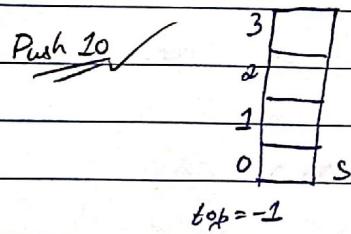


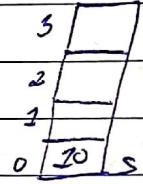
(8)

Implementation of stack using array :-

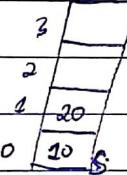
- Elements will be kept in an array.
- We need one variable to keep track of the "top" of the stack.



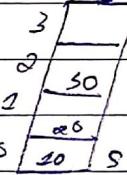
$$\begin{aligned} \text{top} &= \text{top} + 1; \\ \text{top} &= 0 \\ s[\text{top}] &= 10 \end{aligned}$$

Push 20

$$\begin{aligned} \text{top} &= \text{top} + 1 \\ \therefore \text{top} &= 1 \\ s[\text{top}] &= 20 \end{aligned}$$

Push 30

$$\begin{aligned} \text{top} &= \text{top} + 1 \\ \text{top} &= 2 \\ s[\text{top}] &= 30 \end{aligned}$$

Push 40

$$\begin{aligned} \text{top} &= 3 \\ \therefore \text{top} &= 3 \\ s[\text{top}] &= 40 \end{aligned}$$

Stack overflow :-

→ when the value of top reaches (max. size - 1)
we cannot push any more element as there is no more space in the array.

Procedure $\text{push}(S, \text{MAXSIZE}, \text{top}, \text{element})$

1. If ($\text{top} == \text{MAXSIZE}-1$) Then
2. Write ("Stack Overflow").
3. Return.
4. End If.
5. $\text{top} = \text{top} + 1$
6. $S[\text{top}] = \text{element}$
7. Return.

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Procedure $\text{pop}(S, \text{top})$

1. If ($\text{top} == -1$) Then
2. Write ("stack underflow")
3. Return.
4. End If
5. Write ("Deleted Element: ", $s[\text{top}]$)
6. $\text{top} = \text{top} - 1$
7. Return

Procedure $\text{display}(S, \text{top})$

1. If ($\text{top} == -1$) Then
2. Write ("Stack underflow")
3. Return.
4. End If
5. Repeat step 6 for $I = 0, 1, \dots, \text{top}$
6. Write ("The Element: ", $s[I]$)
7. Return.

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The C Programming language
by — Kernighan & Ritchie.

```
#define <stdio.h>
#define maxsize 20
int s[maxsize], top;
int main() {
    top = -1;
    return 0;
}
push();
push();
pop();
push();
display();
return 0;
}

void push() {
    int element;
    printf("Element: ");
    scanf("%d", &element);
    if (top == maxsize - 1)
        printf("Stack Overflow\n");
    else {
        s[top + 1] = element;
        top++;
    }
}
```

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Lecture-7

```
void pop() {
    if (top == -1)
        printf("Stack underflow");
    else {
        printf("Popped element is: %d\n", s[top]);
        top = top - 1;
    }
}
```

* → or can be combined as

```
printf("Popped Element is: %d\n", s[top - 1]);
```

`void display()` {

 int i;

 for ($i=0$; $i \leq top$; $i++$)

 printf("Element is: %d\n", $a[i]$);

 return;

 for top to bottom

 for ($i=top$; $i \geq 0$; $i--$)

 printf ---

[+ Array is implicitly passed by reference.]

Queue

A queue is a linear list where all the insertions are done at one end of the list (known as rear) and all the deletions are done at the other end of the list (known as front). A queue exhibits FIFO property.

Example:-

Insert: 10 20 30

()

(10)

(10 20)

(10 20 30)

Delete: Deleted element is 10

(20, 30)

Delete: Deleted element is 20

(30)

(12)

Delete : Deleted element is 30.

()

Insertion Order : 10 20 30 FIFO

Deletion Order : 10 20 30

Implementation of Queue using Array :

- We use an array to keep the elements of the queue.
- We need two more variables to track of the 'rear' end and the 'front' end.

