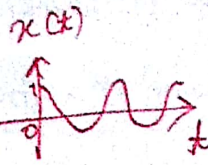
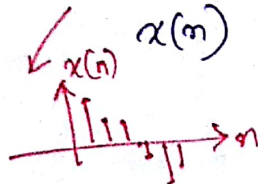


SIGNALS

Continuous-time s/g - defined for all instants of time

 $x(t)$ 

Discrete-time s/g - defined only at discrete instants of time -



* Meaning of discrete - individually separate & distinct.

* Continuous time signals represented by $x(t)$ and discrete time signals represented by $x(n)$, where t and n are independent variables in time domain.

* Four ways of representing discrete-time signals. They are -

- ① Graphical Representation.
- ② Functional Representation.
- ③ Tabular Representation.
- ④ Sequence Representation.

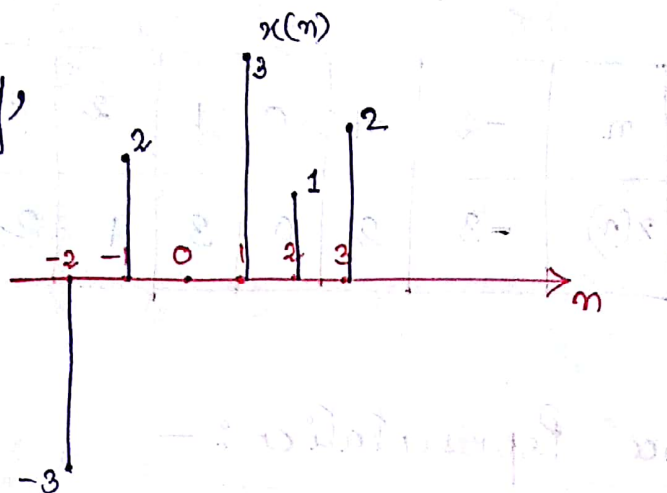
① Graphical Representation :-

Let us consider a s/g $x(n)$ with values

$$x(-2) = -3, \quad x(-1) = 2, \quad x(0) = 0, \quad x(1) = 3$$

$$x(2) = 1 \quad \text{and} \quad x(3) = 2$$

Graphically,



② Functional Representation :-

In this, amplitude of the signal is written against the value of 'n'.

$$\text{Ex:- } ① \quad x(n) = \begin{cases} -3 & \text{for } n = -2 \\ 2 & \text{for } n = -1 \\ 0 & \text{for } n = 0 \\ 3 & \text{for } n = 1 \\ 1 & \text{for } n = 2 \\ 2 & \text{for } n = 3 \end{cases}$$

$$② \quad x(n) = \begin{cases} 2^n, & \text{for } n \geq 0 \\ 0, & \text{for } n < 0 \end{cases}$$

Sampling is defined as the process of measuring the instantaneous values of continuous time s/g in a discrete form.

③ Tabular representation:-

Sampling instant 'n' and the magnitude of the signal at the sampling instant are represented in tabular form.

n	-2	-1	0	1	2	3
x(n)	-3	2	0	3	1	2

④ Sequence Representation:-

$$x(n) = \{-3, 2, 0, 3, 1, 2\}$$

* Arrow mark '↑' denotes that n=0 term.
When no arrow is indicated, the first term corresponds to n=0

