Examples

Math. in confi

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Colofon

This document shows a few formulas coded in MATHML and typeset by CONT_EXT. The examples are taken from an old copy of 'Handbook of Chemistry and Physics' as well as 'Wiskunde voor het HBO (R. van Asselt et al.)'. We assume no responsibility for the coding being 100% all correct.

These examples are typeset using the default settings. There are several ways to influence the look and feel of a formula. Details on how to process MATHML can be found in the XML related documentation that comes with ConTeXt.

You can get more information on $ConT_EXT$ at our website, in T_EX usergroup publications and in (the archives of) the $ConT_EXT$ mailing list.

Hans Hagen Hasselt, January 2001 / June 2008 www.pragma-ade.com

Derivatives

pc-d-001	pc-d-004	pc-d-007	pc-d-010	pc-d-051
pc-d-002	pc-d-005	pc-d-008	pc-d-011	
pc-d-003	pc-d-006	pc-d-009	pc-d-043	

```
\frac{\mathrm{d}a}{\mathrm{d}x} = 0
```

```
\frac{\mathrm{d}x}{\mathrm{d}x} = 1
```

```
\frac{\mathrm{d}au}{\mathrm{d}x} = a\frac{\mathrm{d}u}{\mathrm{d}x}
```

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
    <apply> <times/>
      <ci> a </ci>
      <ci> u </ci>
    </apply>
   </apply>
   <apply> <times/>
    <ci> a </ci>
    <apply> <diff/>
      <ci> u </ci>
    </apply>
   </apply>
 </apply>
```

$$\frac{\mathrm{d}u + v + w}{\mathrm{d}x} = \frac{\mathrm{d}u}{\mathrm{d}x} + \frac{\mathrm{d}v}{\mathrm{d}x} + \frac{\mathrm{d}u}{\mathrm{d}x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
  <apply> <diff/>
    <apply> <plus/>
     <ci> u </ci>
     <ci> v </ci>
     <ci> w </ci>
    </apply>
  </apply>
  <apply> <plus/>
    <apply> <diff/>
     <ci> u </ci>
    </apply>
    <apply> <diff/>
     <ci> v </ci>
    </apply>
    <apply> <diff/>
     <ci> w </ci>
    </apply>
  </apply>
 </apply>
```

$$\frac{\mathrm{d}u\,v}{\mathrm{d}x} = u\,\frac{\mathrm{d}u}{\mathrm{d}x} + v\,\frac{\mathrm{d}v}{\mathrm{d}x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
    <apply> <times/>
      <ci> u </ci>
      <ci> v </ci>
    </apply>
   </apply>
   <apply> <plus/>
    <apply> <times/>
      <ci> u </ci>
      <apply> <diff/>
       </br>
      </apply>
    </apply>
    <apply> <times/>
      <ci> v </ci>
      <apply> <diff/>
       </br>
      </apply>
    </apply>
   </apply>
 </apply>
```

$\frac{\mathrm{d}uvw}{\mathrm{d}x} = uv\frac{\mathrm{d}w}{\mathrm{d}x} + vw\frac{\mathrm{d}u}{\mathrm{d}x} + uw\frac{\mathrm{d}v}{\mathrm{d}x}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'> </apply>
         <apply> <eq/>
                                                                                                                                                                                                                                                 <apply> <diff/>
                          <apply> <times/>
                                  <ci> u </ci>
                                  <ci> v </ci>
                                  <ci> w </ci>
                          </apply>
                  </apply>
                  <apply> <plus/>
                          <apply> <times/>
                                   <ci> u </ci>
                                       <ci> v </ci>
                                  <apply> <diff/>
                                            <br/>

                                            <ci> w </ci>
                                   </apply>
                          </apply>
                          <apply> <times/>
                                   <ci> v </ci>
                                  <ci> w </ci>
                                  <apply> <diff/>
                                           <ci> u </ci>
                                   </apply>
                          </apply>
                          <apply> <times/>
                                  <ci> u </ci>
                                  <ci> w </ci>
                                  <apply> <diff/>
                                            <ci> v </ci>
                                  </apply>
                          </apply>
                 </apply>
```

$$\frac{\mathrm{d}\frac{u}{v}}{\mathrm{d}x} = \frac{v\frac{\mathrm{d}u}{\mathrm{d}x} - u\frac{\mathrm{d}v}{\mathrm{d}x}}{v^2} = \frac{1}{v}\frac{\mathrm{d}u}{\mathrm{d}x} - \frac{u}{v^2}\frac{\mathrm{d}v}{\mathrm{d}x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                                                                                                                                                                                                                                                                                                                                             </apply>
           <apply> <eq/>
                                                                                                                                                                                                                                                                                                                                                                             <apply> <diff/>
                      <apply> <diff/>
                                                                                                                                                                                                                                                                                                                                                                                        <bvar> <ci> x </ci> </bvar>
                                                                                                                                                                                                                                                                                                                                                                                        <ci> u </ci>
                                 <apply> <divide/>
                                                                                                                                                                                                                                                                                                                                                                             </apply>
                                             <ci> u </ci>
                                                                                                                                                                                                                                                                                                                                                                  </apply>
                                             <ci> v </ci>
                                                                                                                                                                                                                                                                                                                                                                  <apply> <times/>
                                                                                                                                                                                                                                                                                                                                                                             <apply> <divide/>
                                 </apply>
                                                                                                                                                                                                                                                                                                                                                                                        <cn> u </cn>
                      </apply>
                      <apply> <divide/>
                                                                                                                                                                                                                                                                                                                                                                                        <apply> <power/>
                                 <apply> <minus/>
                                                                                                                                                                                                                                                                                                                                                                                                    <ci> v </ci>
                                             <apply> <times/>
                                                                                                                                                                                                                                                                                                                                                                                                    <cn> 2 </cn>
                                                         <ci> v </ci>
                                                                                                                                                                                                                                                                                                                                                                                        </apply>
                                                         <apply> <diff/>
                                                                                                                                                                                                                                                                                                                                                                             </apply>
                                                                    <br/>