We call these REAR and FRONT.

Q	0	1	2	3
	10	20		

Rear = 0 , Front = 0

① Insert 10 : Rear = Rear + 1

$$Q[Rear] = 10$$

$$Front = Front + 1$$

② Insert 20 : Rear = Rear + 1

$$Q[Rear] = 20$$

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③ Insert 30 : Rear = Rear + 1

$$Q[Rear] = 30$$

④ Insert 40 : Rear = Rear + 1

$$Q[Rear] = 40$$

⑤ Insert 50 : No more space in array.

Queue Overflow or Queue Full cond^a

Queue Overflow or Queue Full Condition.

Q	0	1	2	3
	10	20	30	40

Rear = 3, Front = 0

#define maxsize 4

int Q[maxsize];

To give error on Queue Overflow [prevent and return] we use :-

If (Rear == maxsize - 1)

Deletions :-

① Delete

② Front = Front + 1

Q	0	1	2	3
	10	20	30	40

#del :- Rear = 3, Front = 1

Queue is always from index 'Front' to index 'Rear'

2. Delete : Front = Front + 1 \rightarrow Rear = 3, Front = 2
20 is deleted.

③ Delete : Front = Front + 1 \rightarrow Rear = 3, Front = 3
30 is deleted

Q	0	1	2	3
	10	20	30	40

Rear = 3, Front = 3

④ In this case,

40 is deleted.

& Rear = -1, Front = -1 \rightarrow [Only set when last element i.e. when Front = Rear & $\neq -1$]

⑤ Delete :- Cannot because

Queue Underflow or Queue Empty Condition.

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Circular Queue :-

Initially, Rear = -1, Front = -1

maxsize = 4

Q	0	1	2	3
	10	20	30	40

Rear = 3, Front = 0

✓ Delete : $Q[Front]$ i.e. $Q[0] \rightarrow [Front = 1, Rear = 3]$

↑
[Insert 50 :- will be inserted at $Q[0]$]

✓ Delete $Q[1]$

| Insert 50

Insert 60)

Inversion circular, whenever
place available it fills. This
solves the space wastage problem
in normal queue..

Circularly Updated :-

→ modulus operator (%)

$$Rear = (Rear + 1) \bmod \text{maxsize}$$

Example when Rear = 3

$$Rear = (3+1) \% 4$$

$$= 4 \% 4$$

$$= 0$$

So, next insertion will be at $Q[0]$

Again insert,

$$Rear = (0+1) \% 4$$

$$= 1 \% 4$$

$$= 1$$

So after prev. insertion, Rear = 0

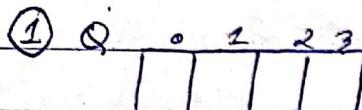
So, insertion will be at $Q[1]$

~~Circular update~~

Circular updating.

Complete e.g. on Circular Queue Insertion & Deletion:-

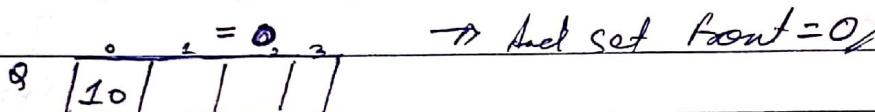
Insert 10, 20, 30, 40



$$\text{Rear} = -1, \text{Front} = -1$$

② Insert 10

$$\begin{aligned} \text{Rear} &= (\text{Rear} + 1) \% 4 \\ &= (-1 + 1) \% 4 \end{aligned}$$



$$\text{Rear} = 0, \text{Front} = 0$$

③ Insert 20

$$\begin{aligned} \text{Rear} &= (0 + 1) \% 4 \\ &= 1 \end{aligned}$$

0	1	2	3
10	20		

$$\text{Rear} = 1, \text{Front} = 0$$

④ Insert 30 :-

$$\begin{aligned} \text{Rear} &= (1 + 1) \% 4 \\ &= 2 \end{aligned}$$

0	1	2	3
10	20	30	

$$\text{Rear} = 2, \text{Front} = 0$$

⑤ Insert 40 :-

$$\begin{aligned} \text{Rear} &= (2 + 1) \% 4 \\ &= 3 \end{aligned}$$

0	1	2	3
10	20	30	40

$$\text{Rear} = 3, \text{Front} = 0$$

* Circ. Queue full cond :- (i) \rightarrow If ($\text{Front} == 0$) & ($\text{Rear} == \text{maxsize} - 1$)