$$x(n) = \{-3, 1, 0, 3, 1, 2\}$$

SUM & PRODUCT OF DISCRETE-TIME SEQUENCE:-

$$\{c_n\} = \{a_n\} + \{b_n\} \rightarrow c_n = a_n + b_n$$

$$\{c_n\} = \{a_n\} \cdot \{b_n\} \rightarrow c_n = a_n \cdot b_n$$

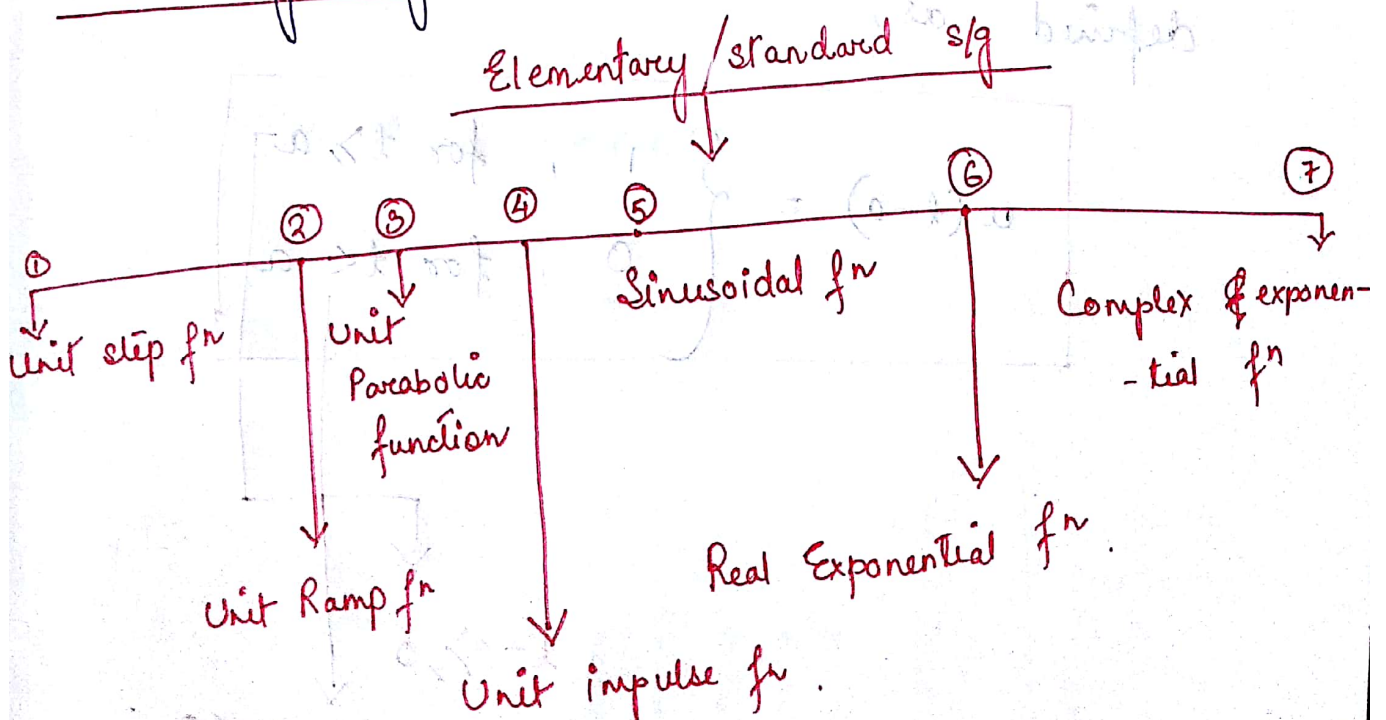
$$\{c_n\} = k \{a_n\} \rightarrow c_n = k a_n$$

↑ multiplication of a sequence by a constant, k , is obtained by multiplying each element of the sequence by that constant.

$$\{c_n\} = k \{a_n\}$$

$$\rightarrow c_n = k a_n$$

Elementary signals:-



① UNIT step-function

Step function :- exists only for the positive time & is zero for negative time.

Unit step function :- if a step function has unity magnitude.

Continuous-time unit step function $u(t)$ defined as,

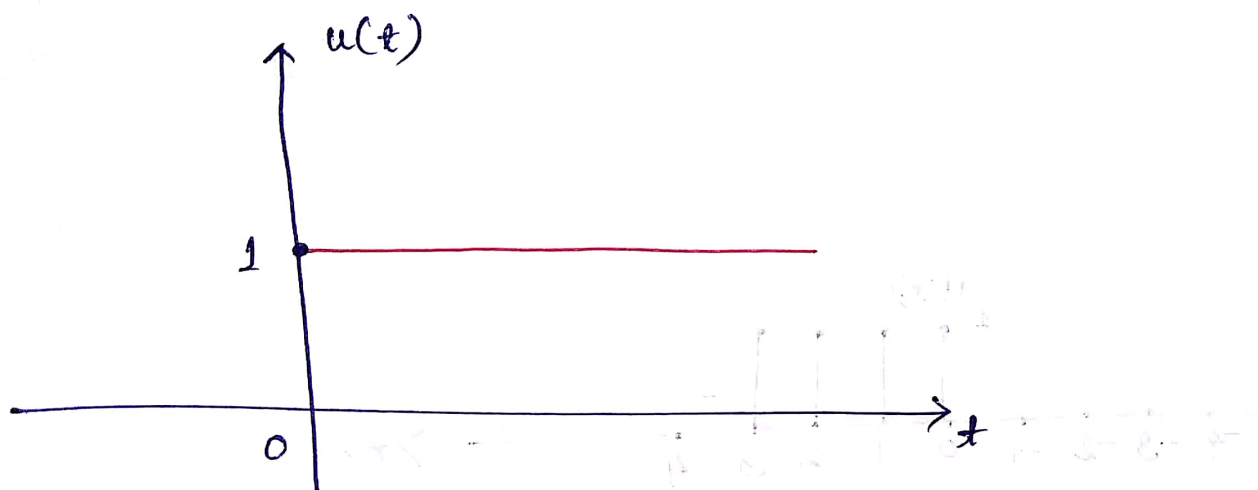
$$u(t) = \begin{cases} 1 & \text{for } t \geq 0 \\ 0 & \text{for } t < 0 \end{cases}$$

