



Program for Fibonacci numbers

The Fibonacci numbers are the sequence.

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144,

In mathematical terms, the sequence F_n of Fibonacci numbers is defined by the recurrence relation



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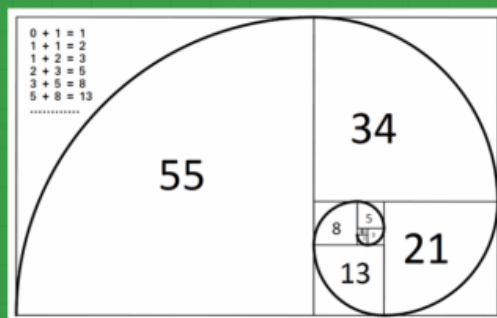
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$$F_n = F_{n-1} + F_{n-2}$$

with seed values

$$F_0 = 0 \text{ and } F_1 = 1.$$

Program for Fibonacci numbers



Given a number n , print n -th Fibonacci Number.

Examples:



Input : n = 2
Output : 1

Input : n = 9
Output : 34

Recommended: Please solve it on "PRACTICE" first, before moving on to the solution.

Write a function *int fib(int n)* that returns F_n . For example, if $n = 0$, then *fib()* should return 0. If $n = 1$, then it should return 1. For $n > 1$, it should return $F_{n-1} + F_{n-2}$

For n = 9
Output:34

Following are different methods to get the nth Fibonacci number.



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Postman

Method 1 (Use recursion)

A simple method that is a direct recursive implementation mathematical recurrence relation given above.

C++



--->

```
//Fibonacci Series using Recursion
#include<bits/stdc++.h>
using namespace std;

int fib(int n)
{
    if (n <= 1)
        return n;
    return fib(n-1) + fib(n-2);
}

int main ()
{
    int n = 9;
    cout << fib(n);
    getch();
}
```



```
    return 0;
}

// This code is contributed
// by Akanksha Rai
```

C

```
//Fibonacci Series using Recursion
#include<stdio.h>
int fib(int n)
{
    if (n <= 1)
        return n;
    return fib(n-1) + fib(n-2);
}

int main ()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}
```

Java

```
//Fibonacci Series using Recursion
class fibonacci
{
    static int fib(int n)
    {
        if (n <= 1)
            return n;
        return fib(n-1) + fib(n-2);
    }

    public static void main (String args[])
    {
        int n = 9;
        System.out.println(fib(n));
    }
}
/* This code is contributed by Rajat Mishra */
```

--->

Python

```
# Function for nth Fibonacci number

def Fibonacci(n):
    if n<0:
        print("Incorrect input")
    # First Fibonacci number is 0
    elif n==0:
        return 0
    # Second Fibonacci number is 1
```



```
elif n==1:
    return 1
else:
    return Fibonacci(n-1)+Fibonacci(n-2)
```

Driver Program

```
print(Fibonacci(9))
```

#This code is contributed by Saket Modi

C#

```
// C# program for Fibonacci Series
// using Recursion
using System;

public class GFG
{
    public static int Fib(int n)
    {
        if (n <= 1)
        {
            return n;
        }
        else
        {
            return Fib(n - 1) + Fib(n - 2);
        }
    }

    // driver code
    public static void Main(string[] args)
    {
        int n = 9;
        Console.Write(Fib(n));
    }
}

// This code is contributed by Sam007
```

PHP

```
<?php
// Fibonacci Series
// using Recursion

// function returns
// the Fibonacci number
function fib($n)
{
    if ($n <= 1)
        return $n;
    return fib($n - 1) +
           fib($n - 2);
}

// Driver Code
$n = 9;
```

```
echo fib($n);

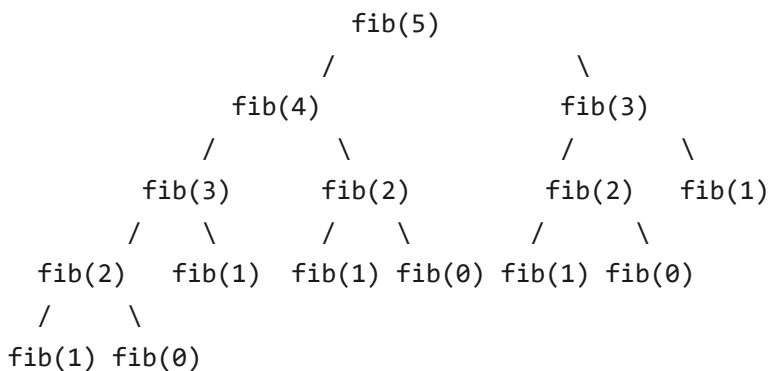
// This code is contributed by aj_36
?>
```