⑥ Delete :-

Delete $Q[\text{Front}]$ i.e. $Q[0]$

$$\begin{aligned} \text{front} &= (\text{front} + 1) \% \text{maxsize} \\ &= (0 + 1) \% 4 \\ &= 1 \end{aligned}$$

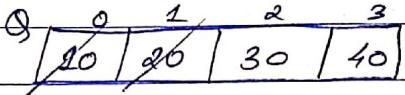
0	1	2	3
10	20	30	40

$$\text{Rear} = 3, \text{Front} = 1$$

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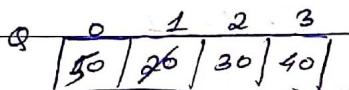
⑦ Delete:

$$\text{front} = (1+1) \% 4 \\ = 2$$



⑧ Insert 50:

$$\text{Rear} = (3+1) \% 4 \\ = 4 \% 4 \\ = 0$$

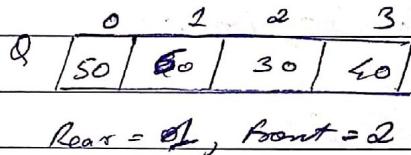


$$Q[Rear] = 50$$

$$\therefore Q[0] = 50$$

⑨ Insert 60:

$$\text{Rear} = (0+1) \% 4 \\ = 1$$



$$Q[Rear] = 60$$

$$\therefore Q[1] = 60$$

* If Queue full cond " → If $(\text{Rear} + 1) \% \text{maxsize} == \text{Front}$

-x-

Lecture - 9

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Normal Queue:

Insert: enqueue, Delete: dequeue

Procedure Enqueue(Q, Rear, Front, maxsize, element)

1. If $(\text{Rear} == \text{maxsize} - 1)$ Then

2. Write ("Queue Overflow")

3. Return

4. EndIf

5. $\text{Rear} = \text{Rear} + 1$

6. $Q[Rear] = \text{element}$

7. If $(\text{Front} == -1)$ Then

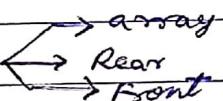
8. $\text{Front} = 0$

9. EndIf

10. Return

Procedure Dequeue (Q, Rear, Front)

1. If ($\text{front} == -1$) Then
2. Write ("Queue Underflow")
3. Return
4. EndIf
5. Write ("Element to be deleted : ", Q[front])
6. If ($\text{front} == \text{Rear}$) Then
7. $\text{Front} = \text{Rear} = -1$
8. Else
9. $\text{front} = \text{front} + 1$
10. EndIf
11. Return

C Implementation → Global 

- One fn for Enqueue
- One fn for Dequeue
- One fn for Display

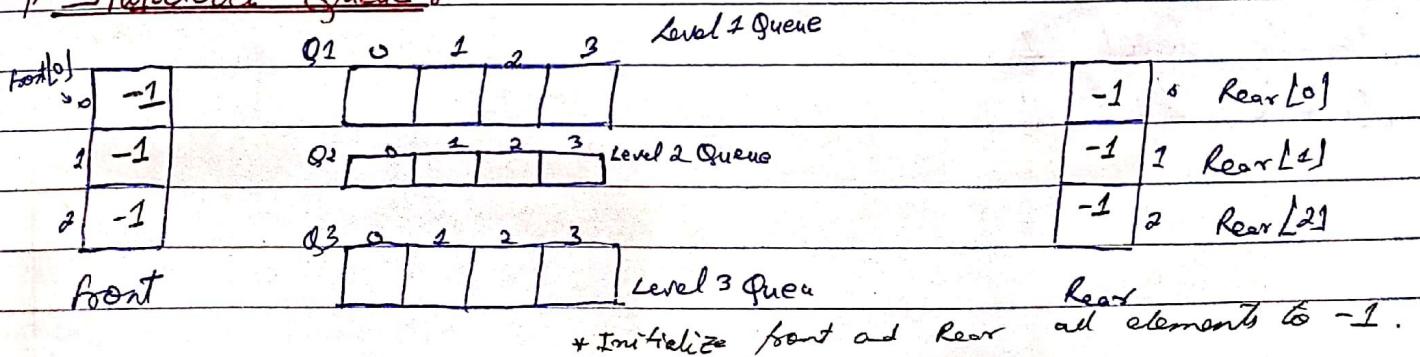
- Declare the array, rear, front locally within main
 - Pass the array, rear, front as arguments

