

## Euler method

\*  $\frac{dy}{dx} = x^2 + y$ ;  $y(0) = 1$  to  $y(0.02)$ ,  $y(0.04)$  and  $y(0.06) = ?$

† From Euler method

$$y_{n+1} = y_n + h f(x_n, y_n)$$

here  $f(x, y) = x^2 + y$

$$x_0 = 0$$

$$y_0 = y(0) = 1$$

$$h = .01$$

Now

~~$$y_1 = y(0.01) = y(0) + .01 \times f(0, 1)$$~~

$$y_1 = y(0.01) = y(0) + .01 \times f(0, 1) = 1 + .01 \times 1 = 1.01$$

$$y_2 = y(0.02) = y(0.01) + .01 \times f(0.01, 1.01) = 1.0201$$

$$y_3 = y(0.03) = y(0.02) + .01 \times f(0.02, 1.0201) = 1.0303$$

$$y_4 = y(0.04) = y(0.03) + .01 \times f(0.03, 1.0303) = 1.0408$$

$$y_5 = y(0.05) = y(0.04) + .01 \times f(0.04, 1.0408) = 1.0510$$

$$y_6 = y(0.06) = y(0.05) + .01 \times f(0.05, 1.0510) = 1.0615$$