

# Correctness Quiz 1

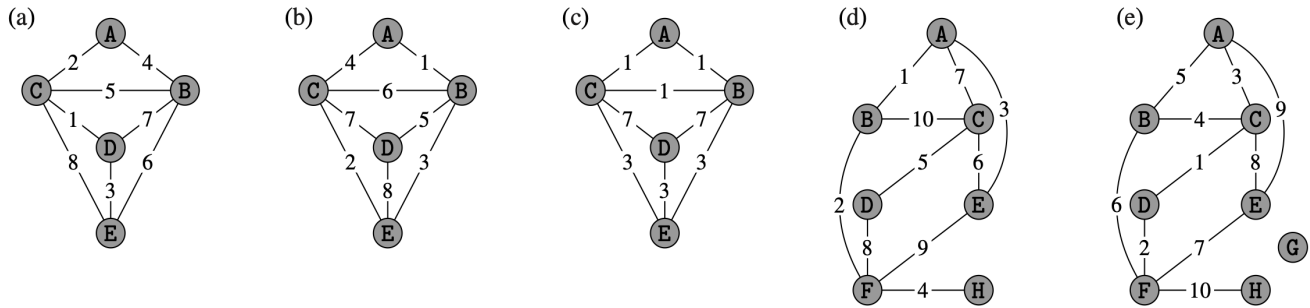
Discrete Structures 2

21 February 2023, 9am

Name: \_\_\_\_\_  
(please write legibly)

1. Prove or disprove: Let  $G = \langle L \cup R, E \rangle$  be an undirected bipartite graph with  $|L| = |R|$ . Suppose every node in the graph (that is, all nodes in  $L$  and  $R$ ) has at least one neighbor. Then the graph is connected.
2. Draw  $\mathcal{K}_3, \mathcal{K}_4$  and  $\mathcal{K}_5$ .
3. Consider an undirected graph  $G$  with  $n$  nodes. In terms of  $n$ , what is the longest *simple* cycle that  $G$  can contain? Give an example.

4. Identify a minimum spanning trees in each of the following graphs. If a minimum spanning tree does not exist explain why under the graph.



5. Match the term to its definition:

_____ isomorphic	(a) a graph (or subgraph) where all possible edges are present between all nodes
_____ acyclic	(b) a graph such that it is possible to draw the graph such that no edges cross
_____ clique	(c) a graph that does not contain any simple paths between nodes and themselves
_____ planar	(d) two graphs for which there is a mapping between nodes and all edge relationships are equivalent