

Are equilibration fix points global optima? Parameter-Robustness of our simple RE model

This notebook checks whether fixed points are global optima in an ensemble where the weights of the achievement function have been varied randomly

```
In[183]:= SetDirectory[$HomeDirectory];
If[! MemberQ[$Path, #], AppendTo[$Path, #] &[
  FileNameJoin[{"git", "DialecticalStructures"}]]];
If[! MemberQ[$Path, #], AppendTo[$Path, #] &[
  FileNameJoin[{"git", "ReflectiveEquilibrium"}]]];
<< DialecticalStructures`BasicTDS`;
<< DialecticalStructures`InductiveReasoning`;
<< DialecticalStructures`CoherenceMeasures`;
<< DialecticalStructures`PositionsAnalytics`;
<< ReflectiveEquilibrium`ReflectiveEquilibrium`;
```

In[*]:=

Setting up the scene

```
In[*]:= ensembleDir = "2020_06_25-0001";
```

Get data from first case.

```
In[*]:= data = Get[FileNameJoin[{
  NotebookDirectory[],
  "results",
  ensembleDir,
  ensembleDir <> "#" <> IntegerString[1, 10, 6] <> ".m"
}]];
senIDs = Cases[data, {"senIDs", _}][[1, 2]];
tau = Cases[data, {"tau", _}][[1, 2]];
param = Cases[data, {"parameters", _}][[1, 2]];
Get initial commitments for all cases.
```

```

In[ ]:= initialComs = Module[{
  n
},
  n = Length[FileNames[ensembleDir <> "*.m", FileNameJoin[{
    NotebookDirectory[],
    "results",
    ensembleDir}]]];
  Table[
    Lookup[
      Cases[
        Get[FileNameJoin[{
          NotebookDirectory[],
          "results",
          ensembleDir,
          ensembleDir <> "#" <> IntegerString[i, 10, 6] <> ".m"
        }]],
        {"posEvolution", _}][[1, 2, 1]],
      "COM"],
    {i, n}
  ]
]

```

```
Out[ ]:= {1090, 121, 118, 1333, 121, 121, 121, 1090, 1333, 1333, 118, 1090, 118, 1333, 118,
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```

Calculate sigma.

```
In[ ]:= PrintTemporary["Creating sigma..."];
sigma = Lookup[
  param,
  "sigma",
  Sigma[tau, True, senIDs]
];
PrintTemporary["...done."];
```

Calculate nPrinciples.

```
In[ ]:= PrintTemporary["Creating nPrinciples..."];
nPrinciples = Lookup[
  param,
  "nPrinciples",
  NPrinciples[sigma, senIDs]
];
PrintTemporary["...done."];
Calculate closedPosition.
```

```
In[ ]:= PrintTemporary["Creating closedPositions..."];
closedPositions =
  DeleteCases[DialecticallyClosedPositions[tau, True, senIDs], 1];
PrintTemporary["...done."];
```

We say that **P** is the set of all permissible theory-commitment pairs $\langle T, C \rangle$, where such a pair is permissible iff C is minimally consistent and T is consistent and closed. (Claus is right in saying that we've defined the notions of theory and commitments such that $\langle T, C \rangle$ -pairs are permissible.) Furthermore, let **T** be the set of all consistent and closed theories, and **C** be the set of all minimally consistent commitments. **C** is the list `Range[3^7]` (integer-representation of partial positions). **T** is a subset of **C**. **P** is hence a list of integer-pairs.

```
In[ ]:= allTCPairs = Tuples[{closedPositions, Range[3 ^ Length[senIDs]]}];
```

We further calculate

- for every T in **T**: `Simplicity[T]` and store the results in SparseArray **Simp**. (`Simplicity[T]` is stored in **Simp** at position T .)

```
In[ ]:= Simp =
  SparseArray[# -> Simplicity[#, nPrinciples[[#]], senIDs] & /@ closedPositions];
```

- for every C in **C** and for every C'_0 in `initialComs`: `Closeness[C, C'_0]` and store the results in SparseArray **Clos**[[*i*]]. (`Closeness[C, C'_0]` is stored in **Clos**[[*i*]] at position C .)

```
In[ ]:= Clos = Map[
  Function[
    initialCom,
    SparseArray[# -> Closeness[#, initialCom, senIDs, KeyTake[param,
      {"ConflictPenalty", "ContractionPenalty", "ExpansionPenalty"}]] &
      /@ Range[3 ^ Length[senIDs]]
  ],
  initialComs
];
```

- for every $\langle T, C \rangle$ in **P**: `Account[T, C]` and store the results in SparseArray **Acco**. (`Account[T, C]` is stored in **Acco** at position $\{T, C\}$.)

