

Merge Sort

Merge Sort is a Divide & Conquer principle based algorithm. The main idea of merge sort is to divide large data-sets into smaller sets of data, and then solve them.

Merge Sort is a recursive algorithm, it divides the given array into smaller half's and then calls itself repeatedly to solve them.

Time Complexity	$\Theta(n \log n)$
Best Case	$\Omega(n \log n)$
Worst Case	$O(n \log n)$
Space Complexity	$O(n)$

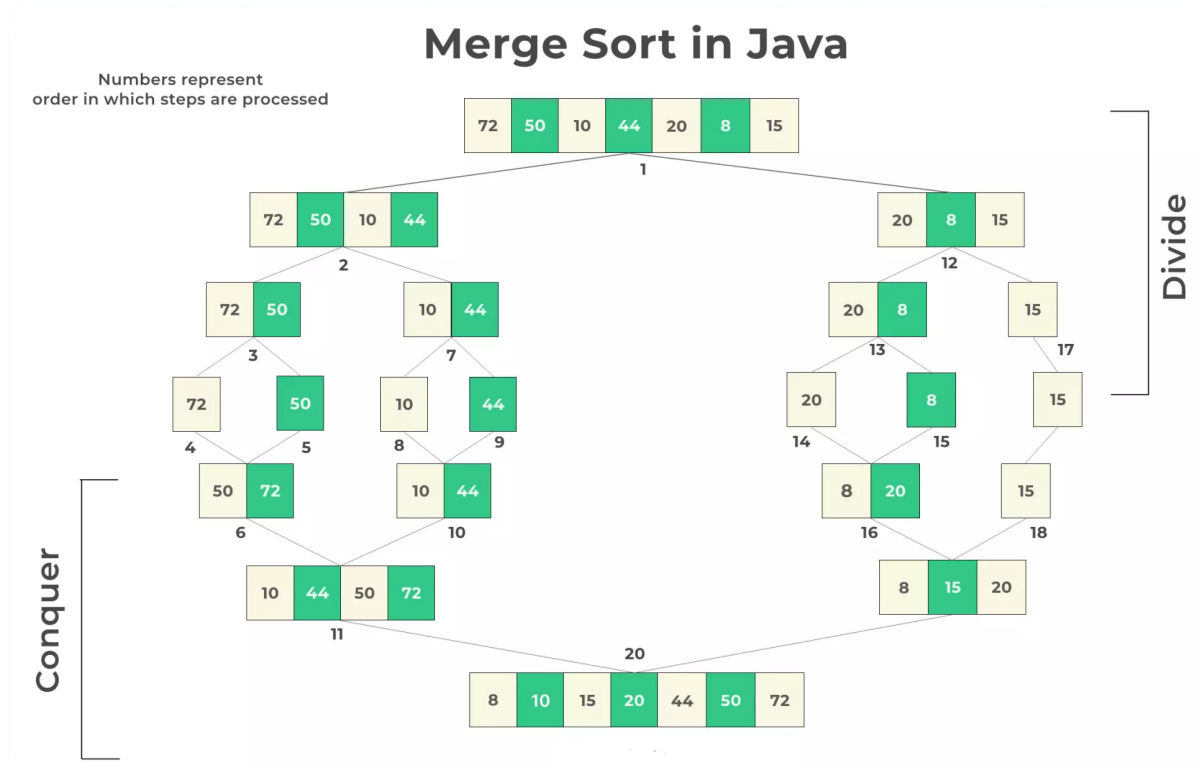
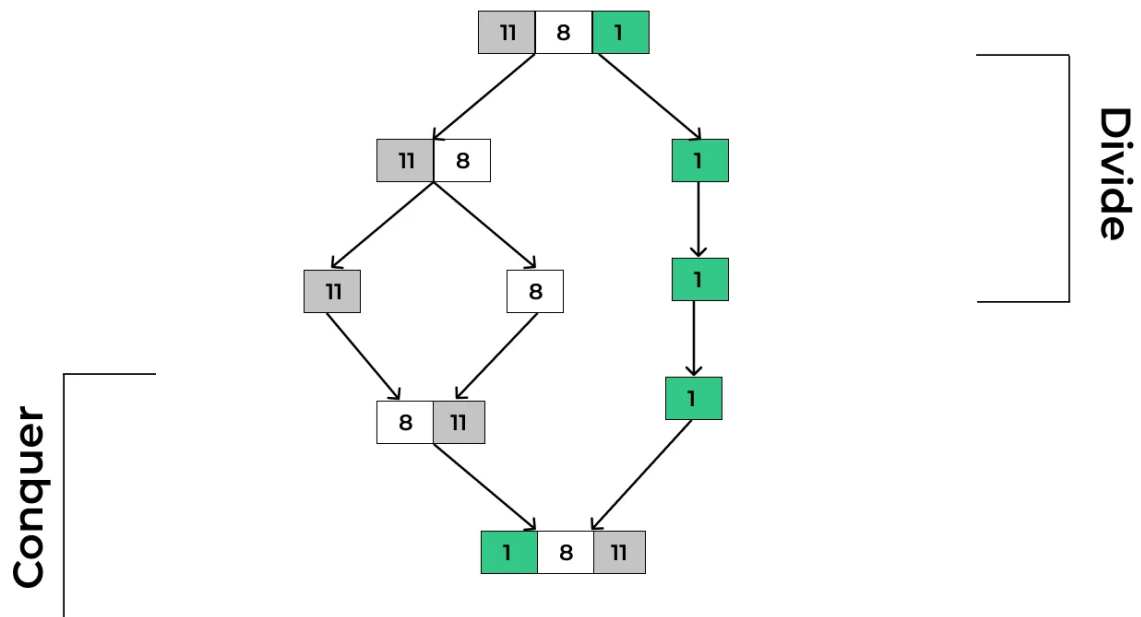
Steps for Merge Sort in Java

Divide

- The **original array** is divided into sub-arrays.
- The sub-arrays are further divided into further sub-arrays until they contain a single element using recursion.

