Machine Learning

- Naïve Bayes Classifier is a probabilistic model
- It is based on Bayes theorem. It is called "naïve" due to the assumption that the features in the dataset are independent which may not be true in the real world.
- Despite this, the classifier performs well.
- It factors all available evidence in form of predictors into the Naïve Bayes rule to obtain more accurate probability
- Results in terms of class membership probabilities, such as the probability that a given sample belongs to a particular class.

- Bayes theorem is based on the concept of conditional probability.
- Conditional probability of an event, is the probability that the event will occur, given that something else has already occurred. For example, probability that an email is likely to be a spam given that the email contains words "lottery"

 Probability is chance of occurrence of an event. It's values is always between 0 and 1

$$P(A) = p/q \qquad P(H) = \frac{1}{2} \qquad H7$$

- Where
- p = number of ways that are favorable to the occurrence of A
- q = the total number of outcomes
- Questions:
 - What is the probability of getting a Head in toss of a coin?
 - What is the probability of getting score 2 when a die is rolled
 - · What is the probability of getting total score of 3 when 2 dice are rolled

Joint Probability – is the probability of multiple events occurring together. For example

- Probability of drawing an ace from a deck of cards 4/52
- Probability of drawing a red colour card from a deck of cards
- Probability of drawing a red colour ace P(Red and Ace) $P(\text{Red } \cap \text{Ace}) = P(\text{Red}) * P(\text{Ace})$ $= \frac{42}{52} \times \frac{24}{52} = \frac{2}{52}$

- Conditional Probability:
 - If you play on 20 of 30 day, then what is probability that you will play on a day?
 - Ans: P(play) = 20/30 = 2/3
 - If it is raining on the day, is the probability that you will play be the same?
 - Given that it is raining (an event has occurred), what is the probability that you will play? This is where conditional probability.
 - This is denoted as P(play | raining)

P(play given that it is raining)

Conditional Probability – it is the probability that an event given another event has occurred. For example,

- **Given the card drawn is red** (an event has occurred)
- What is the probability it is an ace (event not yet observed)?
- Since the card is reu, there interested in aces which is 2. Thus the conditional probability under the given red card is 2/26 \Rightarrow P (Red NAce) / P (Red Since the card is red, there are 26 red cards. Of these 26 possible values we are
- Given an event has occurred, the probability of the other event can be revised using following

following
$$P(A | B) = P(A \cap B) / P(B)$$

$$P(A \cap B) = P(A \cap B) + P(B) + A dq \cdot on B$$

$$P(A \cap B) = P(A) + P(B) \leftarrow A & B$$

$$P(A \cap B) = P(A) + P(B) \leftarrow A & B$$

$$P(A \cap B) = P(A) + P(B) \leftarrow A & B$$

$$P(A \cap B) = P(A) + P(B) \leftarrow A & B$$

Conditional Probability

centifyony talk

India Win India Lose Total

60)	40	100



What is the probability of India Win (IW)?

• P(IW) = 60/100



- What is the probability of Virat scoring a century (VC)?
 - P(VC) = 14/100

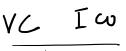


- What is the probability of India win and Virat scoring a century?
 - P(IW and VC) = P(IW ∩ VC) = 10/100



What is the probability of India Win, given that Virat has score century?

- P(IW | VC) = 10/14
- P(IW | VC) = 10/14 = (10/100) / (14/100) = P(IW ∩ VC) / P(VC)





$$\lambda$$



Bayes theorem

- $P(A \mid B) = P(A \cap B) / P(B)$
- $P(A \cap B) = P(A \mid B) * P(B)$
- But $P(A \cap B) = P(B \cap A)$
- Therefore,
- P(A | B) * P(B) = P(B | A) * P(A)

conditional probability · prior probability posterior probability = evidence

P(Mineral Tent Pos) = P(Test H.1 x P(BNA) = 12(B|A) * P(A)

Training Det

$$posterior\ probability = \frac{conditional\ probability \cdot prior\ probability}{evidence}$$

- P(A | B) = P(B | A) * P(A) / P(B)
- In the context of a classification problem, the Bayes theorem equation is: What is the probability that a particular object belongs to a class given its observed feature values? P (Canar Xi

$$w_i = Correct$$

$$w_i = Correct$$

$$w_i = P(\mathbf{x}_i \mid \mathbf{w}_j) \cdot P(\mathbf{w}_j)$$

$$P(\mathbf{w}_j \mid \mathbf{x}_i) = P(\mathbf{x}_i \mid \mathbf{w}_j) \cdot P(\mathbf{w}_j)$$

$$P(\mathbf{w}_i \mid \mathbf{x}_i) = P(\mathbf{x}_i \mid \mathbf{w}_j) \cdot P(\mathbf{w}_j)$$

- \mathbf{x}_i be the feature vector of sample $i, i \in \{1, 2, ..., n\}$,
- $\underline{\omega_j}$ be the notation of class $j, j \in \{1, 2, ..., m\}$,
- and $P(\mathbf{x}_i \mid \omega_j)$ be the probability of observing sample \mathbf{x}_i given that is belongs to class ω_i .

- Class is predicted based on maximum posterior probability of class
- If P(default | x_i) > P(not-default | x_i), then classify as "default" else classify as "not-default".
- If P(cancer | x_i) > P(not-cancer | x_i), then classify as "cancer" else classify as "healthy".

Page 11

For a d-dimensional features $(x_1, x_2... x_d)$, the class conditional probability

can be calculated as follows
$$P(\omega_{j} \mid \mathbf{x}_{i}) = \underbrace{\frac{P(\mathbf{x}_{i} \mid \omega_{j}) \cdot P(\omega_{j})}{P(\omega_{j})}}_{P(\mathbf{x}_{i} \mid \omega_{j}) \cdot P(\mathbf{x}_{d} \mid \omega_{j}) = \prod_{k=1}^{d} P(x_{k} \mid \omega_{j})}_{P(\mathbf{x}_{k} \mid \omega_{j}) \cdot P(\mathbf{x}_{d} \mid \omega_{j}) = \prod_{k=1}^{d} P(x_{k} \mid \omega_{j})}$$

Bayes classifier formula assumes independence of features.

©

Page 12

Exercise

Naïve Bayes Classifier

X 5

Gaussian NB

1 Continuous

MultinomedNB

Discovete

BernolliNB

Binary (o or 1)

Page 13

©

Missing Date > (1) Delete (Not the first choice)

2) Replace with Median, mean, much

3 Importation - R - MICE

Xn Regression to preduct missing X.

3 Special logic

X, X₂ -. 20-9 15-9.

= 910 1