Output

34

Time Complexity: $T(n) = T(n-1) + T(n-2)$ which is exponential.

We can observe that this implementation does a lot of repeated work (see the following recursion tree). So this is a bad implementation for nth Fibonacci number.



Extra Space: $O(n)$ if we consider the function call stack size, otherwise $O(1)$.

Method 2 (Use Dynamic Programming)

We can avoid the repeated work done in the method 1 by storing the Fibonacci numbers calculated so far.

C

```
//Fibonacci Series using Dynamic Programming
#include<stdio.h>

int fib(int n)
{
    /* Declare an array to store Fibonacci numbers. */
    int f[n+2]; // 1 extra to handle case, n = 0
    int i;

    /* 0th and 1st number of the series are 0 and 1 */
    f[0] = 0;
    f[1] = 1;

    for (i = 2; i <= n; i++)
    {
        /* Add the previous 2 numbers in the series
           and store it */
        f[i] = f[i-1] + f[i-2];
    }

    return f[n];
}
```



```
int main ()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}
```

Java

```
// Fibonacci Series using Dynamic Programming
class fibonacci
{
    static int fib(int n)
    {
        /* Declare an array to store Fibonacci numbers. */
        int f[] = new int[n+2]; // 1 extra to handle case, n = 0
        int i;

        /* 0th and 1st number of the series are 0 and 1*/
        f[0] = 0;
        f[1] = 1;

        for (i = 2; i <= n; i++)
        {
            /* Add the previous 2 numbers in the series
            and store it */
            f[i] = f[i-1] + f[i-2];
        }

        return f[n];
    }

    public static void main (String args[])
    {
        int n = 9;
        System.out.println(fib(n));
    }
}
/* This code is contributed by Rajat Mishra */
```

Python

```
---> # Fibonacci Series using Dynamic Programming
def fibonacci(n):

    # Taking 1st two fibonacci nubers as 0 and 1
    FibArray = [0, 1]

    while len(FibArray) < n + 1:
        FibArray.append(0)

    if n <= 1:
        return n
    else:
        if FibArray[n - 1] == 0:
            FibArray[n - 1] = fibonacci(n - 1)
```

```
        if FibArray[n - 2] == 0:
            FibArray[n - 2] = fibonacci(n - 2)

    FibArray[n] = FibArray[n - 2] + FibArray[n - 1]
    return FibArray[n]

print(fibonacci(9))
```

C#

```
// C# program for Fibonacci Series
// using Dynamic Programming
using System;
class fibonacci {

static int fib(int n)
{

    // Declare an array to
    // store Fibonacci numbers.
    // 1 extra to handle
    // case, n = 0
    int []f = new int[n + 2];
    int i;

    /* 0th and 1st number of the
       series are 0 and 1 */
    f[0] = 0;
    f[1] = 1;

    for (i = 2; i <= n; i++)
    {
        /* Add the previous 2 numbers
           in the series and store it */
        f[i] = f[i - 1] + f[i - 2];
    }

    return f[n];
}

// Driver Code
public static void Main ()
{
    int n = 9;
    Console.WriteLine(fib(n));
}

}

// This code is contributed by anuj_67.
```

PHP

```
<?php
//Fibonacci Series using Dynamic
// Programming

function fib( $n)
{
```

```

/* Declare an array to store
Fibonacci numbers. */

// 1 extra to handle case,
// n = 0
$f = array();
$i;

/* 0th and 1st number of the
series are 0 and 1*/
$f[0] = 0;
$f[1] = 1;

for ($i = 2; $i <= $n; $i++)
{
    /* Add the previous 2
    numbers in the series
    and store it */
    $f[$i] = $f[$i-1] + $f[$i-2];
}

return $f[$n];
}

$n = 9;
echo fib($n);

// This code is contributed by
// anuj_67.
?>

```

Output:

34

Method 3 (Space Optimized Method 2)

We can optimize the space used in method 2 by storing the previous two numbers only because that is all we need to get the next Fibonacci number in series.