```
In[ ]:= Account = AccountFunction[param];
```

```

In[ ]:= Acco = Monitor[
  SparseArray[
    Flatten[Table[
      {closedPositions[[i]], c} →
        Account[c, closedPositions[[i]], sigma, senIDs],
      {i, Length[closedPositions]}, {c, 3^Length[senIDs]}
    ],
    1
  ],
  ProgressIndicator[i, {1, Length[closedPositions]}]
];

```

Evaluating fixed points

```

In[ ]:= WeightAccount[alpha_, beta_] :=  $\frac{\alpha * \beta}{\alpha + \beta - \alpha * \beta}$ ;
WeightSystematicity[alpha_, beta_] :=  $\frac{\beta - \alpha * \beta}{\alpha + \beta - \alpha * \beta}$ ;
WeightCloseness[alpha_, beta_] :=
  1 - (WeightAccount[alpha, beta] + WeightSystematicity[alpha, beta]);

In[ ]:= {WeightAccount[#1, #2], WeightSystematicity[#1, #2], WeightCloseness[#1, #2]} &[
  0.35, 0.75]
Out[ ]:= {0.313433, 0.58209, 0.104478}

In[ ]:= {WeightAccount[#1, #2], WeightSystematicity[#1, #2], WeightCloseness[#1, #2]} &[
  0.4, 0.8]
Out[ ]:= {0.363636, 0.545455, 0.0909091}

In[ ]:= {WeightAccount[#1, #2], WeightSystematicity[#1, #2], WeightCloseness[#1, #2]} &[
  0.45, 0.85]
Out[ ]:= {0.416894, 0.509537, 0.0735695}

In[ ]:=
AchievementFunction[tcp_, alpha_, beta_, caseindex_] := Module[{wa, ws, wc},
  (*Calculate weights*)
  wa = WeightAccount[alpha, beta];
  ws = WeightSystematicity[alpha, beta];
  wc = WeightCloseness[alpha, beta];
  (*Calculate achievement value*)
  ws * Simp[[First[tcp]]] +
  wc * Clos[[caseindex, Last[tcp]]] + wa * Acco[[First[tcp], Last[tcp]]]
];

```

```
In[ ]:= (* TEST *)
```

```
AchievementFunction[
  {closedPositions[[4]], 68},
  0.8, 0.4,
  3
]
```

```
Out[ ]:= 0.888683
```

```
In[ ]:= diagnostics = Module[{
  casedata, initialCom, finalstate, n, allAchievementValues, alpha, beta
},
  n = Length[FileNames[ensembleDir <> "#*.m", FileNameJoin[{
    NotebookDirectory[],
    "results",
    ensembleDir}]]];
  Table[
    (
      PrintTemporary["Analysing ensemble-member " <> ToString[i]];
      casedata = Get[FileNameJoin[{
        NotebookDirectory[],
        "results",
        ensembleDir,
        ensembleDir <> "#" <> IntegerString[i, 10, 6] <> ".m"
      }]];

      initialCom = Lookup[
        Cases[casedata, {"posEvolution", _}][[1, 2, 1]],
        "COM"];
      PrintTemporary["  initial commitments: " <> ToString[initialCom]];

      finalstate = Lookup[
        Cases[casedata, {"posEvolution", _}][[1, 2, -1]],
        {"THE", "COM"}];

      alpha = Lookup[
        Cases[casedata, {"parameters", _}][[1, 2]],
        "alpha"];
      PrintTemporary["  alpha: " <> ToString[alpha]];

      beta = Lookup[
        Cases[casedata, {"parameters", _}][[1, 2]],
        "beta"];
      PrintTemporary["  beta: " <> ToString[beta]];

      allAchievementValues =
        (AchievementFunction[#, alpha, beta, i] &) /@ allTCPairs;
      (*Return as entry i in diagnostics:*)
    )
  ];
```

```

    {
      i,
      First[finalstate] == Last[finalstate],
      Max[allAchievementValues] -
        AchievementFunction[finalstate, alpha, beta, i]
    }
  ),
  {i, n}
]
];

```

In[]:= **diagnostics**

```

Out[ ]:= { {1, False, 0.}, {2, False, 0.}, {3, True, 0.}, {4, True, 0.}, {5, True, 0.},
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```