Conquering/ Merging

- Then the sub-lists are combined together in the desired (sorted) order.
- The time complexity of the merge sort is $O(n \log n)$ for best/ worst / average cases



```
package Sort;

public class Merge1 {
```

```

public static void printArray(int[] arr, int size) {
    for (int i = 0; i < size; i++) {
        System.out.print(arr[i] + " ");
    }
    System.out.println();
}

// this function apply merging and sorting in the array
static void mergeSort(int[] a, int left, int right) {
    int mid;
    if (left < right) {
        // can also use mid = left + (right - left) / 2
        // this can avoid data type overflow
        mid = (left + right) / 2;

        // recursive calls to sort first half and second half sub-arrays
        mergeSort(a, left, mid);
        mergeSort(a, mid + 1, right);
        merge(a, left, mid, right);
    }
}

// after sorting this function merge the array
static void merge(int[] arr, int left, int mid, int right) {
    int i, j, k;
    int n1 = mid - left + 1;
    int n2 = right - mid;

    // create temp arrays to store left and right sub-arrays
    int L[] = new int[n1];
    int R[] = new int[n2];

    // Copying data to temp arrays L[] and R[]
    for (i = 0; i < n1; i++)
        L[i] = arr[left + i];

    for (j = 0; j < n2; j++)
        R[j] = arr[mid + 1 + j];

    // here we merge the temp arrays back into arr[l..r]
    i = 0; // Starting index of L[i]
    j = 0; // Starting index of R[i]
    k = left; // Starting index of merged sub-array
//10,9,7,12,78,34,33,101,23,44      L->10,9,7,101,23,44  R->12,78,34,33
    while (i < n1 && j < n2) {
        // place the smaller item at arr[k] pos
        if (L[i] <= R[j]) {
            arr[k] = L[i];
            i++;
        } else {
            arr[k] = R[j];
            j++;
        }
        k++;
    }
    // Copy the remaining elements of L[], if any
    while (i < n1) {

```

```

        arr[k] = L[i];
        i++;
        k++;
    }
    // Copy the remaining elements of R[], if any
    while (j < n2) {
        arr[k] = R[j];
        j++;
        k++;
    }
}

public static void main(String[] args) {
    int[] a = { 12, 8, 4, 14, 36, 64, 15, 72, 67, 84 };

    int size = a.length;

    System.out.println("Array Before Sort:");
    printArray(a, size);

    mergeSort(a, 0, size - 1);

    System.out.println("Array After Sort:");
    printArray(a, size);
}
}

```

```

package Sort;

public class Merge2 {
    // this function display the array
    public static void printArray(int[] arr, int size) {
        for (int i = 0; i < size; i++) {
            System.out.print(arr[i] + " ");
        }
        System.out.println();
    }

    // main function of the program
    public static void main(String[] args) {
        int[] a = { 12, 8, 4, 14, 36, 64, 15, 72, 67, 84 };

        int size = a.length;

        System.out.println("Array Before Sort:");
        printArray(a, size);

        mergeSort(a, 0, size - 1);

        System.out.println("Array After Sort:");
        printArray(a, size);
    }
}

```

```

// this function apply merging and sorting in the array
static void mergeSort(int[] a, int left, int right) {
    int mid;
    if (left < right) {
        // can also use mid = left + (right - left) / 2
        // this can avoid data type overflow
        mid = (left + right) / 2;

        // recursive calls to sort first half and second half sub-arrays
        mergeSort(a, left, mid);
        mergeSort(a, mid + 1, right);
        merge(a, left, mid, right);
    }
}

// after sorting this function merge the array
static void merge(int[] a, int left, int mid, int right) {
    int i = left; // starting index of left sub-array
    int j = mid + 1; // starting index of right sub-array
    int index = left; // used to place items in temp[]
    int[] temp = new int[10];

    while (i <= mid && j <= right) {
        // place the smaller item at temp[index]
        if (a[i] < a[j]) {
            temp[index] = a[i];
            i = i + 1;
        } else {
            temp[index] = a[j];
            j = j + 1;
        }
        index++;
    }

    // i > mid would mean all items for left
    // sub-array were successfully placed, and there
    // must be unplaced right sub-array items
    if (i > mid) {
        while (j <= right) {
            temp[index] = a[j];
            index++;
            j++;
        }
    } else {
        while (i <= mid) {
            temp[index] = a[i];
            index++;
            i++;
        }
    }
    int p = left;

    while (p < index) {
        a[p] = temp[p];
        p++;
    }
}

```

```
}
```

The space complexity is the same i.e. $O(n)$ in both cases as even though there are two subarrays in method 1 they in total have n array items and method 2 also with one single array also has n array items.

- Merge sort is quick algorithm and does sorting in only $O(n \log n)$ time
- However, it comes with a cost, which is extra space complexity which is too high in comparison to others which is $o(n)$
- While, one good thing is there that for all cases, the time complexity remains the same i.e. average, best, worst