C/C++

```

// Fibonacci Series using Space Optimized Method
#include<stdio.h>
int fib(int n)
{
    int a = 0, b = 1, c, i;
    if( n == 0)
        return a;
    for (i = 2; i <= n; i++)
    {
        c = a + b;
        a = b;
        b = c;
    }
    return b;
}

```




```
int main ()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}
```

Java

```
// Java program for Fibonacci Series using Space
// Optimized Method
class fibonacci
{
    static int fib(int n)
    {
        int a = 0, b = 1, c;
        if (n == 0)
            return a;
        for (int i = 2; i <= n; i++)
        {
            c = a + b;
            a = b;
            b = c;
        }
        return b;
    }

    public static void main (String args[])
    {
        int n = 9;
        System.out.println(fib(n));
    }
}

// This code is contributed by Mihir Joshi
```

Python

```
# Function for nth fibonacci number - Space Optimisatation
# Taking 1st two fibonacci numbers as 0 and 1

def fibonacci(n):
    a = 0
    b = 1
    if n < 0:
        print("Incorrect input")
    elif n == 0:
        return a
    elif n == 1:
        return b
    else:
        for i in range(2, n+1):
            c = a + b
            a = b
            b = c
        return b

# Driver Program
```

```
print(fibonacci(9))

#This code is contributed by Saket Modi
```

C#

```
// C# program for Fibonacci Series
// using Space Optimized Method
using System;

namespace Fib
{
    public class GFG
    {
        static int Fib(int n)
        {
            int a = 0, b = 1, c = 0;

            // To return the first Fibonacci number
            if (n == 0) return a;

            for (int i = 2; i <= n; i++)
            {
                c = a + b;
                a = b;
                b = c;
            }

            return b;
        }

        // Driver function
        public static void Main(string[] args)
        {
            int n = 9;
            Console.Write("{0} ", Fib(n));
        }
    }
}

// This code is contributed by Sam007.
```

PHP

```
<?php
// PHP program for Fibonacci Series
// using Space Optimized Method

function fib( $n)
{
    $a = 0;
    $b = 1;
    $c;
    $i;
    if( $n == 0)
        return $a;
    for($i = 2; $i <= $n; $i++)
```

```

    {
        $c = $a + $b;
        $a = $b;
        $b = $c;
    }
    return $b;
}

// Driver Code
$n = 9;
echo fib($n);

// This code is contributed by anuj_67.
?>

```

Output :

34

Time Complexity: $O(n)$ **Extra Space:** $O(1)$ **Method 4 (Using power of the matrix $\begin{Bmatrix} 1 & 1 \\ 1 & 0 \end{Bmatrix}$)**

This another $O(n)$ which relies on the fact that if we n times multiply the matrix $M = \begin{Bmatrix} 1 & 1 \\ 1 & 0 \end{Bmatrix}$ to itself (in other words calculate $\text{power}(M, n)$), then we get the $(n+1)$ th Fibonacci number as the element at row and column (0, 0) in the resultant matrix.

The matrix representation gives the following closed expression for the Fibonacci numbers:

$$\begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix}^n = \begin{pmatrix} F_{n+1} & F_n \\ F_n & F_{n-1} \end{pmatrix}.$$

C

```

#include <stdio.h>

/* Helper function that multiplies 2 matrices F and M of size 2*2, and
puts the multiplication result back to F[][] */
void multiply(int F[2][2], int M[2][2]);

/* Helper function that calculates F[][] raise to the power n and puts the
result in F[][]
Note that this function is designed only for fib() and won't work as general
power function */
void power(int F[2][2], int n);

int fib(int n)
{
    int F[2][2] = {{1,1},{1,0}};
    if (n == 0)
        return 0;
    power(F, n-1);

    return F[0][0];
}

