CHI-SQUARE TEST (22 Test)

 χ^2 describes the magnitude of discrepency been theory and observation.

eq: In tossing of a coin 200 times, the theoritical considerations leads to a result giving head 100 times and tail 100 times but these healts one rarely a chievable.

If 0_i (i=(1,1,3,...) is a set of observed (experimental) frequencies and E_i (i=1,2,...,n) is the corresponding set of expected (theoretical) frequencies. Then $\chi^2 = \sum_{i=1}^n \left[\frac{(0_i - E_i)^2}{E_i} \right]$

where $\Sigma 0^{\circ} = \Sigma E^{\circ} = N$ degree of freedom $(d \cdot f \cdot) = n - 1$ Note: (1) 16 $\chi^2 = 0$ then observed and expected forg.

(2) If $\chi^2 > 0$ then they don't agree exactly.

Degree of Freedom

Degree of Freedom (d.f.), v = n - k

where n = total no. of obs.

K = ro. of independent constraints

B. The following table gives the no. of unidents that took place in an industry various days of the week. Test it accidents are uniformly dictaributed over the week.

Day M T W TR F S No. of accident 14 18 12 11 15 14 Som:

Null typothesis Ho: The accidents one uniformly distributed over the week.

Under Ho, the expected forego of accidents on each day = $\frac{84}{6}$ = 14

Observed Freq. Oi	17	18	(2	11	15	14	
Expected foug. Ei	14	14	(4	14	14	14	
(0:-Ei)2	0	16	4	٩	1	0	

$$\chi^2 = \frac{\sum (0i - Ei)^2}{Ei}$$

$$=\frac{30}{14}$$

Significance:
$$5\%$$

$$n = 6$$

$$d._{\xi} = n - 1$$

$$= 5$$

Conclusion: Table value of X^2 at 5% level ob significance for (6-1-)5 d.b is 11.070

5% = 0.05 1 Level of significance

ROW - 5 (dt)

Co(m - 0.05)

Ans - 11.070

" o calculated value of χ^2 is less than tabulated value

os Ho is accepted

i.e. The accidents on uniformly distributed over the week.

S- A die is thrown 270 times and the results of these throws are given below

Mar on the die 1 2 3 4 5 6
Frequency 40 32 29 59 57 59

Test whether the die is biased on not.

9. Records taken of the number of male and bemale births in 800 femilies having four children are as follows

No. of male births	0	1	2	3	· ·
No. of female births	4	3	2	1	٥
No. 07	31	178	290	236	94

test whether the data are consistent with the hypothesis that the binomal law holds and the chance of male birth is equal to that of female namely p=q=1/2

Som: Ho: The data are consistent with the hypothesis of equal perobability for male and temple birth. i.e. $P = 9 = \frac{1}{2}$.

The theoretical frequency is given by $N(92) = N \times P(X=92)$ Here, N= total freq. N(91) = ro. of Jamilies with a male children

 $p(x-9) = {}^{n}c_{\pi} p^{9}q^{n-9}$

where p = prob. of a male both q = 1 " " benale " n = no. of Children

 $N(0) = N_0$, families with 0 male children $= N \times P(X=0)$ $= 800 \left(\frac{4}{5} \left(\frac{1}{5}\right)^4\right)^4$ $= 800 \times \frac{1}{2} = 50$

$$N(1) = 800 \times I(x=1) = 800 \left({^{1}C_{1}(\frac{1}{2})^{1}(\frac{1}{2})^{3}} \right)$$

$$= 200$$

$$N(2) = 800 \cdot P(x = \lambda) = 800 \left[4c_2 \left(\frac{1}{2} \right)^2 \left(\frac{1}{2} \right)^2 \right]$$

$$= 300$$

$$N(3) = 800 \times P(x=3) = 800 \left[\frac{1}{4} \cdot 3 \left(\frac{1}{7} \right) \right]$$

$$N(4) = 800 \times P(X=4) = 800 \left[4c_4 \left(\frac{1}{2} \right)^4 \right]$$
= 50

observed Frequency 0?	32	178	290	236	94
Expedded Friguely Ei	50	200	<i>3</i> 00	200	50
0; - E;	-18	-22	- 1 <i>D</i>	36	44
(O;-E;)2	324	484	(00	1296	(936
(0;-t;)2	6.48	2.42	Q, } <i>}</i> }	6.48	38.72

$$\chi^2 = \frac{5(0i-Ei)^2}{Ei} = 54.433$$

Conclusion? Table value of 2° at 5%

level of significance for 5-1=4 d.f. is 9.488

... calculated value of 2° to greater than

the tabulated value
... Ho is sujected

Hence, the data are not consistent with the hypothesis that the binomial law holds and that the powbubility of male and beneal with it same.

g. fit a Poisson distribution distribution to the following data and best the goodness of fit

Tm1	٥	1	2	3	4
 	109	65	22	3	l

Mode:

- Of the data is given in a series of 'n' numbers then d.f. = n-1
- a) in case of Binomial dist, d.f=n-1
- (3) " Poisson dist., d.6=n-2
- (4) " " Normal dist., dif = n-3.