NN_DebarajBarua_091017

October 14, 2017

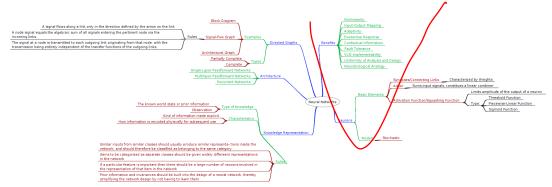
- 1 Hochschule Bonn-Rhein-Sieg
- 2 Neural Networks, WS17/18
- 3 Assignment 01 (09-October-2017)

```
In [1]: import sympy as sp
    import numpy as np
    sp.init_printing(use_latex=True)
    from IPython.display import Image
```

3.0.1 Question 2: Read chapter 1 from Haykin's book; summarize or sketch your insights in mind-map or an outline or a summary.

```
In [2]: Image("Images/MindMap.png")
Out[2]:
```

Neural Networks



Note:

Please click here (navigation possible from Jupyter Notebok) to view the mind map in higher resolution as a clickable html file.

3.0.2 Question 4: From Haykin's book, Chapter 1 problems – "Models of a neuron", solve any 2 out of 11 (1.1 to 1.11). use sympy package to solve them.

3.0.3 1.1

An example of a logistic function is defined by

$$\varphi(v) = \frac{1}{1 + e^{(-av)}}$$

whose limiting values are 0 and 1. Show that the derivative of $\varphi(v)$ with respect to v is given by

$$\frac{d\varphi}{dv} = a\varphi(v)[1 - \varphi(v)]$$

What is the value of this derivative at the origin?

derivative of logistic function is:

Out[3]:

$$\frac{ae^{-av}}{\left(1+e^{-av}\right)^2}$$

So, we see that the derivative of the function is:

$$\frac{d\varphi}{dv} = \frac{ae^{-av}}{(1 + e^{-av})^2}$$

$$= a \cdot \frac{1}{1 + e^{-av}} \cdot \frac{e^{-av}}{(1 + e^{-av})}$$

$$= a\varphi(v) \left[\frac{1 + e^{-av} - 1}{(1 + e^{-av})} \right]$$

$$= a\varphi(v) [1 - \varphi(v)]$$

At origin,
$$\varphi(0) = \frac{1}{2}$$

So, $\frac{d\varphi}{dv}\Big|_{v=0} = \frac{a}{4}$

Value of derivative of logistic function at v=0, is:

Out [4]:

 $\frac{a}{4}$

3.0.4 1.3

Yet another sigmoid function is the algebraic sigmoid:

$$\varphi(v) = \frac{v}{\sqrt{1 + v^2}}$$

whose limiting values are -1 and +1. Show that derivative of $\varphi(v)$ with respect to v is

$$\frac{d\varphi}{dv} = \frac{\varphi^3(v)}{v^3}$$

What is the value of this derivative at the origin?

derivative of algebraic sigmoid function is:

Out [5]:

$$-\frac{v^2}{(v^2+1)^{\frac{3}{2}}} + \frac{1}{\sqrt{v^2+1}}$$

So, we see that the derivative of the function is:

$$\begin{split} \frac{d\varphi}{dv} &= \frac{1}{\sqrt{v^2 + 1}} - \frac{v^2}{(v^2 + 1)^{\frac{3}{2}}} \\ &= \frac{v}{\sqrt{v^2 + 1}} \cdot \frac{1}{v} - \frac{v}{\sqrt{(v^2 + 1)}} \cdot \frac{v}{(v^2 + 1)} \\ &= \varphi \cdot \left[\frac{1}{v} - \frac{v}{1 + v^2}\right] \\ &= \varphi \cdot \left[\frac{1 + v^2 - v^2}{v(1 + v^2)}\right] \\ &= \frac{\varphi}{v} \cdot \frac{v^2}{1 + v^2} \cdot \frac{1}{v^2} \\ &= \frac{\varphi}{v^3} \cdot \varphi^2 \\ &= \frac{\varphi^3(v)}{v^3} \end{split}$$

At
$$v = 0$$
,
So, $\frac{d\varphi}{dv}\Big|_{v=0} = 1$

Value of derivative of algebraic sigmoid at v=0, is:
Out[6]:

1

3.0.5 Question 5: From Haykin's book, Chapter 1 problems – "Network architectures", solve any 2 out of 7 (1.12 to 1.19) including 1.13.

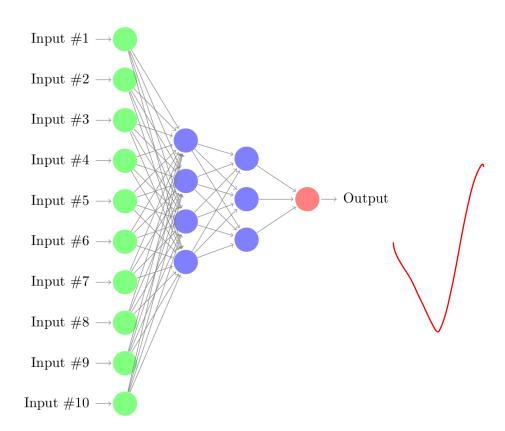
1.12

A fully connected feedforward network has 10 source nodes. 2 hidden layers, one with 4 neurons a

In [7]: Image("Images/Network.png")

Out[7]:

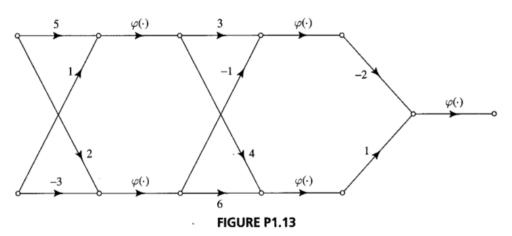
Input Hidden Hidden Output Layer Layer 1 Layer 2 Layer



(a) Figure P1.13 shows the signal-flow graph of a 2-2-2-1 feedforward network. The function $\varphi(\cdot)$ denotes a logistic function. Write the input/output mapping defined by this network.

In [8]: Image("Images/ScreenshotP113.png") #screenshot from Haykins book, Chapter 1b
Out[8]:

Chapter 1 Introduction



(b) Suppose the output neuron in the signal-flow graph for Figure P1.13 operates in the linear region. Write the linear input-output mapping defined by this new network.

3.0.6 Question 6: Solve 1.20 or 1.21 in section "Knowledge representation"