```



```

void multiply(int F[2][2], int M[2][2])
{
    int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
    int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
    int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
    int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

    F[0][0] = x;
    F[0][1] = y;
    F[1][0] = z;
    F[1][1] = w;
}

void power(int F[2][2], int n)
{
    int i;
    int M[2][2] = {{1,1},{1,0}};

    // n - 1 times multiply the matrix to {{1,0},{0,1}}
    for (i = 2; i <= n; i++)
        multiply(F, M);
}

/* Driver program to test above function */
int main()
{
    int n = 9;
    printf("%d", fib(n));
    getchar();
    return 0;
}

```

Java

```

class fibonacci
{
    static int fib(int n)
    {
        int F[][] = new int[][]{{1,1},{1,0}};
        if (n == 0)
            return 0;
        power(F, n-1);

        return F[0][0];
    }

    /* Helper function that multiplies 2 matrices F and M of size 2*2, and
    puts the multiplication result back to F[][] */
    static void multiply(int F[][], int M[][])
    {
        int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
        int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
        int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
        int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

        F[0][0] = x;
        F[0][1] = y;
        F[1][0] = z;
    }
}

```

```

F[1][1] = w;
}

/* Helper function that calculates F[][] raise to the power n and puts the
result in F[][]
Note that this function is designed only for fib() and won't work as general
power function */
static void power(int F[][], int n)
{
    int i;
    int M[][] = new int[][]{{1,1},{1,0}};

    // n - 1 times multiply the matrix to {{1,0},{0,1}}
    for (i = 2; i <= n; i++)
        multiply(F, M);
}

/* Driver program to test above function */
public static void main (String args[])
{
    int n = 9;
    System.out.println(fib(n));
}
}
/* This code is contributed by Rajat Mishra */

```

Python 3

```

# Helper function that multiplies
# 2 matrices F and M of size 2*2,
# and puts the multiplication
# result back to F[][]

# Helper function that calculates
# F[][] raise to the power n and
# puts the result in F[][]
# Note that this function is
# designed only for fib() and
# won't work as general
# power function
def fib(n):
    F = [[1, 1],
          [1, 0]]
    if (n == 0):
        return 0
    power(F, n - 1)

    return F[0][0]

def multiply(F, M):

    x = (F[0][0] * M[0][0] +
          F[0][1] * M[1][0])
    y = (F[0][0] * M[0][1] +
          F[0][1] * M[1][1])
    z = (F[1][0] * M[0][0] +
          F[1][1] * M[1][0])
    w = (F[1][0] * M[0][1] +
          F[1][1] * M[1][1])

```

```

F[0][0] = x
F[0][1] = y
F[1][0] = z
F[1][1] = w

```

```
def power(F, n):
```

```

    M = [[1, 1],
          [1, 0]]

```

```

    # n - 1 times multiply the
    # matrix to {{1,0},{0,1}}
    for i in range(2, n + 1):
        multiply(F, M)

```

```
# Driver Code
```

```

if __name__ == "__main__":
    n = 9
    print(fib(n))

```

```

# This code is contributed
# by Chitranayal

```

C#

```

// C# program to find fibonacci number.
using System;

```

```
class GFG {
```

```

    static int fib(int n)
    {
        int [,]F = new int[,] {{1, 1},
                                {1, 0} };

        if (n == 0)
            return 0;
        power(F, n-1);

        return F[0,0];
    }

```

```

/* Helper function that multiplies 2
matrices F and M of size 2*2, and puts
the multiplication result back to F[][] */
static void multiply(int [,]F, int [,]M)
{

```

```

    int x = F[0,0]*M[0,0] + F[0,1]*M[1,0];
    int y = F[0,0]*M[0,1] + F[0,1]*M[1,1];
    int z = F[1,0]*M[0,0] + F[1,1]*M[1,0];
    int w = F[1,0]*M[0,1] + F[1,1]*M[1,1];

```

```

    F[0,0] = x;
    F[0,1] = y;
    F[1,0] = z;
    F[1,1] = w;

```

```
}
```

```

/* Helper function that calculates F[][]
raise to the power n and puts the result
in F[][] Note that this function is designed
only for fib() and won't work as general

```



```

power function */
static void power(int [,]F, int n)
{
    int i;
    int [,]M = new int[,]{ {1, 1},
                           {1, 0} };

    // n - 1 times multiply the matrix to
    // {{1,0},{0,1}}
    for (i = 2; i <= n; i++)
        multiply(F, M);
}

/* Driver program to test above function */
public static void Main ()
{
    int n = 9;
    Console.WriteLine(fib(n));
}

// This code is contributed by anuj_67.