                                                                                                                                                                                                                                                                                                                                                                             <apply> <diff/>
                                                                    <ci> u </ci>
                                                                                                                                                                                                                                                                                                                                                                                        <br/>

                                                         </apply>
                                                                                                                                                                                                                                                                                                                                                                                        <ci> v </ci>
                                             </apply>
                                                                                                                                                                                                                                                                                                                                                                             </apply>
                                             <apply> <times/>
                                                                                                                                                                                                                                                                                                                                                                  </apply>
                                                         <ci> u </ci>
                                                                                                                                                                                                                                                                                                                                                      </apply>
                                                         <apply> <diff/>
                                                                                                                                                                                                                                                                                                                                          </apply>
                                                                    <ci> v </ci>
                                                         </apply>
                                             </apply>
                                 </apply>
                                 <apply> <power/>
                                            <ci> v </ci>
                                             <cn> 2 </cn>
                                 </apply>
                      </apply>
                      <apply> <minus/>
                                 <apply> <times/>
                                             <apply> <divide/>
                                                         < cn> 1 </ cn>
                                                         <ci> v </ci>
```

content colofon index go back - + Derivatives: pc-d-007

$\frac{\mathrm{d}u^n}{\mathrm{d}x} = n\left(u\right)^{n-1} \frac{\mathrm{d}u}{\mathrm{d}x}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
     <apply> <power/>
      <ci> u </ci>
      <ci> n </ci>
     </apply>
   </apply>
   <apply> <times/>
    <ci> n </ci>
     <apply> <power/>
      <ci> u </ci>
      <apply> <minus/>
        <ci> n </ci>
        < cn> 1 </ cn>
      </apply>
    </apply>
     <apply> <diff/>
      <ci> u </ci>
    </apply>
   </apply>
 </apply>
```

$\frac{\mathrm{d}\sqrt{u}}{\mathrm{d}x} = \frac{1}{2\sqrt{u}} \frac{\mathrm{d}u}{\mathrm{d}x}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
     <apply> <root/>
      <ci> u </ci>
     </apply>
   </apply>
   <apply> <times/>
     <apply> <divide/>
      < cn> 1 </ cn>
      <apply> <times/>
        < cn> 2 </ cn>
        <apply> <root/>
          <ci> u </ci>
        </apply>
      </apply>
     </apply>
     <apply> <diff/>
      <ci> u </ci>
     </apply>
   </apply>
 </apply>
```

$$\frac{\mathrm{d}\frac{1}{u}}{\mathrm{d}x} = -\frac{1}{u^2} \frac{\mathrm{d}u}{\mathrm{d}x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
     <apply> <divide/>
      <cn> 1 </cn>
      <ci> u </ci>
     </apply>
   </apply>
   <apply> <times/>
     <apply> <minus/>
      <apply> <divide/>
        < cn> 1 </ cn>
        <apply> <power/>
          <ci> u </ci>
          <cn> 2 </cn>
        </apply>
      </apply>
     </apply>
     <apply> <diff/>
      <ci> u </ci>
     </apply>
   </apply>
 </apply>
```

$$\frac{\mathrm{d}\frac{1}{u^n}}{\mathrm{d}x} = -\frac{n}{(u)^{n+1}} \frac{\mathrm{d}u}{\mathrm{d}x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
     <apply> <divide/>
       <cn> 1 </cn>
       <apply> <power/>
         <ci> u </ci>
         <cn> n </cn>
       </apply>
     </apply>
   </apply>
   <apply> <times/>
     <apply> <minus/>
       <apply> <divide/>
         <ci> n </ci>
         <apply> <power/>
          <ci> u </ci>
          <apply> <plus/>
            <ci> n </ci>
            < cn > 1 < / cn >
          </apply>
         </apply>
       </apply>
     </apply>
     <apply> <diff/>
       <ci> u </ci>
     </apply>
   </apply>
 </apply>
```

$$\frac{\mathrm{d}}{\mathrm{d}x} = \frac{\mathrm{d}\log\left(u + \sqrt{u^2 + 1}\right)}{\mathrm{d}x} = \frac{1}{\sqrt{u^2 + 1}}\frac{\mathrm{d}u}{\mathrm{d}x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                                                                                                                                                                                                                                               </apply>
       <apply> <eq/>
                                                                                                                                                                                                                                                                               < cn> 1 </ cn>
                <apply> <diff/>
                                                                                                                                                                                                                                                                       </apply>
                        <bvar> <ci> x </ci> </bvar>
                                                                                                                                                                                                                                                              </apply>
                       <apply> <inverse/>
                                                                                                                                                                                                                                                       </apply>
                                <apply> <sinh/>
                                                                                                                                                                                                                                                       <apply> <diff/>
                                        <ci> u </ci>
                                                                                                                                                                                                                                                              <br/>

                                </apply>
                                                                                                                                                                                                                                                              <ci> u </ci>
                       </apply>
                                                                                                                                                                                                                                                      </apply>
                </apply>
                                                                                                                                                                                                                                              </apply>
                <apply> <diff/>
                                                                                                                                                                                                                                      </apply>
                       <apply> <log/>
                                <apply> <plus/>
                                        <ci> u </ci>
                                        <apply> <root/>
                                                <apply> <plus/>
                                                        <apply> <power/>
                                                                <ci> u </ci>
                                                                <cn> 2 </cn>
                                                        </apply>
                                                        < cn> 1 </ cn>
                                                </apply>
                                        </apply>
                                </apply>
                       </apply>
                </apply>
                <apply> <times/>
                       <apply> <divide/>
                                < cn> 1 </ cn>
                                <apply> <root/>
                                        <apply> <plus/>
                                                 <apply> <power/>
                                                        <ci> u </ci>
                                                        <cn> 2 </cn>
```

