02_Exercise1_MaxL

April 22, 2018

1 Assignment 02

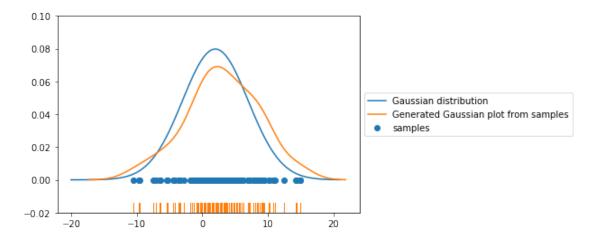
1.1 Exercise 01

```
In [8]: import numpy as np
    import matplotlib.pyplot as plt
    import scipy as sp
    import seaborn as sns
    from mpl_toolkits.mplot3d import Axes3D
    from scipy.stats import multivariate_normal
    import pandas as pd
```

Let's suppose we have a set of observations $x = (x_1, x_N)^T$, that are drawn independent and identically distributed (i.i.d) from a Gaussian distribution with unknown mean μ and variance σ^2 For this example, we are going to assume that the unknown parameters are μ =2 and σ^2 =25 and the number of samples N=100.

1.1.1 Task1:

Plot this (unknown) distribution together with the samples in the range [-20, 20].



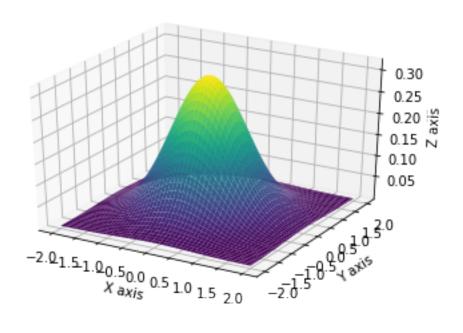
1.1.2 Task2:

- Implement the likelihood function in python (you can simply use the existing python implementations)
- Use a general optimization method to find the values for μ and σ^2 .

1.1.3 Task3:

Given: $\mu = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \Sigma = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}$ 1. Visualise a Gaussian with the given parameters. 2. Visualise a marginal Gaussian. 3. Visualise a slice of Gaussian.

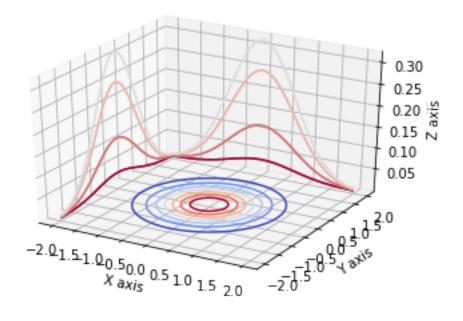
```
sigma = np.array([[0.5, 0], [0, 0.5]])
N = 100
X = np.linspace(-2, 2, N)
Y = np.linspace(-2, 2, N)
X, Y = np.meshgrid(X,Y)
pos = np.empty(X.shape + (2,))
pos[:, :, 0] = X; pos[:, :, 1] = Y
rv = multivariate_normal(mu, sigma)
\#dist = np.random.multivariate\_normal(mu, [[variance\_x, 0], [0, variance\_y]], N)
Z = rv.pdf(pos)
fig = plt.figure()
ax = fig.gca(projection='3d')
ax.plot_surface(X, Y, Z ,cmap='viridis')
ax.set_xlabel('X axis')
ax.set_ylabel('Y axis')
ax.set_zlabel('Z axis')
plt.show()
```



2 TODO

3 Visualise a marginal Gaussian.?????

```
In [7]: fig = plt.figure()
    ax = fig.gca(projection='3d')
    cset = ax.contour(X, Y, Z, zdir='z', offset=0, cmap=cm.coolwarm)
    cset = ax.contour(X, Y, Z, zdir='y', offset=2, cmap=cm.coolwarm)
    cset = ax.contour(X, Y, Z, zdir='x', offset=-2, cmap=cm.coolwarm)
    ax.set_xlabel('X axis')
    ax.set_ylabel('Y axis')
    ax.set_zlabel('Z axis')
    plt.show()
```



3.0.1 Task4:

Given:

Number of samples is 1000 from them 330 samples are labeled as class A and 670 samples are labeled as class B. There are 2 features X1 and X2. It is observed that p(A, X1)=248, p(A, X2)=82, p(B, X1)=168, p(B, X2)=502

Compute:

- Prior p(A), p(B)
- Likelihood p(X1|A), p(X1|B)
- Posterior p(A|X1)

```
In [11]: N = 1000
        N_A = 330
        N_B = 670
        P_AX1 = 0.248
        P_AX2 = 0.082
        P_BX1 = 0.168
        p_BX2 = 0.502
        P_A = N_A/N
        P_B = N_B/N
        P_X1_A = P_AX1 / P_A
        P_X1_B = P_BX1 / P_B
        P_A_X1 = P_AX1/((P_X1_A * P_A) + (P_X1_B * P_B))
        print ("Prior P(A)=",P_A,", P(B)=",P_B)
        print ("Likelihood P(X1|A)=",P_X1_A,", P(X1|B)=",P_X1_B)
        print ("Posterior P(A|X1)=",P_A_X1)
Prior P(A) = 0.33, P(B) = 0.67
Likelihood P(X1|A) = 0.751515151515151515, P(X1|B) = 0.2507462686567164
Posterior P(A|X1)= 0.5961538461538461
```