```

PHP

```

<?php
// PHP program for above approach
function fib($n)
{
    $F = array(array(1, 1),
                array(1, 0));
    if ($n == 0)
        return 0;
    power($F, $n - 1);

    return $F[0][0];
}

function multiply(&$F, &$M)
{
    $x = $F[0][0] * $M[0][0] +
          $F[0][1] * $M[1][0];
    $y = $F[0][0] * $M[0][1] +
          $F[0][1] * $M[1][1];
    $z = $F[1][0] * $M[0][0] +
          $F[1][1] * $M[1][0];
    $w = $F[1][0] * $M[0][1] +
          $F[1][1] * $M[1][1];

    $F[0][0] = $x;
    $F[0][1] = $y;
    $F[1][0] = $z;
    $F[1][1] = $w;
}

function power(&$F, $n)
{
    $M = array(array(1, 1),
                array(1, 0));

    // n - 1 times multiply the

```

```

// matrix to {{1,0},{0,1}}
for ($i = 2; $i <= $n; $i++)
    multiply($F, $M);
}

// Driver Code
$n = 9;
echo fib($n);

// This code is contributed
// by ChitraNayal
?>

```

Time Complexity: $O(n)$

Extra Space: $O(1)$

Method 5 (Optimized Method 4)

The method 4 can be optimized to work in $O(\text{Log}n)$ time complexity. We can do recursive multiplication to get power(M, n) in the previous method (Similar to the optimization done in [this](#) post)

C

```

#include <stdio.h>

void multiply(int F[2][2], int M[2][2]);

void power(int F[2][2], int n);

/* function that returns nth Fibonacci number */
int fib(int n)
{
    int F[2][2] = {{1,1},{1,0}};
    if (n == 0)
        return 0;
    power(F, n-1);
    return F[0][0];
}

/* Optimized version of power() in method 4 */
void power(int F[2][2], int n)
{

```




```

    if( n == 0 || n == 1)
        return;
    int M[2][2] = {{1,1},{1,0}};

    power(F, n/2);
    multiply(F, F);

    if (n%2 != 0)
        multiply(F, M);
}

void multiply(int F[2][2], int M[2][2])
{
    int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
    int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
    int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
    int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

    F[0][0] = x;
    F[0][1] = y;
    F[1][0] = z;
    F[1][1] = w;
}

/* Driver program to test above function */
int main()
{
    int n = 9;
    printf("%d", fib(9));
    getchar();
    return 0;
}

```

Java

```

//Fibonacci Series using Optimized Method
class fibonacci
{
    /* function that returns nth Fibonacci number */
    static int fib(int n)
    {
        int F[][] = new int[][]{{1,1},{1,0}};
        if (n == 0)
            return 0;
        power(F, n-1);

        return F[0][0];
    }

    static void multiply(int F[][], int M[][])
    {
        int x = F[0][0]*M[0][0] + F[0][1]*M[1][0];
        int y = F[0][0]*M[0][1] + F[0][1]*M[1][1];
        int z = F[1][0]*M[0][0] + F[1][1]*M[1][0];
        int w = F[1][0]*M[0][1] + F[1][1]*M[1][1];

        F[0][0] = x;
        F[0][1] = y;
        F[1][0] = z;
        F[1][1] = w;
    }
}

```

```

/* Optimized version of power() in method 4 */
static void power(int F[][], int n)
{
    if( n == 0 || n == 1)
        return;
    int M[][] = new int[][]{{1,1},{1,0}};

    power(F, n/2);
    multiply(F, F);

    if (n%2 != 0)
        multiply(F, M);
}

/* Driver program to test above function */
public static void main (String args[])
{
    int n = 9;
    System.out.println(fib(n));
}
/* This code is contributed by Rajat Mishra */