content colofon index go back - +

Derivatives: pc-d-043

$\frac{\mathrm{d}\int\limits_{p}^{q}f(x,a)\,\mathrm{d}x}{\mathrm{d}a}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <diff/>
    <apply> <int/>
      <lowlimit> <ci> p </ci> </lowlimit>
      <uplimit> <ci> q </ci> </uplimit>
      <apply>
        <fn> <ci> f </ci> </fn>
        <ci> x </ci>
        <ci> a </ci>
      </apply>
    </apply>
   </apply>
 </apply>
```

Integrals

pc-i-022

pc-i-380

$$\int \left(\frac{1}{x\sqrt{\pm a^2x^2}}\right) dx = -\frac{1}{a}\log\frac{a + \sqrt{\pm a^2x^2}}{x}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                                          <cn> 2 </cn>
 <apply> <eq/>
                                                                        </apply>
   <apply> <int/>
                                                                        <apply> <power/>
     <ci> x </ci>
     <apply> <divide/>
                                                                          <cn> 2 </cn>
       <cn> 1 </cn>
                                                                        </apply>
       <apply> <times/>
                                                                      </apply>
         <ci> x </ci>
                                                                    </apply>
         <apply> <root/>
                                                                  </apply>
                                                                  <ci> x </ci>
           <apply> <fn> <ci> &plusminus; </ci> </fn>
             <apply> <power/>
                                                                </apply>
               <ci> a </ci>
                                                              </apply>
               <cn> 2 </cn>
                                                            </apply>
             </apply>
                                                          </apply>
             <apply> <power/>
                                                        </apply>
               <ci> x </ci>
                                                      <cn> 2 </cn>
             </apply>
           </apply>
         </apply>
       </apply>
     </apply>
   </apply>
   <apply> <minus/>
     <apply> <times/>
       <apply> <divide/>
         <cn> 1 </cn> <ci> a </ci>
       </apply>
       <apply> <log/>
         <apply> <divide/>
           <apply> <plus/>
             <ci> a </ci>
             <apply> <root/>
               <apply> <fn> <ci> &plusminus; </ci> </fn>
                 <apply> <power/>
                    <ci> a </ci>
```

content colofon index go back - +

$$\int \left(\frac{1}{\cos(ax)(\pm 1\sin(ax))}\right) dx = \left(\mp \frac{1}{2a(\pm 1\sin(ax))}\right) + \frac{1}{2a}\log\tan\left(\frac{\pi}{4} + \frac{ax}{2}\right)$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                                              <ci> a </ci>
                                                                              <ci> x </ci>
  <apply> <eq/>
    <apply> <int/>
                                                                            </apply>
      <bvar> <ci> x </ci> </bvar>
                                                                          </apply>
      <apply> <divide/>
                                                                        </apply>
        < cn > 1 < / cn >
                                                                     </apply>
        <apply> <times/>
                                                                   </apply>
          <apply> <cos/>
                                                                 </apply>
            <apply> <times/>
                                                                 <apply> <times/>
               <ci> a </ci>
                                                                   <apply> <divide/>
               <ci> x </ci>
                                                                      < cn> 1 </ cn>
            </apply>
                                                                     <apply> <times/>
          </apply>
                                                                        <cn> 2 </cn>
          <apply> <fn> <ci> &plusminus; </ci> </fn>
                                                                        <ci> a </ci>
            < cn> 1 </ cn>
                                                                     </apply>
            <apply> <sin/>
                                                                   </apply>
               <apply> <times/>
                                                                   <apply> <log/>
                 <ci> a </ci>
                                                                      <apply> <tan/>
                 <ci> x </ci>
                                                                        <apply> <plus/>
               </apply>
                                                                          <apply> <divide/>
            </apply>
                                                                            <ci> &pi; </ci>
          </apply>
                                                                            <cn> 4 </cn>
        </apply>
                                                                          </apply>
      </apply>
                                                                          <apply> <divide/>
    </apply>
                                                                            <apply> <times/>
                                                                              <ci> a </ci>
    <apply> <plus/>
      <apply> <fn> <ci> &minusplus; </ci> </fn>
                                                                              <ci> x </ci>
        <apply> <divide/>
                                                                            </apply>
          < cn> 1 </ cn>
                                                                            <cn> 2 </cn>
          <apply> <times/>
                                                                          </apply>
            \langle cn \rangle 2 \langle cn \rangle
                                                                        </apply>
            <ci> a </ci>
                                                                     </apply>
            <apply> <fn> <ci> &plusminus; </ci> </fn>
                                                                   </apply>
               < cn> 1 </ cn>
                                                                 </apply>
               <apply> <sin/>
                                                               </apply>
                 <apply> <times/>
                                                             </apply>
```

content colofon index go back - +

Series

pc-s-001 pc-s-002 pc-s-003 wh-s-001 wh-s-002

$1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\tau}{4}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
    <apply> <plus/>
      <cn> 1 </cn>
      <apply> <minus/>
        <apply> <divide/>
          < cn> 1 </ cn>
          <cn> 3 </cn>
        </apply>
      </apply>
      <apply> <divide/>
        < cn> 1 </ cn>
        <cn> 5 </cn>
      </apply>
      <apply> <minus/>
        <apply> <divide/>
          <cn> 1 </cn>
          <cn> 7 </cn>
        </apply>
      </apply>
      <ci> &cdots; </ci>
    </apply>
    <apply> <divide/>
      <ci> &pi; </ci>
      <cn> 4 </cn>
    </apply>
</apply>
```

