

Naive Bayes

Naive Bayes Algorithm (classification)

Naive Bayes is a probabilistic machine learning algorithm based on Bayes' theorem. Despite its simplicity, Naive Bayes is surprisingly effective for a wide range of classification tasks, especially when dealing with large feature spaces.

Bayes' Theorem

$$P(A/B) = \frac{P(A) \cdot P(B/A)}{P(B)}$$

$P(A/B) \rightarrow$ Prob. of A, given B has occurred

$P(B/A) \rightarrow$ Prob. of B, given A has occurred

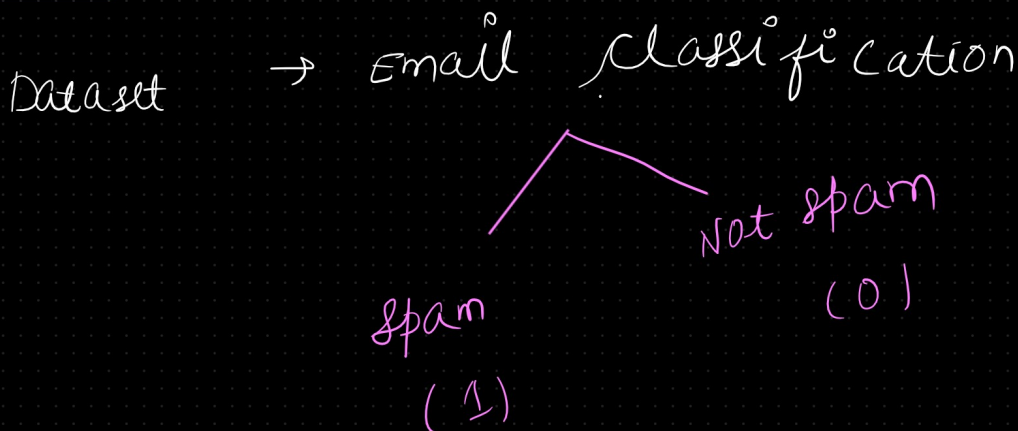
$P(A), P(B) \rightarrow$ Independent Event of A and B

→ Naive Bayes is a straightforward and efficient classification algorithm based on Bayes' theorem and the assumption of feature independence

Naive → Assumption
↳

The "Naive" in Naive Bayes comes from the assumption of feature independence. It assumes that the presence of a particular feature in a class is independent of the presence of other features.

Intuition



→ Aim: To predict whether a new email is spam or Not

Training \rightarrow

$P(\text{word} / \text{spam}) \rightarrow$ Prob. of a word occurring in spam email

$P(\text{word} / \text{not-spam}) \rightarrow$ " " " in a not spam email

Prediction

Bayes Theorem
 \downarrow

$$P(\text{spam/email}) = \frac{P(\text{spam}) \cdot P(\text{email} / \text{spam})}{P(\text{email})}$$

$$\therefore P(\text{email} / \text{spam}) = P(\text{word}_1 / \text{spam}) \times P(\text{word}_2 / \text{spam})$$

$$P(\text{not spam} / \text{email}) = \frac{P(\text{not spam}) \cdot P(\text{email} / \text{not spam})}{P(\text{email})}$$

Decision : $P(\text{spam/email}) > P(\text{not-spam/email})$

$\therefore \text{Email} \rightarrow \underline{\text{spam}}$

Key Advantages:

- Simple and easy to implement.
- Works well with high-dimensional data.
- Requires relatively few training data.

Key Limitations:

- Strong assumption of feature independence, which may not hold true in all cases.
- May not perform well if features are correlated.

x y
 $x \uparrow$ $y \uparrow$