→ ←

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Lecture - 10

Multilevel Queue :-



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Insert 10 to level 1

if ($\text{Rear}[0] == \text{maxsize} - 1$)

$$\text{Rear}[0] = \text{Rear}[0] + 1$$

$$Q_1[\text{Rear}[0]] = 10$$

$$Q_1[0] = 10$$

$$Front[0] = Front[0] + 1.$$

Insert 20 to level 1

$$\text{Rear}[0] = \text{Rear}[0] + 1$$

$$Q_1[\text{Rear}[0]] = 20$$

$$Q_1[1] = 20$$

Insert 30 to level 1

At the end,

Insert 40 to level 1

front[0]	Q1[0]	1	2	3	Level 1 Queue
0	10	20	30	40	

Insert 40 to level 2

front[0]	Q1[0]	1	2	3	Level 2 Queue	3	End[0]
0	Q2[0]	1	2	3		1	End[1]

Insert 50 to level 2

front[0]	Q1[0]	1	2	3	Level 2 Queue	1	2	End[1]
0	40	50				1	2	End[1]

Insert 60 to level 3

front[0]	Q1[0]	1	2	3	Level 3 Queue	Rear
0	60	70				

Insert 70 to level 3

front[0]	Q1[0]	1	2	3	Level 3 Queue	Rear
0	60	70				

Write ("Deleted Element: ", $Q1[Front[0]]$):

$$\text{Front}[0] = \text{Front}[0] + 1$$

Delete level 1

Delete level 1

Delete level 1

- This scheme can be used to implement multiple queues
- This scheme can also be used to implement a "priority queue".

Priority Queue

- Each element has a priority.
- Priorities are expressed using integers.
- ① Sometimes lower integers represent higher priority.
- ② Sometimes lower integers represent lower priority.

Element:

A	priority	0
B	priority	1

In a priority queue, the element with the highest priority is deleted first.

Normal FIFO queue



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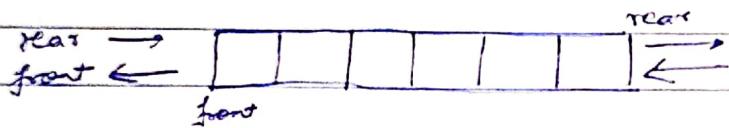
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Lecture - 11

Implementation of priority queue using multilevel queue :-

Double ended queue :-

Insertions and deletions can be done at both ends of the queue.



Linked Linear List (Linked List) :-

Static memory allocation

↳ memory allocated at compile time.

int *x;

n = 10;

Dynamic memory allocation

↳ memory allocated at run (execution) time.

e.g. malloc fn in C.

~~E.g.~~ struct node {

int roll;

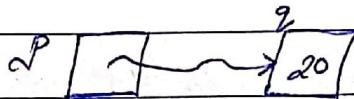
float cgpa;

?;

struct node *ptr;

e.g. malloc function in C

```
int *p;
int q;
p = &q;
*q = 20;
```



q refers to the contents of q by *p

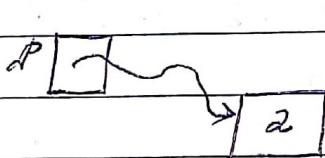
```
int *p;
p = (int *) malloc(sizeof(int));
```

typecasting

char *

scanf ("%d", p);

*p = *p + 1;



portability

int *p;

int n;

printf ("How many?");

scanf ("%d", &n);

p = (int *) malloc(sizeof(int) * n);

p[0] = 50;

Linked List -

It is a linked representation of a linear list.

e.g. (10 20 30)

We have nodes that are dynamically allocated.

A node is, a block of memory. Each such block has an address.