# Data Structures and Algorithms 1 Assignment

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Question 1: Write a program that, given a list of integers, finds all 2-pairs of integers that have the same product. A 2-pair is 2 distinct pairs of integers ((a,b),(c,d)) where a X b = c X d and a  $\neq$  b  $\neq$  c  $\neq$  d. The range of integers in the list should be from 1 to 1024.

#### Statement of completion: Attempted and completed

The user has to enter how many integers he wants to input. The program validates his input and makes sure not to choose a number less than 4, because with such a small list no pairs can be found. This is an optimisation to save time from searching for pairs when they clearly can never be found. When the list is entered, the algorithm validates that input as well and makes sure that the numbers are not greater than 1024. The method pairs() uses nested for loops to find all products that match and have different factors.

#### **Testing**

prompt	Input	Expected Output	Actual Output
Ask how many numbers are to be entered	10	You can start entering your numbers	You can start entering your numbers
Ask how many numbers are to be entered	3	You need to enter more than 3 integers to find pairs	
Asked to enter numbers	2 6 7 8 4 3 16 1024 1 512	Outputs all distinct pairs and number of pairs found	Outputs all distinct pairs and number of pairs found
User enters a number larger than 1024	2666	Please enter an integer that is less than or equal to 1024	Please enter an integer that is less than or equal to 1024
User enters numbers that result in no pairs	1294	No pairs were found	No pairs were found

#### Output:

10 numbers are entered and all distinct pairs are outputted.

```
How many numbers do you want to enter?

You can start entering your numbers:

2
6
7
8
4
3
16
1024
1
512
Distinct pair of integers : ((2,6),(4,3))
Distinct pair of integers : ((2,8),(16,1))
Distinct pair of integers : ((2,4),(8,1))
Distinct pair of integers : ((2,4),(8,1))
Distinct pair of integers : ((2,3),(6,1))
Distinct pair of integers : ((2,16),(8,4))
Distinct pair of integers : ((2,1024),(4,512))
Distinct pair of integers : ((2,512),(1024,1))
Distinct pair of integers : ((6,8),(3,16))
Distinct pair of integers : ((6,4),(8,3))
Distinct pair of integers : ((6,512),(3,1024))
Distinct pair of integers : ((8,1024),(16,512))
Distinct pair of integers : ((8,512),(4,1024))
A total of distinct pairs:12
```

When the user wants to enter less than 4 numbers the program does not let him as there can never be pairs for a list which is less than 4.

```
How many numbers do you want to enter?

You need to enter more than 3 integers to be able to find pairs.
```

When the user enters a number greater than 1024, he is asked to re-enter integer until it's a valid one.

```
2666
Please enter an integer that is less than or equal to 1024
99907
Please enter an integer that is less than or equal to 1024
77
```

# When no pairs are found

```
How many numbers do you want to enter?

4
You can start entering your numbers:

2
9
6
No pairs were found
```

#### Source Code:

#### question\_1.java

```
Scanner input = new Scanner(System.in);
```

```
}
}

}

}

if (counter>0) { //if counter is greater than 0 display number of pairs found
    System.out.println("A total of distinct pairs:" + counter);

}else { //else notify the user that no pairs were found
    System.out.println("No pairs were found");
}
}
```

Question 2: Write a program that uses an ADT Stack to evaluate arithmetic expressions in RPN format. The contents of the stack should be displayed on the screen during evaluation. The allowed arithmetic operators are +, -, x, and /

#### Statement of completion: Attempted and completed

For this question the stack functions push() and pop() are used to populate or remove from top of stack. A switch case is used so that when an operator is used the program pops two times and performs the respective calculation and pushes the answer on top of stack again.

#### Output:

This is an example that uses all four operators. RPN used is: 5.5 + 2.8.3 - \*/

```
Please specify the length of you RPN (numbers and operators):

The RPN should be entered number/operator at a time (starting from the left most side of your expression)
Enter number/operator:

Push [5.0]
Enter number/operator:

Push [5.0, 5.0]
Enter number/operator:

Performing addition... [10.0]
Enter number/operator:

Push [10.0, 2.0]
Enter number/operator:

Push [10.0, 2.0, 8.0]
Enter number/operator:

Push [10.0, 2.0, 8.0]
Enter number/operator:

Push [10.0, 2.0, 8.0, 3.0]
Enter number/operator:

Performing subtraction... [10.0, 2.0, 5.0]
Enter number/operator:

Performing multiplication... [10.0, 10.0]
Enter number/operator:

Performing division... [1.0]
Result is: 1.0
```

#### Source Code

#### question\_2.java

```
public static void main(String[] args) {
```

Question 3: Write a Boolean function that checks if a number is prime. Also implement the Sieve of Eratosthenes algorithm. Explain any optimizations made.

