

1. (d)

$$\begin{aligned} \frac{dJ}{d\theta} &= -\left(\frac{1}{n}\right) \sum_i \left\{ y^i \left(\frac{1}{\sigma(z)} \right) \cdot \sigma(z) \cdot (1 - \sigma(z)) (x^i)^T \right. \\ &\quad \left. - (1 - y^i) \left(\frac{1}{1 - \sigma(z)} \right) (-\sigma(z)) (1 - \sigma(z)) (x^i)^T \right\} \\ &= -\left(\frac{1}{n}\right) \sum_i \left\{ y^i (1 - \sigma(z)) (x^i)^T - (1 - y^i) \sigma(z) (x^i)^T \right\} \\ &= -\left(\frac{1}{n}\right) \sum_i (y^i - \sigma(z)) (x^i)^T \\ \text{where } z &= \theta (x^i)^T \end{aligned}$$