$$1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots = \frac{\pi^2}{6}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <plus/>
      < cn> 1 </ cn>
      <apply> <divide/>
        <cn> 1 </cn>
        <apply> <power/>
          <cn> 2 </cn>
          <cn> 2 </cn>
        </apply>
      </apply>
      <apply> <divide/>
        <cn> 1 </cn>
        <apply> <power/>
          <cn> 3 </cn>
          <cn> 2 </cn>
        </apply>
      </apply>
      <apply> <divide/>
        < cn > 1 < / cn >
        <apply> <power/>
          <cn> 4 </cn>
          <cn> 2 </cn>
        </apply>
      </apply>
      <ci> &cdots; </ci>
    </apply>
    <apply> <divide/>
      <apply> <power/>
        <ci> &pi; </ci>
        <cn> 2 </cn>
      </apply>
      <cn> 6 </cn>
    </apply>
 </apply>
```

Series: pc-s-002

$$1 - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                              <cn> 12 </cn>
  <apply> <eq/>
                                                            </apply>
    <apply> <plus/>
                                                          </apply>
                                                        < cn> 1 </ cn>
      <apply> <minus/>
        <apply> <divide/>
          < cn> 1 </ cn>
          <apply> <power/>
            <cn> 2 </cn>
            <cn> 2 </cn>
          </apply>
        </apply>
      </apply>
      <apply> <divide/>
        <cn> 1 </cn>
        <apply> <power/>
          <cn> 3 </cn>
          <cn> 2 </cn>
        </apply>
      </apply>
      <apply> <minus/>
        <apply> <divide/>
          < cn> 1 </ cn>
          <apply> <power/>
            <cn> 4 </cn>
            <cn> 2 </cn>
          </apply>
        </apply>
      </apply>
      <ci> &cdots; </ci>
    </apply>
    <apply> <divide/>
      <apply> <power/>
        <ci> &pi; </ci>
        <cn> 2 </cn>
      </apply>
```

$\forall x \in \left[e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!} + \dots \right]$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                                <apply> <divide/>
 <apply> <forall/>
                                                                  <apply> <power/>
    <condition>
                                                                    <ci> x </ci>
     <apply> <in/>
                                                                    <ci> n </ci>
        <ci> x </ci>
                                                                  </apply>
        <ci> &reals; </ci>
                                                                  <apply> <factorial/>
                                                                    <ci> n </ci>
     </apply>
    </condition>
                                                                  </apply>
    <apply> <eq/>
                                                                </apply>
     <apply> <power/>
                                                                <ci> &cdots; </ci>
        <ci> &exponentiale; </ci>
                                                              </apply>
        <ci> x </ci>
                                                            </apply>
     </apply>
                                                          </apply>
     <apply> <plus/>
                                                        < cn> 1 </ cn>
        <ci> x </ci>
        <apply> <divide/>
          <apply> <power/>
            <ci> x </ci>
            <cn> 2 </cn>
          </apply>
          <apply> <factorial/>
            <cn> 2 </cn>
          </apply>
        </apply>
        <apply> <divide/>
          <apply> <power/>
            <ci> x </ci>
            <cn> 3 </cn>
          </apply>
          <apply> <factorial/>
            <cn> 3 </cn>
          </apply>
        </apply>
        <ci> &cdots; </ci>
```

$\forall x \in \left[(e)^{-x} = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots + (-1)^n \frac{x^n}{n!} \dots \right]$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                                     <apply> <factorial/>
 <apply> <forall/>
                                                                       <cn> 3 </cn>
    <condition>
                                                                     </apply>
      <apply> <in/>
                                                                   </apply>
        <ci> x </ci>
                                                                 </apply>
        <ci> &reals; </ci>
                                                                 <ci> &cdots; </ci>
      </apply>
                                                                 <apply> <times/>
    </condition>
                                                                   <apply> <power/>
    <apply> <eq/>
                                                                     <apply> <minus/>
      <apply> <power/>
                                                                       < cn > 1 < / cn >
        <ci> &exponentiale; </ci>
                                                                     </apply>
                                                                     <ci> n </ci>
        <apply> <minus/>
          <ci> x </ci>
                                                                   </apply>
        </apply>
                                                                   <apply> <divide/>
      </apply>
                                                                     <apply> <power/>
      <apply> <plus/>
                                                                       <ci> x </ci>
        < cn> 1 </ cn>
                                                                       <ci> n </ci>
                                                                     </apply>
        <apply> <minus/>
          <ci> x </ci>
                                                                     <apply> <factorial/>
        </apply>
                                                                       <ci> n </ci>
        <apply> <divide/>
                                                                     </apply>
          <apply> <power/>
                                                                   </apply>
            <ci> x </ci>
                                                                   <ci> &cdots; </ci>
            <cn> 2 </cn>
                                                                 </apply>
          </apply>
                                                               </apply>
          <apply> <factorial/>
                                                             </apply>
            <cn> 2 </cn>
                                                          </apply>
          </apply>
                                                         </apply>
        <apply> <minus/>
          <apply> <divide/>
            <apply> <power/>
              <ci> x </ci>
              <cn> 3 </cn>
            </apply>
```

