} = 76.62 \text{ mV}$$

$$r_2 = 6.49 \Omega \Rightarrow I_2 = \frac{V}{r_2} = \frac{4.76 \text{ mV}}{6.49 \Omega} = 0.733 \text{ mA}$$

$$I_{max} = 2.2 \text{ mA} - 0.733 \text{ mA} = 1.467 \text{ mA}$$

