Correct

and then summing all these together.

Yes, each activation of the output volume is computed by multiplying the parameters from only one filter with a volumic slice of the input volume