Logs

wh-l-001 wh-l-002 wh-l-003 wh-l-004

$\forall a > 0 \land b > 0 \mid \log_{g}(gab) = \log_{g}ga + \log_{g}gb$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <forall/>
    <condition>
      <apply> <and/>
        <apply> <qt/>
          <ci> a </ci>
          <cn> 0 </cn>
        </apply>
        <apply> <qt/>
          <ci> b </ci>
          < cn> 0 </cn>
        </apply>
      </apply>
    </condition>
    <apply> <eq/>
      <apply> <log/>
        <ld><logbase> <ci> g </ci> </logbase>
        <apply> <times/>
          <ci> a </ci>
          <ci> b </ci>
        </apply>
      </apply>
      <apply> <plus/>
        <apply> <log/>
          <logbase> <ci> g </ci> </logbase>
          <ci> a </ci>
        </apply>
        <apply> <log/>
          <ld><logbase> <ci> g </ci> </logbase>
          <ci> b </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\forall a > 0 \land b > 0 \mid \log_{g} g \frac{a}{b} = \log_{g} g a - \log_{g} g b$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <forall/>
    <condition>
      <apply> <and/>
        <apply> <qt/>
          <ci> a </ci>
          < cn> 0 </cn>
        </apply>
        <apply> <qt/>
          <ci> b </ci>
          < cn> 0 </cn>
        </apply>
      </apply>
    </condition>
    <apply> <eq/>
      <apply> <log/>
        <ld><logbase> <ci> g </ci> </logbase>
        <apply> <divide/>
          <ci> a </ci>
          <ci> b </ci>
        </apply>
      </apply>
      <apply> <minus/>
        <apply> <log/>
          <ld><logbase> <ci> g </ci> </logbase>
          <ci> a </ci>
        </apply>
        <apply> <log/>
          <ld><logbase> <ci> g </ci> </logbase>
          <ci> b </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

Logs: wh-l-002

$\forall b \in \land a > 0 \mid \log_g (ga^b) = b \log_g ga$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <forall/>
    <condition>
      <apply> <and/>
        <apply> <in/>
          <ci> b </ci>
          <ci> &reals; </ci>
        </apply>
        <apply> <qt/>
          <ci> a </ci>
          < cn> 0 </cn>
        </apply>
      </apply>
    </condition>
    <apply> <eq/>
      <apply> <log/>
        <ld><logbase> <ci> g </ci> </logbase>
        <apply> <power/>
          <ci> a </ci>
          <ci> b </ci>
        </apply>
      </apply>
      <apply> <times/>
        <ci> b </ci>
        <apply> <log/>
          <ld><logbase> <ci> g </ci> </logbase>
          <ci> a </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\forall a > 0 \mid \log_{\theta} ga = \frac{\log_{p} pa}{\log_{p} pg}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <forall/>
    <condition>
      <apply> <and/>
        <apply> <qt/>
          <ci> a </ci>
          < cn> 0 </cn>
        </apply>
      </apply>
    </condition>
    <apply> <eq/>
      <apply> <log/>
        <ld><logbase> <ci> g </ci> </logbase>
        <ci> a </ci>
      </apply>
      <apply> <divide/>
        <apply> <log/>
          <ld><logbase> <ci> p </ci> </logbase>
          <ci> a </ci>
        </apply>
        <apply> <log/>
          <ld><logbase> <ci> p </ci> </logbase>
          <ci> q </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

Goniometrics

wh-g-001	wh-g-005	wh-g-009	wh-g-013
wh-g-002	wh-g-006	wh-g-010	wh-g-014
wh-g-003	wh-g-007	wh-g-011	wh-g-015
wh-g-004	wh-g-008	wh-g-012	wh-g-016

$\sin(x+y) = \sin x \cos y + \cos x \sin y$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <sin/>
      <apply> <plus/>
        <ci> x </ci>
        <ci> y </ci>
      </apply>
    </apply>
    <apply> <plus/>
      <apply> <times/>
        <apply> <sin/>
          <ci> x </ci>
        </apply>
        <apply> <cos/>
          <ci> y </ci>
        </apply>
      </apply>
      <apply> <times/>
        <apply> <cos/>
          <ci> x </ci>
        </apply>
        <apply> <sin/>
          <ci> y </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\sin(x - y) = \sin x \cos y - \cos x \sin y$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <sin/>
      <apply> <minus/>
       <ci> x </ci>
       <ci> y </ci>
      </apply>
   </apply>
   <apply> <minus/>
      <apply> <times/>
       <apply> <sin/>
         <ci> x </ci>
        </apply>
        <apply> <cos/>
         <ci> y </ci>
       </apply>
     </apply>
      <apply> <times/>
       <apply> <cos/>
         <ci> x </ci>
        </apply>
       <apply> <sin/>
         <ci> y </ci>
       </apply>
      </apply>
   </apply>
 </apply>
```

$\cos(x+y) = \cos x \cos y - \sin x \sin y$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <cos/>
      <apply> <plus/>
        <ci> x </ci>
        <ci> y </ci>
      </apply>
    </apply>
    <apply> <minus/>
      <apply> <times/>
        <apply> <cos/>
          <ci> x </ci>
        </apply>
        <apply> <cos/>
          <ci> y </ci>
        </apply>
      </apply>
      <apply> <times/>
        <apply> <sin/>
          <ci> x </ci>
        </apply>
        <apply> <sin/>
          <ci> y </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\frac{\cos(x-y) = \cos x \cos y + \sin x \sin y}{\cos(x-y)}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <cos/>
      <apply> <minus/>
       <ci> x </ci>
       <ci> y </ci>
      </apply>
   </apply>
   <apply> <plus/>
      <apply> <times/>
       <apply> <cos/>
         <ci> x </ci>
        </apply>
        <apply> <cos/>
         <ci> y </ci>
       </apply>
     </apply>
      <apply> <times/>
       <apply> <sin/>
         <ci> x </ci>
        </apply>
       <apply> <sin/>
         <ci> y </ci>
       </apply>
      </apply>
   </apply>
 </apply>
```

