

$$1.1(a) \quad (h, w) = (10, 11)$$

$$k = 3$$

$$s = 2$$

$$h' = (h + 2p - f) / s + 1$$

$$= (10 - 3) / 2 + 1$$

$$= 4$$

$$w' = (11 - 3) / 2 + 1 = 5$$

$$(h', w') = (4, 5)$$

$$(b) \quad c' = F$$

$$h' = \frac{(H + 2p - D(k-1) - 1)}{s} + 1$$

$$w' = \frac{(W + 2p - D(k-1) - 1)}{s} + 1$$

$$(c', h', w')$$

$$(c) \quad x \in \mathbb{R}^{5 \times 2}$$

$$w \in \mathbb{R}^{1 \times 2 \times 3} \leftarrow \text{one kernel of size '3'}$$

$$\text{output size} = \underline{5-3} + 1 = 3 = (1 \times 3)$$

$$w = \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \end{bmatrix}$$

$$x = \begin{bmatrix} x_{11} & x_{12} & x_{13} & x_{14} & x_{15} \\ x_{21} & x_{22} & x_{23} & x_{24} & x_{25} \end{bmatrix}$$

$$(i) \quad \sigma_1 = w_{11}x_{11} + w_{12}x_{12} + w_{13}x_{13} + w_{21}x_{21} + w_{22}x_{22} + w_{23}x_{23}$$

$$= \sum_{c=1}^2 \sum_{i=1}^3 w_{ci} x_{ci}$$

$$\text{or, } o_j = \sum_{c=1}^2 \sum_{i=j}^{j+2} w_{c(j-i+1)} x_{ci}$$

$$f_w(x) = \text{output} = [o_1, o_2, o_3] \in \mathbb{R}^{1 \times 3}$$

$$(ii) \quad \frac{\partial \text{output}}{\partial w} \in \mathbb{R}^{1 \times 2 \times 3}$$

$$\frac{\partial o_1}{\partial w_{ij}} = x_{ij}, \quad \frac{\partial o_2}{\partial w_{ij}} = x_{i(j+1)}, \quad \frac{\partial o_3}{\partial w_{ij}} = x_{i(j+2)}$$

$$\frac{\partial o}{\partial w} \in \mathbb{R}^{1 \times 3 \times 2 \times 3}, \quad \text{omit dim} = 1$$

$$(iii) \quad \frac{\partial o_1}{\partial x_{ij}} = w_{ij}, \quad \frac{\partial o_2}{\partial x_{ij}} = w_{i(j-1)}, \quad \frac{\partial o_3}{\partial x_{ij}} = w_{i(j-2)}$$

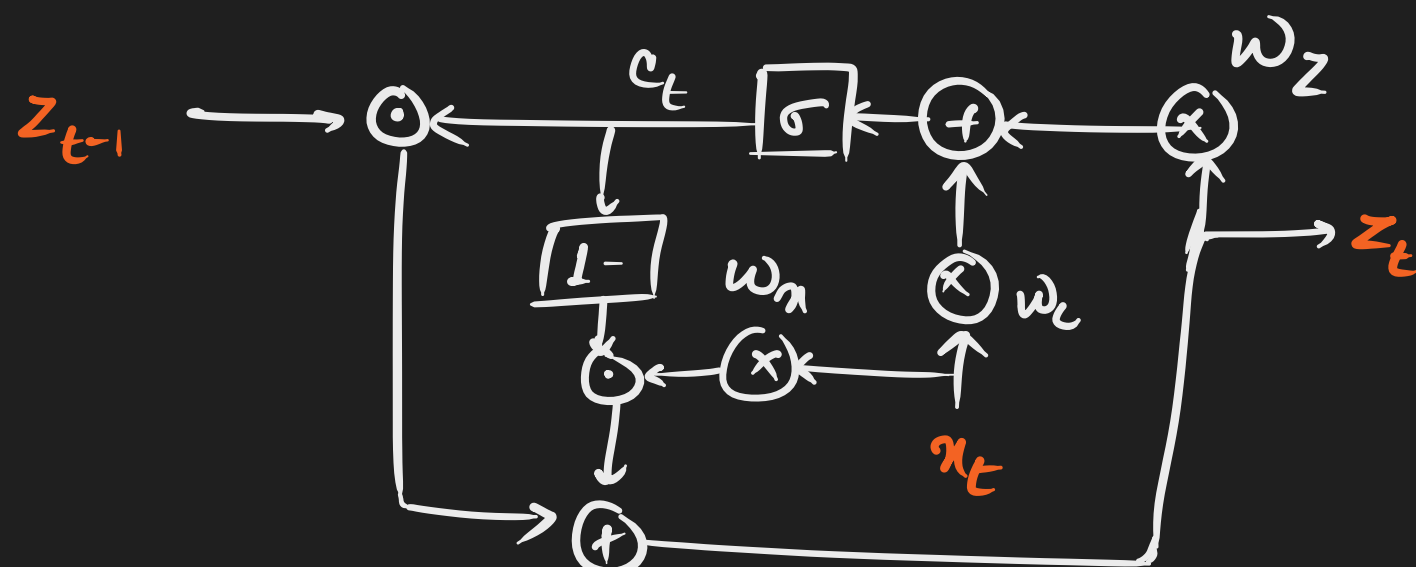
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$$\frac{\partial o}{\partial x} \in \mathbb{R}^{1 \times 3 \times 5 \times 2}, \quad \text{omit dim} = 1$$

$$(iv) \quad \frac{dl}{dw} \in \mathbb{R}^{1 \times 2 \times 3}$$

$$\frac{dl}{dw} = \frac{dl}{\underbrace{dw}_{\text{output given}}} \propto \frac{d \text{out}}{dw}$$

1.2(a)



$$(b) \quad c_t \in \mathbb{R}^m$$

$$(c) \quad \frac{dl}{dw_n} \in \mathbb{R}^{m \times n}$$

(d) Probably not.