

$$(c) \int_0^3 \delta(t) \sin 5\pi t \, dt$$

Solⁿ: We know, $\delta(t) = \begin{cases} 1, & t=0 \\ 0, & \text{elsewhere} \end{cases}$

$$\begin{aligned} \therefore \int_0^3 \delta(t) \sin 5\pi t \, dt &= \left[\sin 5\pi t \right]_{t=0} \\ &= 0 \end{aligned}$$

$$(d) \int_{-2}^{\infty} (t-2)^3 \delta(t-2) dt$$

Solⁿ. We know,

$$\delta(t-2) = \begin{cases} 1, & t=2 \\ 0, & \text{elsewhere} \end{cases}$$

$$\begin{aligned} \therefore \int_{-2}^{\infty} (t-2)^3 \delta(t-2) dt \\ &= \left[(t-2)^3 \right]_{t=2} \\ &= 0 \end{aligned}$$