$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
   <apply> <tan/>
      <apply> <plus/>
       <ci> x </ci>
       <ci> y </ci>
     </apply>
   </apply>
   <apply> <divide/>
      <apply> <plus/>
        <apply> <tan/>
          <ci> x </ci>
       </apply>
       <apply> <tan/>
          <ci> y </ci>
       </apply>
      </apply>
      <apply> <minus/>
        <cn> 1 </cn>
       <apply> <times/>
          <apply> <tan/>
            <ci> x </ci>
          </apply>
          <apply> <tan/>
            <ci> y </ci>
          </apply>
        </apply>
      </apply>
   </apply>
 </apply>
```

$\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
   <apply> <tan/>
      <apply> <minus/>
       <ci> x </ci>
       <ci> y </ci>
     </apply>
   </apply>
   <apply> <divide/>
      <apply> <minus/>
       <apply> <tan/>
          <ci> x </ci>
        </apply>
       <apply> <tan/>
          <ci> y </ci>
       </apply>
      </apply>
      <apply> <plus/>
        < cn> 1 </ cn>
       <apply> <times/>
          <apply> <tan/>
            <ci> x </ci>
          </apply>
          <apply> <tan/>
            <ci> y </ci>
          </apply>
        </apply>
      </apply>
   </apply>
 </apply>
```

$\sin p + \sin q = 2\sin \frac{p+q}{2}\cos \frac{p-q}{2}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <plus/>
      <apply> <sin/>
        <ci> p </ci>
      </apply>
      <apply> <sin/>
        <ci> q </ci>
      </apply>
    </apply>
    <apply> <times/>
      <cn> 2 </cn>
      <apply> <sin/>
        <apply> <divide/>
          <apply> <plus/>
            <ci> p </ci>
            <ci> q </ci>
          </apply>
          <cn> 2 </cn>
        </apply>
      </apply>
      <apply> <cos/>
        <apply> <divide/>
          <apply> <minus/>
            <ci> p </ci>
            <ci> q </ci>
          </apply>
          <cn> 2 </cn>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\sin p - \sin q = 2\cos \frac{p+q}{2}\sin \frac{p-q}{2}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <minus/>
      <apply> <sin/>
        <ci> p </ci>
      </apply>
      <apply> <sin/>
        <ci> q </ci>
      </apply>
    </apply>
    <apply> <times/>
      <cn> 2 </cn>
      <apply> <cos/>
        <apply> <divide/>
          <apply> <plus/>
            <ci> p </ci>
            <ci> q </ci>
          </apply>
          <cn> 2 </cn>
        </apply>
      </apply>
      <apply> <sin/>
        <apply> <divide/>
          <apply> <minus/>
            <ci> p </ci>
            <ci> q </ci>
          </apply>
          <cn> 2 </cn>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\cos p + \cos q = 2\cos\frac{p+q}{2}\cos\frac{p-q}{2}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <plus/>
      <apply> <cos/>
        <ci> p </ci>
      </apply>
      <apply> <cos/>
        <ci> q </ci>
      </apply>
    </apply>
    <apply> <times/>
      <cn> 2 </cn>
      <apply> <cos/>
        <apply> <divide/>
          <apply> <plus/>
            <ci> p </ci>
            <ci> q </ci>
          </apply>
          <cn> 2 </cn>
        </apply>
      </apply>
      <apply> <cos/>
        <apply> <divide/>
          <apply> <minus/>
            <ci> p </ci>
            <ci> q </ci>
          </apply>
          <cn> 2 </cn>
        </apply>
      </apply>
    </apply>
  </apply>
```

$\cos p - \cos q = -2\sin\frac{p+q}{2}\sin\frac{p-q}{2}$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <eq/>
    <apply> <minus/>
      <apply> <cos/>
        <ci> p </ci>
      </apply>
      <apply> <cos/>
        <ci> q </ci>
      </apply>
    </apply>
    <apply> <minus/>
      <apply> <times/>
        <cn> 2 </cn>
        <apply> <sin/>
          <apply> <divide/>
             <apply> <plus/>
              <ci> p </ci>
              <ci> q </ci>
            </apply>
            <cn> 2 </cn>
          </apply>
        </apply>
        <apply> <sin/>
          <apply> <divide/>
            <apply> <minus/>
              <ci> p </ci>
              <ci> q </ci>
            </apply>
            <cn> 2 </cn>
          </apply>
        </apply>
      </apply>
    </apply>
  </apply>
```

$2\sin\alpha\cos\beta = \sin(\alpha + \beta) + \sin(\alpha - \beta)$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <times/>
      <cn> 2 </cn>
      <apply> <sin/>
       <ci> &alpha; </ci>
      </apply>
      <apply> <cos/>
       <ci> &beta; </ci>
      </apply>
   </apply>
   <apply> <plus/>
      <apply> <sin/>
        <apply> <plus/>
         <ci> &alpha; </ci>
          <ci> &beta; </ci>
       </apply>
      </apply>
      <apply> <sin/>
       <apply> <minus/>
         <ci> &alpha; </ci>
         <ci> &beta; </ci>
       </apply>
      </apply>
   </apply>
  </apply>
```

$2\cos\alpha\sin\beta = \sin(\alpha + \beta) - \sin(\alpha - \beta)$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <times/>
      <cn> 2 </cn>
      <apply> <cos/>
       <ci> &alpha; </ci>
      </apply>
      <apply> <sin/>
       <ci> &beta; </ci>
      </apply>
   </apply>
   <apply> <minus/>
      <apply> <sin/>
        <apply> <plus/>
         <ci> &alpha; </ci>
          <ci> &beta; </ci>
       </apply>
      </apply>
      <apply> <sin/>
       <apply> <minus/>
         <ci> &alpha; </ci>
         <ci> &beta; </ci>
       </apply>
      </apply>
   </apply>
  </apply>
```