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{470, False, 0.}, {471, True, 0.}, {472, True, 0.}, {473, True, 0.},
{474, True, 0.}, {475, True, 0.}, {476, False, 0.}, {477, False, 0.},
{478, False, 0.}, {479, False, 0.}, {480, True, 0.}, {481, True, 0.},
{482, False, 0.}, {483, False, 0.}, {484, False, 0.}, {485, False, 0.0016429},
{486, True, 0.}, {487, True, 0.}, {488, True, 0.}, {489, False, 0.},
{490, True, 0.0033136}, {491, False, 0.}, {492, True, 0.00272551},
{493, True, 0.}, {494, True, 0.}, {495, False, 0.}, {496, True, 0.},
{497, False, 0.}, {498, False, 0.}, {499, False, 0.}, {500, False, 0.}}

```

Analyse diagnostics

How many final states are global optima (absolute, ratio)?

```
In[*]:= Count[diagnostics, e_ /; (e[[3]] == 0)]
```

```
Out[*]:= 439
```

```
In[*]:= N[Count[diagnostics, e_ /; (e[[3]] == 0)] / Length@diagnostics]
```

```
Out[*]:= 0.878
```

How many final states are full RE states (absolute, ratio)?

```
In[*]:= Count[diagnostics, e_ /; (e[[3]] == 0) && e[[2]]]
```

```
Out[*]:= 289
```

```
In[*]:= N[Count[diagnostics, e_ /; (e[[3]] == 0) && e[[2]]] / Length@diagnostics]
```

```
Out[*]:= 0.578
```

How many of the global optima are full RE states?

```
In[*]:= N[Count[diagnostics, e_ /; (e[[3]] == 0) && e[[2]]] /  
Count[diagnostics, e_ /; (e[[3]] == 0)]]
```

```
Out[*]:= 0.658314
```

Alpha/beta values that yield fixed points that are no optima

In[]:=

```
(
  Lookup[
    Cases[
      Get[FileNameJoin[{
        NotebookDirectory[],
        "results",
        ensembleDir,
        ensembleDir <> "#" <> IntegerString[#, 10, 6] <> ".m"
      }]],
      {"parameters", _}][[1, 2]],
      {"alpha", "beta"}] &
    ) /@ Cases[diagnostics, e_ /; (e[[3]] != 0)][[All, 1]]
```

```
Out[ ]:= { {0.611781, 0.90668}, {0.599839, 0.657184},
  {0.845875, 0.901509}, {0.814728, 0.954657},
  {0.925996, 0.025199}, {0.552157, 0.591515}, {0.908832, 0.883413},
  {0.930125, 0.557585}, {0.952517, 0.790852}, {0.54865, 0.934608},
  {0.901092, 0.889485}, {0.547763, 0.943285}, {0.744138, 0.989753},
  {0.977511, 0.587197}, {0.887016, 0.107306}, {0.645537, 0.82728},
  {0.52994, 0.859647}, {0.965531, 0.458517}, {0.9286, 0.898796},
  {0.6873, 0.829992}, {0.970634, 0.975537}, {0.586447, 0.614009},
  {0.643676, 0.881376}, {0.650105, 0.825179}, {0.896564, 0.157768},
  {0.994953, 0.170713}, {0.271374, 0.27144}, {0.894058, 0.473949},
  {0.976909, 0.957823}, {0.901346, 0.92391}, {0.981345, 0.989705},
  {0.773179, 0.81341}, {0.66264, 0.886034}, {0.924561, 0.113834},
  {0.982164, 0.152807}, {0.911913, 0.767892}, {0.986336, 0.58619},
  {0.512376, 0.622323}, {0.59321, 0.910963}, {0.901356, 0.588891},
  {0.907153, 0.969344}, {0.566474, 0.628257}, {0.900117, 0.434084},
  {0.584062, 0.702414}, {0.804093, 0.994052}, {0.687529, 0.716555},
  {0.925757, 0.111858}, {0.972607, 0.084451}, {0.707279, 0.732825},
  {0.898266, 0.140121}, {0.87715, 0.797582}, {0.62264, 0.638556},
  {0.766055, 0.855051}, {0.806607, 0.98144}, {0.947817, 0.607373},
  {0.901829, 0.295271}, {0.873147, 0.136451}, {0.893524, 0.943434},
  {0.985078, 0.436679}, {0.597048, 0.886979}, {0.737011, 0.865849} }
```