Shifted unit step function $u(t-a)$ defined as,

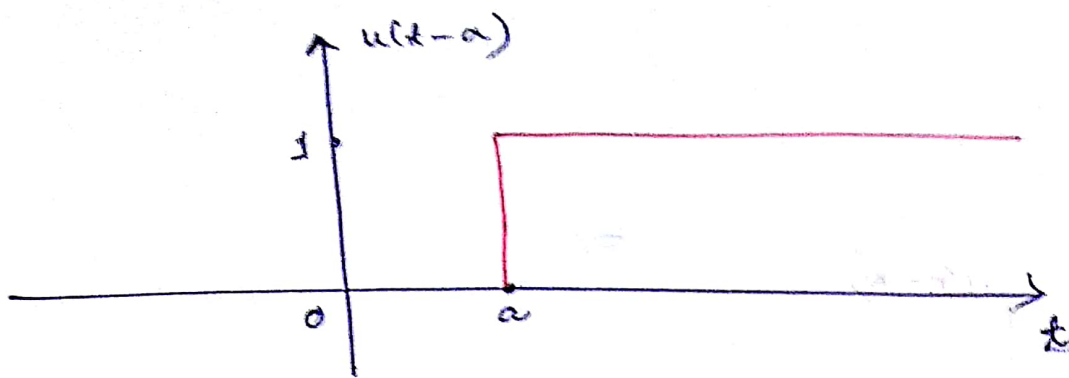
$$u(t-a) = \begin{cases} 1, & \text{for } t \geq a \\ 0, & \text{for } t < a \end{cases}$$

$t-a \geq 0$

$t-a < 0$



① unit step fn.

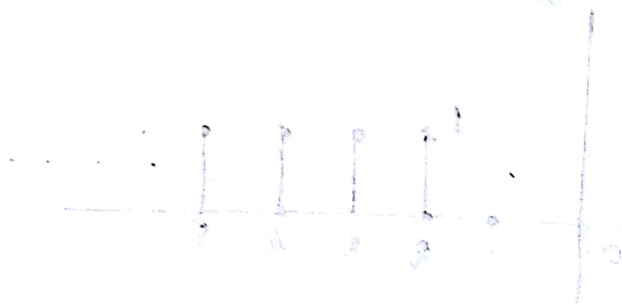


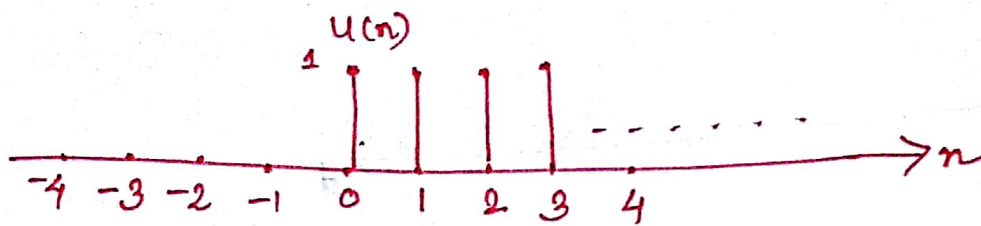
⑥ Delayed unit step function.

Discrete-time unit step function:-

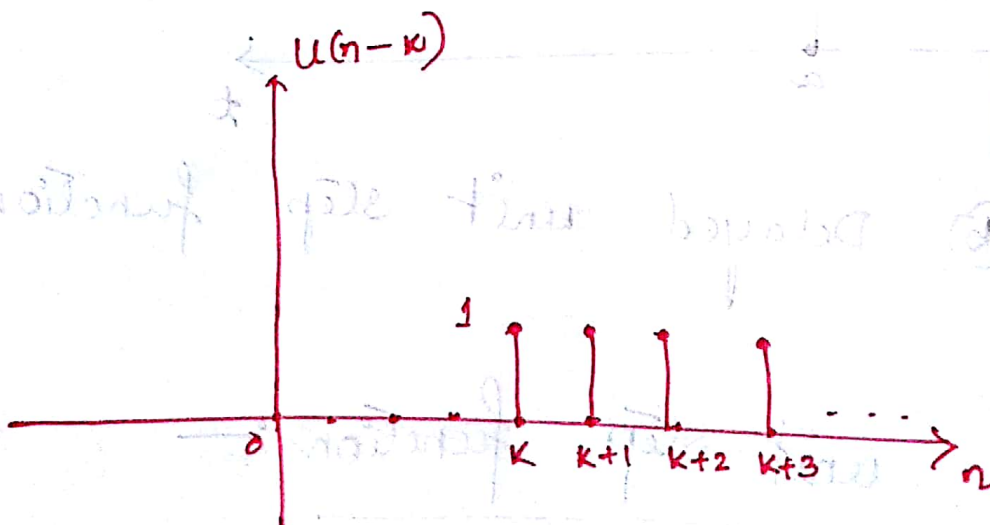
$$u(n) = \begin{cases} 1, & n \geq 0 \\ 0, & n < 0 \end{cases}$$

$$u(n-k) = \begin{cases} 1, & n \geq k \\ 0, & n < k \end{cases}$$





$u(n)$



$u(n-k)$

$$u(n-2) \Rightarrow ?$$

$$u(n-2) \Rightarrow \begin{cases} 1 & n \leq n \\ 0 & n > n \end{cases} = (n - n)$$