```

Python 3

```

# Fibonacci Series using
# Optimized Method

# function that returns nth
# Fibonacci number
def fib(n):

    F = [[1, 1],
          [1, 0]]
    if (n == 0):
        return 0
    power(F, n - 1)

    return F[0][0]

def multiply(F, M):

    x = (F[0][0] * M[0][0] +
          F[0][1] * M[1][0])
    y = (F[0][0] * M[0][1] +
          F[0][1] * M[1][1])
    z = (F[1][0] * M[0][0] +
          F[1][1] * M[1][0])
    w = (F[1][0] * M[0][1] +
          F[1][1] * M[1][1])

    F[0][0] = x
    F[0][1] = y
    F[1][0] = z
    F[1][1] = w

# Optimized version of
# power() in method 4
def power(F, n):

```



```

    if( n == 0 or n == 1):
        return;
    M = [[1, 1],
         [1, 0]];

    power(F, n // 2)
    multiply(F, F)

    if (n % 2 != 0):
        multiply(F, M)

# Driver Code
if __name__ == "__main__":
    n = 9
    print(fib(n))

# This code is contributed
# by Chitranayal

```

C#

```

// Fibonacci Series using
// Optimized Method
using System;

class GFG
{
    /* function that returns
    nth Fibonacci number */
    static int fib(int n)
    {
        int[,] F = new int[,]{{1, 1},
                               {1, 0}};

        if (n == 0)
            return 0;
        power(F, n - 1);

        return F[0, 0];
    }

    static void multiply(int[,] F,
                        int[,] M)
    {
        int x = F[0, 0] * M[0, 0] +
                F[0, 1] * M[1, 0];
        int y = F[0, 0] * M[0, 1] +
                F[0, 1] * M[1, 1];
        int z = F[1, 0] * M[0, 0] +
                F[1, 1] * M[1, 0];
        int w = F[1, 0] * M[0, 1] +
                F[1, 1] * M[1, 1];

        F[0, 0] = x;
        F[0, 1] = y;
        F[1, 0] = z;
        F[1, 1] = w;
    }

    /* Optimized version of
    power() in method 4 */
    static void power(int[,] F, int n)

```

```

{
    if( n == 0 || n == 1)
        return;
    int[,] M = new int[,]{{1, 1},
                           {1, 0}};

    power(F, n / 2);
    multiply(F, F);

    if (n % 2 != 0)
        multiply(F, M);
}

// Driver Code
public static void Main ()
{
    int n = 9;
    Console.Write(fib(n));
}

// This code is contributed
// by ChitraNayal

```

Time Complexity: $O(\text{Log} n)$

Extra Space: $O(\text{Log} n)$ if we consider the function call stack size, otherwise $O(1)$.

Method 6 ($O(\text{Log } n)$ Time)

Below is one more interesting recurrence formula that can be used to find n 'th Fibonacci Number in $O(\text{Log } n)$ time.

If n is even then $k = n/2$:

$$\text{---> } F(n) = [2 * F(k-1) + F(k)] * F(k)$$

If n is odd then $k = (n + 1)/2$

$$F(n) = F(k) * F(k) + F(k-1) * F(k-1)$$

How does this formula work?

The formula can be derived from above matrix equation.

$$\begin{pmatrix} 1 & 1 \\ 1 & 0 \end{pmatrix}^n = \begin{pmatrix} F_{n+1} & F_n \\ F_n & F_{n-1} \end{pmatrix}.$$



Taking determinant on both sides, we get

$$(-1)^n = F_{n+1}F_{n-1} - F_n^2$$

Moreover, since $A^n A^m = A^{n+m}$ for any square matrix A, the following identities can be derived (they are obtained from two different coefficients of the matrix product)

$$F_m F_n + F_{m-1} F_{n-1} = F_{m+n-1}$$

By putting $n = n+1$,

$$F_m F_{n+1} + F_{m-1} F_n = F_{m+n}$$

Putting $m = n$

$$F_{2n-1} = F_n^2 + F_{n-1}^2$$

$$F_{2n} = (F_{n-1} + F_{n+1})F_n = (2F_{n-1} + F_n)F_n \text{ (Source: Wiki)}$$

To get the formula to be proved, we simply need to do following

If n is even, we can put $k = n/2$

If n is odd, we can put $k = (n+1)/2$

Below is the implementation of above idea.