#### Statement of completion: Attempted and completed

The program has two functions, one for the prime numbers and the other for the sieve of Eratosthenes. As an optimisation in finding whether it is prime or not, the square root of the entered number is found so that the program will search from 2 up to the square root. Then it checks if entered number is divisible by two, and if it is not, the algorithm searches only through the odd numbers.

#### **Testing**

prompt	Input	Expected Output	Actual Output		
	Check if prime number				
Enter a number	19	19.0 is a prime	19.0 is a prime		
Enter a number	200	200.0 is not a prime	200.0 is not a prime		
		number.	number.		
Sieve of Eratosthenes					
The limit is asked to	30	2 3 5 7 11 13 17 19 23	2 3 5 7 11 13 17 19 23		
be entered		29	29		

#### Output:

Case 1: Prime number is entered

```
Enter a number:
19
19.0 is a prime number.
```

Case 2: A number that is not prime is entered

```
Enter a number:
200
200.0 is not a prime number.
```

Sieve of Eratosthenes

```
Enter the limit up until the Sieve of Eratosthenes is to be computed (enter an integer):

2
3
5
7
11
13
17
19
23
29
```

#### Source Code

#### Question\_3.java

```
.mport java.util.*
   private static boolean prime(double num)
```

```
one and break the loop
```

Question 4: Write a program that accepts an input a sequence of integers (one by one) and then incrementally builds a Binary Search Tree (BST). There is no need to balance the BST.

Statement of completion: Not attempted

<u>Question 5:</u> Write a program that finds an approximation to the square root of a given number n using an iterative numerical method such as the Newton Raphson Method

<u>Statement of completion</u>: Attempted and completed. The program works on integers only and no decimal numbers.

To calculate the square root the Babylonian method was implemented. An initial guess is made, a formula is then applied to get a more accurate guess. The new estimation and previous estimation are compared and this algorithm keeps on looping until both estimations match up to 4 decimal places.

# **Testing:**

prompt	Input	Expected Output	Actual Output
Enter a number to	144	Square root of 144 is:	Square root of 144.0 is:
apply square root on		12	12.0
Enter a number to	8	Square root of 8 is:	Square root of 8 is:
apply square root on		2.8284	2.8284

### Output:

Case 1: A square number is entered

```
Enter a number to apply square root on:
144
Square root of 144.0 is: 12.0
```

#### Case 2: A number which isn't a perfect square number

```
Enter a number to apply square root on:

Square root of 8.0 is: 2.8284
```

#### Source Code

question\_5.java

<u>Question 6:</u> Write a program that, given an array of integers, finds all integers in the array that are repeated more than once. Try to find the fastest and most memory-efficient way of doing this.

# Statement of completion: Attempted and completed

At first, I implemented a different algorithm where each number stored in the array referenced a different index of the array. If two numbers referenced the same index, it implied that that number is repeated. But this algorithm worked only on numbers that are less than the length of the list. Therefore, I chose the algorithm shown below so that the program works on all numbers.

# **Testing:**

prompt	Input	Expected Output	Actual Output
Enter amount of	8	Prompt the user 8	It Prompts the user 8
numbers to be		times to input a	times to input a
entered		number	number
All 8 numbers	1 55 999 28 55 6 999 1	The repeated integers	The repeated integers
entered with		are: 1 55 999	are: 1 55 999
duplicates in the list			
All 8 numbers are	7 11 11 11 8 9 9 6	Checking for repeated	Checking for repeated
entered and		integers	integers
numbers are		Repeated: 11	Repeated: 11
repeated more than		Repeated: 11	Repeated: 11
twice		Repeated:9	Repeated:9
None of the entered	123	Checking for repeated	Checking for repeated
integers are		integers	integers
repeated		There are no repeated	There are no repeated
		integers	integers

# Output:

# Case 1: Duplicates

```
Please enter the amount of numbers to be entered:

You can start inputting the integers
Enter:

Enter:

Enter:

99
Enter:

28
Enter:

6
Enter:

6
Enter:

1
Checking for repeated integers...
repeated:
1
repeated:
55
repeated:
999
```

Case 2: Repeated more than twice. Here the program does not print the repeated more than twice integers, once.

```
Please enter the amount of numbers to be entered:

7
You can start inputting the integers
Enter:

11
Enter:
12
Enter:
13
Enter:
15
Enter:
16
Checking for repeated integers...
repeated:
11
repeated:
11
```

If there are no repeated integers the user is notified.

```
Please enter the amount of numbers to be entered:

You can start inputting the integers
Enter:

Enter:

Enter:

Checking for repeated integers...
There are no repeated integers.
```

#### Source code

question\_6.java

Question 7: Write a recursive function that finds the largest number in a given list of integers.