$2\cos\alpha\cos\beta = \cos(\alpha + \beta) + \cos(\alpha - \beta)$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <times/>
      <cn> 2 </cn>
      <apply> <cos/>
       <ci> &alpha; </ci>
      </apply>
      <apply> <cos/>
       <ci> &beta; </ci>
      </apply>
   </apply>
   <apply> <plus/>
      <apply> <cos/>
        <apply> <plus/>
         <ci> &alpha; </ci>
          <ci> &beta; </ci>
       </apply>
      </apply>
      <apply> <cos/>
       <apply> <minus/>
         <ci> &alpha; </ci>
         <ci> &beta; </ci>
       </apply>
      </apply>
   </apply>
  </apply>
```

$-2\sin\alpha\cos\beta = \sin(\alpha + \beta) - \sin(\alpha - \beta)$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
 <apply> <eq/>
   <apply> <minus/>
      <apply> <times/>
       <cn> 2 </cn>
       <apply> <sin/>
         <ci> &alpha; </ci>
       </apply>
       <apply> <cos/>
         <ci> &beta; </ci>
       </apply>
      </apply>
    </apply>
    <apply> <minus/>
      <apply> <sin/>
       <apply> <plus/>
          <ci> &alpha; </ci>
         <ci> &beta; </ci>
       </apply>
      </apply>
      <apply> <sin/>
       <apply> <minus/>
          <ci> &alpha; </ci>
         <ci> &beta; </ci>
       </apply>
     </apply>
    </apply>
 </apply>
```

$$\forall ABC \left| \frac{a}{\sin \alpha} + \frac{b}{\sin \beta} + \frac{c}{\sin \gamma} \right|$$

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
  <apply> <forall/>
    <condition>
      <mrow>
        <mi> &triangle; </mi>
        <mi> A </mi>
        <mi> B </mi>
        <mi> C </mi>
      </mrow>
    </condition>
    <apply> <plus/>
      <apply> <divide/>
        <ci> a </ci>
        <apply> <sin/>
          <ci> &alpha; </ci>
        </apply>
      </apply>
      <apply> <divide/>
        <ci> b </ci>
        <apply> <sin/>
          <ci> &beta; </ci>
        </apply>
      </apply>
      <apply> <divide/>
        <ci> c </ci>
        <apply> <sin/>
          <ci> &gamma; </ci>
        </apply>
      </apply>
    </apply>
  </apply>
```

```
\forall ABC \begin{vmatrix} a^2 = b^2 + c^2 - 2bc \cos \alpha \\ b^2 = a^2 + c^2 - 2ac \cos \beta \\ c^2 = a^2 + b^2 - 2ab \cos \gamma \end{vmatrix}
```

```
<math xmlns='http://www.w3c.org/mathml' version='2.0'>
                                                             </apply>
 <apply> <forall/>
                                                            <apply> <eq/>
    <condition>
                                                               <apply> <power/>
                                                                 <ci> b </ci>
      <mrow>
        <mi> &triangle; </mi>
                                                                 <cn> 2 </cn>
        <mi> A </mi>
                                                               </apply>
        <mi> B </mi>
                                                               <apply> <plus/>
        <mi> C </mi>
                                                                 <apply> <power/>
      </mrow>
                                                                   <ci> a </ci>
    </condition>
                                                                   <cn> 2 </cn>
    <apply> <eq/>
                                                                 </apply>
                                                                 <apply> <power/>
      <apply> <power/>
        <ci> a </ci>
                                                                   <ci> c </ci>
        <cn> 2 </cn>
                                                                   <cn> 2 </cn>
                                                                 </apply>
      </apply>
      <apply> <plus/>
                                                                 <apply> <minus/>
        <apply> <power/>
                                                                   <apply> <times/>
          <ci> b </ci>
                                                                     <cn> 2 </cn>
          <cn> 2 </cn>
                                                                     <ci> a </ci>
        </apply>
                                                                     <ci> c </ci>
        <apply> <power/>
                                                                     <apply> <cos/>
          <ci> c </ci>
                                                                       <ci> &beta; </ci>
          <cn> 2 </cn>
                                                                     </apply>
        </apply>
                                                                   </apply>
        <apply> <minus/>
                                                                 </apply>
          <apply> <times/>
                                                               </apply>
            < cn> 2 </cn>
                                                             </apply>
            <ci> b </ci>
                                                            <apply> <eq/>
            <ci> c </ci>
                                                               <apply> <power/>
            <apply> <cos/>
                                                                 <ci> c </ci>
                                                                 <cn> 2 </cn>
              <ci> &alpha; </ci>
            </apply>
                                                               </apply>
          </apply>
                                                               <apply> <plus/>
        </apply>
                                                                 <apply> <power/>
                                                                   <ci> a </ci>
      </apply>
```