C++

```

// C++ Program to find n'th fibonacci Number in
// with O(Log n) arithmetic operations
#include <bits/stdc++.h>
using namespace std;

const int MAX = 1000;

// Create an array for memoization
int f[MAX] = {0};

// Returns n'th fibonacci number using table f[]
int fib(int n)
{
    // Base cases
    if (n == 0)
        return 0;
    if (n == 1 || n == 2)
        return (f[n] = 1);

    // If fib(n) is already computed
    if (f[n])
        return f[n];

```



```

int k = (n & 1)? (n+1)/2 : n/2;

// Applying above formula [Note value n&1 is 1
// if n is odd, else 0.
f[n] = (n & 1)? (fib(k)*fib(k) + fib(k-1)*fib(k-1))
           : (2*fib(k-1) + fib(k))*fib(k);

return f[n];
}

/* Driver program to test above function */
int main()
{
    int n = 9;
    printf("%d ", fib(n));
    return 0;
}

```

Java

```

// Java Program to find n'th fibonacci
// Number with O(Log n) arithmetic operations
import java.util.*;

class GFG {

    static int MAX = 1000;
    static int f[];

    // Returns n'th fibonacci number using
    // table f[]
    public static int fib(int n)
    {
        // Base cases
        if (n == 0)
            return 0;

        if (n == 1 || n == 2)
            return (f[n] = 1);

        // If fib(n) is already computed
        if (f[n] != 0)
            return f[n];

        int k = (n & 1) == 1? (n + 1) / 2
                           : n / 2;

        // Applying above formula [Note value
        // n&1 is 1 if n is odd, else 0.
        f[n] = (n & 1) == 1? (fib(k) * fib(k) +
                           fib(k - 1) * fib(k - 1))
                           : (2 * fib(k - 1) + fib(k))
                           * fib(k);

        return f[n];
    }

    /* Driver program to test above function */
    public static void main(String[] args)
    {
        int n = 9;
    }
}

```

```

        f= new int[MAX];
        System.out.println(fib(n));
    }
}

// This code is contributed by Arnav Kr. Mandal.

```

Python

```

# Python 3 Program to find n'th fibonacci Number in
# with O(Log n) arithmetic operations
MAX = 1000

# Create an array for memoization
f = [0] * MAX

# Returns n'th fibonacci number using table f[]
def fib(n) :
    # Base cases
    if (n == 0) :
        return 0
    if (n == 1 or n == 2) :
        f[n] = 1
        return (f[n])

    # If fib(n) is already computed
    if (f[n]) :
        return f[n]

    if( n & 1) :
        k = (n + 1) // 2
    else :
        k = n // 2

    # Applying above formula [Note value n&1 is 1
    # if n is odd, else 0.
    if((n & 1) ) :
        f[n] = (fib(k) * fib(k) + fib(k-1) * fib(k-1))
    else :
        f[n] = (2*fib(k-1) + fib(k))*fib(k)

    return f[n]

# Driver code
n = 9
print(fib(n))

```

This code is contributed by Nikita Tiwari.

C#

```

// C# Program to find n'th
// fibonacci Number with
// O(Log n) arithmetic operations
using System;

class GFG

```

```

{

static int MAX = 1000;
static int[] f;

// Returns n'th fibonacci
// number using table f[]
public static int fib(int n)
{
    // Base cases
    if (n == 0)
        return 0;

    if (n == 1 || n == 2)
        return (f[n] = 1);

    // If fib(n) is already
    // computed
    if (f[n] != 0)
        return f[n];

    int k = (n & 1) == 1 ? (n + 1) / 2
                        : n / 2;

    // Applyting above formula
    // [Note value n&1 is 1 if
    // n is odd, else 0.
    f[n] = (n & 1) == 1 ? (fib(k) * fib(k) +
                        fib(k - 1) * fib(k - 1))
                        : (2 * fib(k - 1) + fib(k)) *
                        fib(k);

    return f[n];
}

// Driver Code
static void Main()
{
    int n = 9;
    f = new int[MAX];
    Console.WriteLine(fib(n));
}
}

// This code is contributed by mits

