# Financial math problems solutions

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## 1 Binomial model

#### 2 Ito Integral

 $h(\cdot)$  -is a harmonic function if:

$$\sum_{i=1}^{n} \frac{\partial^2 h}{x_i^2} = 0.$$

 $h(\cdot)$  -is a subharmonic function if:

$$\sum_{i=1}^{n} \frac{\partial^2 h}{x_i^2} \ge 0.$$

Prove that for independent Wiener processes  $W_1, \ldots, W_n$  and a processes X is defined by the formula:  $X(t) = h(W_1(t), \ldots, W_n(t))$ . Show that if h is harmonic (subharmonic)  $\Rightarrow X$  is a martingale (submartingale).

#### 3 Stochastic differential equations

## 4 Black-Scholes