```
<cn> 2 </cn>
       </apply>
       <apply> <power/>
         <ci> b </ci>
         <cn> 2 </cn>
       </apply>
       <apply> <minus/>
         <apply> <times/>
           <cn> 2 </cn>
           <ci> a </ci>
           <ci> b </ci>
           <apply> <cos/>
              <ci> &gamma; </ci>
           </apply>
         </apply>
       </apply>
     </apply>
    </apply>
  </apply>
```

Derivatives

$$\frac{\mathrm{d}a}{\mathrm{d}x} = 0$$

$$\frac{\mathrm{d}x}{\mathrm{d}x} = 1$$

$$\frac{\mathrm{d}au}{\mathrm{d}x} = a\frac{\mathrm{d}u}{\mathrm{d}x}$$

$$\frac{\mathrm{d}u + v + w}{\mathrm{d}x} = \frac{\mathrm{d}u}{\mathrm{d}x} + \frac{\mathrm{d}v}{\mathrm{d}x} + \frac{\mathrm{d}w}{\mathrm{d}x}$$

$$\frac{\mathrm{d}uv}{\mathrm{d}x} = u\frac{\mathrm{d}u}{\mathrm{d}x} + v\frac{\mathrm{d}v}{\mathrm{d}x}$$

$$\frac{\mathrm{d} u v w}{\mathrm{d} x} = u v \frac{\mathrm{d} w}{\mathrm{d} x} + v w \frac{\mathrm{d} u}{\mathrm{d} x} + u w \frac{\mathrm{d} v}{\mathrm{d} x}$$

$$\frac{\mathrm{d}\frac{u}{v}}{\mathrm{d}x} = \frac{v\frac{\mathrm{d}u}{\mathrm{d}x} - u\frac{\mathrm{d}v}{\mathrm{d}x}}{v^2} = \frac{1}{v}\frac{\mathrm{d}u}{\mathrm{d}x} - \frac{u}{v^2}\frac{\mathrm{d}v}{\mathrm{d}x}$$

$$\frac{\mathrm{d}u^n}{\mathrm{d}x} = n\left(u\right)^{n-1} \frac{\mathrm{d}u}{\mathrm{d}x}$$

$$\frac{\mathrm{d}\sqrt{u}}{\mathrm{d}x} = \frac{1}{2\sqrt{u}}\frac{\mathrm{d}u}{\mathrm{d}x}$$

$$\frac{\mathrm{d}\frac{1}{u}}{\mathrm{d}x} = -\frac{1}{u^2} \frac{\mathrm{d}u}{\mathrm{d}x}$$

$$\frac{\mathrm{d}\frac{1}{u^n}}{\mathrm{d}x} = -\frac{n}{(u)^{n+1}}\frac{\mathrm{d}u}{\mathrm{d}x}$$

$$\frac{\mathrm{d}}{\mathrm{d}x} = \frac{\mathrm{d}\log\left(u + \sqrt{u^2 + 1}\right)}{\mathrm{d}x} = \frac{1}{\sqrt{u^2 + 1}}\frac{\mathrm{d}u}{\mathrm{d}x}$$

$$\frac{\mathrm{d}\int\limits_{p}^{q}f(x,a)\,\mathrm{d}x}{\mathrm{d}a}$$

Integrals

$$\int \left(\frac{1}{x\sqrt{\pm a^2x^2}}\right) dx = -\frac{1}{a}\log\frac{a + \sqrt{\pm a^2x^2}}{x}$$

$$\int \left(\frac{1}{\cos(ax)(\pm 1\sin(ax))}\right) dx = \left(\mp \frac{1}{2a(\pm 1\sin(ax))}\right) + \frac{1}{2a}\log\tan\left(\frac{\pi}{4} + \frac{ax}{2}\right)$$

Series

$$1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$$

$$1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots = \frac{\pi^2}{6}$$

$$1 - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$$

$$\forall x \in \left[e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots + \frac{x^n}{n!} + \dots \right]$$

$$\forall x \in \left[(e)^{-x} = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots + (-1)^n \frac{x^n}{n!} \dots \right]$$

Logs

$$\forall a > 0 \land b > 0 \mid \log_{\theta}(gab) = \log_{\theta}ga + \log_{\theta}gb$$

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$$\forall a > 0 \land b > 0 \mid \log_{g} g \frac{a}{b} = \log_{g} g a - \log_{g} g b$$

$$\forall b \in \land a > 0 \mid \log_g (ga^b) = b \log_g ga$$

$$\forall a > 0 \mid \log_{g} ga = \frac{\log_{p} pa}{\log_{p} pg}$$

Goniometrics

$$\sin(x+y) = \sin x \cos y + \cos x \sin y$$

$$\sin(x - y) = \sin x \cos y - \cos x \sin y$$

$$\cos(x+y) = \cos x \cos y - \sin x \sin y$$

$$\cos(x - y) = \cos x \cos y + \sin x \sin y$$

$$\tan(x+y) = \frac{\tan x + \tan y}{1 - \tan x \tan y}$$

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$$\tan(x - y) = \frac{\tan x - \tan y}{1 + \tan x \tan y}$$

$$\sin p + \sin q = 2\sin \frac{p+q}{2}\cos \frac{p-q}{2}$$

$$\sin p - \sin q = 2\cos\frac{p+q}{2}\sin\frac{p-q}{2}$$

$$\cos p + \cos q = 2\cos\frac{p+q}{2}\cos\frac{p-q}{2}$$

$$\cos p - \cos q = -2\sin\frac{p+q}{2}\sin\frac{p-q}{2}$$

$$2\sin\alpha\cos\beta = \sin(\alpha + \beta) + \sin(\alpha - \beta)$$

$$2\cos\alpha\sin\beta = \sin(\alpha + \beta) - \sin(\alpha - \beta)$$

$$2\cos\alpha\cos\beta = \cos(\alpha+\beta) + \cos(\alpha-\beta)$$

$$-2\sin\alpha\cos\beta = \sin(\alpha + \beta) - \sin(\alpha - \beta)$$

$$\forall ABC \mid \frac{a}{\sin \alpha} + \frac{b}{\sin \beta} + \frac{c}{\sin \gamma}$$

$$\forall ABC \begin{vmatrix} a^{2} = b^{2} + c^{2} - 2bc \cos \alpha \\ b^{2} = a^{2} + c^{2} - 2ac \cos \beta \\ c^{2} = a^{2} + b^{2} - 2ab \cos \gamma \end{vmatrix}$$