Statement of completion: Attempted and completed.

# **Testing:**

prompt	Input	Expected Output	Actual Output
Enter amount of	9	Prompt the user 9times	It Prompts the user 9
numbers to be		to input a number	times to input a
entered			number
All 9 numbers	700 5 1 88 9 1000 8 50	The maximum number	The maximum number
entered with	10	in your list is: 1000	in your list is: 1000
duplicates in the list			

# Output:

```
How many numbers do you want to enter?

9
You can start entering your numbers:
Enter number:
700
Enter number:
5
Enter number:
1
Enter number:
9
Enter number:
9
Enter number:
1000
Enter number:
50
Enter number:
10
The maximum number in your list is: 1000
```

#### Source code

#### question\_7.java

```
.mport java.util.*;
```

Question 8: Write a function that computes cosine or sine by taking the first n terms of the appropriate series expansion.

Statement of completion: Attempted and completed.

In this question the Maclaurin Series expansions of sine and cosine were implemented. The user can choose which one he wants to use at the beginning of the program and after one of them is calculated.

# Testing:

prompt	Input	Expected Output	Actual Output
Choose between	1	Prompt the user to	Enter a number to
sine or cosine or		enter the number to	calculate the sine of:
exit		calculate the sine of	
Enter a number to	3.14	Prompt the user to	Enter a number that
calculate the sine		enter a limit of the	represent the first n
of:		series	terms:
Asked to enter limit	6	sin(3.14) result	The answer for sine of
of series			3.14 is:
			0.0026434192764328446
Choose between	2	Prompt the user to	Enter a number to
sine or cosine or		enter the number to	calculate the cosine of:
exit		calculate the cosine of	
Enter a number to	3.14	Prompt the user to	Enter a number that
calculate the cosine		enter a limit of the	represent the first n
of:		series	terms:
Asked to enter limit	6	cos(3.14) result	The answer for cosine of
of series			3.14 is: -
			0.9998989681026615
Choose between	3	Terminate program	Exiting
sine or cosine or			Program terminates
exit			

# Output:

Sine is chosen and sin(3.14) is calculated according to the series limit specified during execution

```
----Menu----

1. Sine
2. Cosine
3.Exit

1
Enter a number to calculate the sine of:
3.14
Enter a number that represent the first n terms:
6
The answer for sine of 3.14 is: 0.0026434192764328446
----Menu---
1. Sine
2. Cosine
3.Exit
```

Cosine is chosen and cos(3.14) is calculated according to the series limit specified during execution

```
----Menu----

1. Sine

2. Cosine

3.Exit

2

Enter a number to calculate the cosine of:

3.16

Enter a number that represent the first n terms:

6

The answer for cosine of 3.14 is: -0.9998989681026615
-----Menu----

1. Sine

2. Cosine

3.Exit
```

#### Exit is chosen

```
----Menu----

1. Sine

2. Cosine

3.Exit

3
Exiting...
```

#### Source Code:

question\_8.java

```
double power2 = Math.pow(x, (double)times);
double div = power2 / (double)factorial;
double cosine = power1 * div;
```

```
System.out.println("The answer for cosine of " + x + " is: " + answer);
}

public static void sine() {
    double answer = 0.00;
    Scanner input = new Scanner(System.in);
    System.out.println("Enter a number to calculate the sine of: ");
    double x = input.nextDouble();
    System.out.println("Enter a number that represent the first n terms: ");
    double n = (double)input.nextInt();

    //performs the maclaurin expansion calculation for sine
    for(int i = 0; (double)i <= n; ++i) {
        double power1 = Math.pow(-1.0D, (double)i);
        int times = 2 * i + 1;
        int factorial = fact(times);
        double power2 = Math.pow(x, (double)times);
        double div = power2 / (double)factorial;
        double sine = power1 * div;
        if (i == 0) {
            answer = x;
        } else {
                 answer += sine;
        }
    }

    System.out.println("The answer for sine of " + x + " is: " + answer);
}</pre>
```

Question 9: Write a function that returns the sum of the first n numbers of the Fibonacci sequence (Wikipedia).

# Statement of completion: Attempted and Completed

For this task, a for loop was used to generate a Fibonacci sequence and find the total sum between the numbers generated.

# **Testing:**

prompt	Input	Expected Output	Actual Output
Enter amount of	8	Outputs the computed	Fibonacci Sequence of
numbers to be		Fibonacci sequence up	the first 8 terms: 1 2 3
entered		to 8 terms and their	5 8 13 21
		sum	Total sum: 54

# Output:

```
Enter the number of the first n terms:

Fibonacci Sequence of the first 8 terms:

1
2
3
5
8
13
21
Total sum: 54
```

#### Source Code

question\_9.java