```

PHP

```

<?php
// PHP Program to find n'th
// fibonacci Number in with
// O(Log n) arithmetic operations

$MAX = 1000;

// Returns n'th fibonacci
// number using table f[]
function fib($n)
{
    global $MAX;

```



```
// Create an array for memoization
$f = array_fill(0, $MAX, NULL);

// Base cases
if ($n == 0)
    return 0;
if ($n == 1 || $n == 2)
    return ($f[$n] = 1);

// If fib(n) is already computed
if ($f[$n])
    return $f[$n];

$k = ($n & 1) ? ($n + 1) / 2 : $n / 2;

// Applying above formula
// [Note value n&1 is 1 if
// n is odd, else 0.
$f[$n] = ($n & 1) ? (fib($k) * fib($k) +
                    fib($k - 1) * fib($k - 1)) :
            (2 * fib($k - 1) + fib($k)) * fib($k);

return $f[$n];
}

// Driver Code
$n = 9;
echo fib($n);

// This code is contributed
// by Chitranayal
?>
```

Output :

34

Time complexity of this solution is $O(\log n)$ as we divide the problem to half in every recursive call.

Method 7

Another approach:(Using formula)

In this method we directly implement the formula for nth term in the fibonacci series.

$$F_n = \{[(\sqrt{5} + 1)/2]^n\} / \sqrt{5}$$

Reference: <http://www.maths.surrey.ac.uk/hosted-sites/R.Knott/Fibonacci/fibFormula.html>

--->

C++

```
// C++ Program to find n'th fibonacci Number
#include<iostream>
#include<cmath>

int fib(int n) {
    double phi = (1 + sqrt(5)) / 2;
    return round(pow(phi, n) / sqrt(5));
}

// Driver Code
```



```
int main ()
{
    int n = 9;
    std::cout << fib(n) << std::endl;
    return 0;
}
//This code is contributed by Lokesh Mohanty.
```

C

```
// C Program to find n'th fibonacci Number
#include<stdio.h>
#include<math.h>
int fib(int n) {
    double phi = (1 + sqrt(5)) / 2;
    return round(pow(phi, n) / sqrt(5));
}
int main ()
{
    int n = 9;
    printf("%d", fib(n));
    return 0;
}
```

Java

```
// Java Program to find n'th fibonacci Number
import java.util.*;

class GFG {

    static int fib(int n) {
        double phi = (1 + Math.sqrt(5)) / 2;
        return (int) Math.round(Math.pow(phi, n)
                                / Math.sqrt(5));
    }

    // Driver Code
    public static void main(String[] args) {
        int n = 9;
        System.out.println(fib(n));
    }
}
// This code is contributed by PrinciRaj1992
```

--->

C#

```
// C# Program to find n'th fibonacci Number
using System;

public class GFG
{
    static int fib(int n)
    {
        double phi = (1 + Math.Sqrt(5)) / 2;
        return (int) Math.Round(Math.Pow(phi, n)
```

```
        / Math.Sqrt(5));  
    }  
  
    // Driver code  
    public static void Main()  
    {  
        int n = 9;  
        Console.WriteLine(fib(n));  
    }  
}  
  
// This code is contributed by 29AjayKumar
```

PHP

```
<?php  
// PHP Program to find n'th  
// fibonacci Number  
  
function fib($n)  
{  
    $phi = (1 + sqrt(5)) / 2;  
    return round(pow($phi, $n) / sqrt(5));  
}  
  
// Driver Code  
$n = 9;  
echo fib($n) ;  
  
// This code is contributed by Ryuga  
?>
```

Output:

34

Time Complexity: $O(1)$

Space Complexity: $O(1)$

--->



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This method is contributed by Chirag Agarwal.

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Please write comments if you find the above codes/algorithms incorrect, or find other ways to solve the same problem.

References:

http://en.wikipedia.org/wiki/Fibonacci_number

<http://www.ics.uci.edu/~eppstein/161/960109.html>

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